

Demystifying Bitcoin



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Have you heard about?

• Bitcoin

• Blockchain

• Ethereum

• Signatures

• Proof of work

• Smart contracts

• Turing Completeness

• NP vs P

• Consensus

• Snapshot



Perspectives

- ☞ **(1) The journalist**
- ☞ **(2) The user**
- ☞ **(3) The participant**
- ☞ **(4) The engineer**
- ☞ **(5) The scientist**

(1) The Journalist

- ☞ **2008: Financial crisis – Nakamoto (1/21m)**
 - **From 1c to 8000\$ through 20000\$**
- ☞ **From trading hardware to general trading**
- ☞ **2014: Ethereum (CH) - Now 800 \$**
- ☞ **2020: Libra - FacebookCoin**

Perspectives

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(2) The User

BLOCKCHAIN

🔔 🔄 [SIGN OUT](#)

[DASHBOARD](#)

Transactions

[BITCOIN](#)

[ETHER](#) New!

[BUY & SELL](#)

[SECURITY CENTER](#)

[SETTINGS](#)

[FAQ](#)

BE YOUR OWN BANK.®

🇧🇮 0.00000546 BTC | 🇪🇹 0.102338636803627092 ETH

[Send](#) [Request](#)

\$23.08

[Export Private Key](#)

[ALL](#) [SENT](#) [RECEIVED](#)

✓ SENT July 21 @ 10:10 AM	To: 0x9970b7e233555a037311be1f3261b59393d6981f From: My Ethereum Wallet	Add a description	0.0001 ETH
Transaction Confirmed ✓		Transaction Fee:	
> SENT July 18 @ 02:54 PM	To: 0x16a6920db1f14fc473325cf94a5e2d20c1fba868 From: My Ethereum Wallet	Add a description	0.0001416... ETH
> RECEIVED July 17 @ 11:44 AM	To: My Ethereum Wallet From: 0x3b0bc51ab9de1e5b7b6e34e5b960285805c41736	Add a description	0.08380039 ETH
> RECEIVED July 13 @ 03:03 PM	To: My Ethereum Wallet From: 0xeed16856d551569d134530ee3967ec79995e2051	test, hey jamiel! ✎	0.01966193 ETH

(2) The User

- ☞ **The wallet: 1 private key + several public keys**
- ☞ **Transaction validation**
 - signing + gossiping + mining + chaining
- ☞ **Transaction commitment**
 - After time t : thousands of users have seen it

(3) The Participant

Honey, I'm home!
I found a block today!

5	3			7				
6			1	9	5			
	9	8					6	
8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9



✦...Miner Jack...✦

(3) The Participant

Block:	<input type="text" value="0"/> <input type="text" value="1"/>
Nonce:	<input type="text" value="2790"/>
Data:	<input type="text" value="NCore"/>
Hash:	<input type="text" value="0000c5f693ac77a18ae73ace5df932457fc62e8dfa23c2f3c6d8ebb125ba7843"/>
	<input type="button" value="Mine"/>

(3) The Participant

- ☞ **To validate a transaction, a miner has to solve a puzzle including it**
 - **Fairness and cooperation**
- ☞ **Incentive: 12 bitcoins / puzzle**
 - **50 bitcoins 3 years ago**
- ☞ **Total: 21 millions bitcoins**
 - **Now: 17 millions**

(4) The Engineer

- Joinning (a P2P network)
- Signing (a transaction)
- Gossiping (the transaction)
- Gathering (a block)
- Mining (proof of work - nonce)
- Chaining (hash)
- Gossiping (the block)
- Committing/Aborting



TECHNOLOGIES OF A BLOCKCHAIN



Asymmetric Encryption

Transaction signing



Hash Functions

Transaction/block hashing as well as obfuscating public keys



Merkle Trees

Efficient way to package transactions into blocks



Key-Value Database

Lookups of previous transactions (prevent double-spends)



P2P Communication Protocol

Sharing transactions and blocks



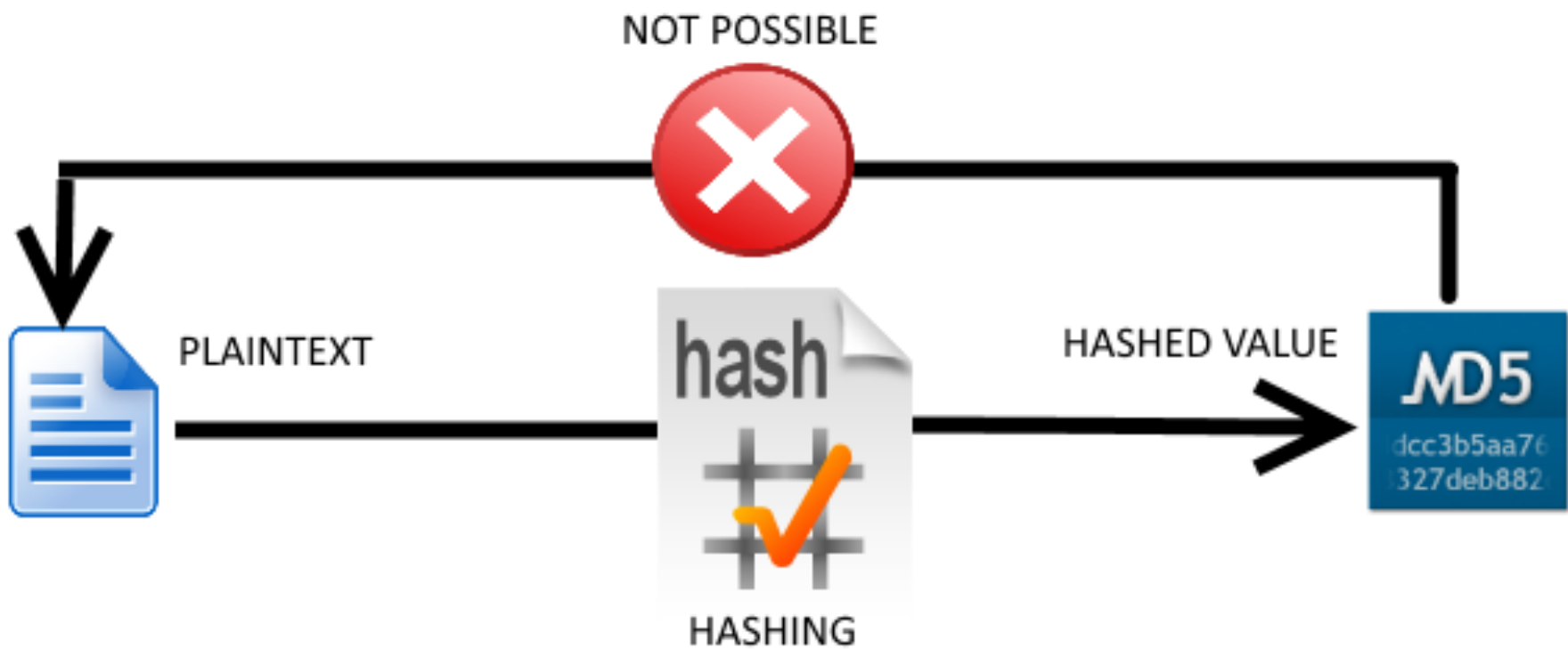
Proof of Work

Method to achieve consensus



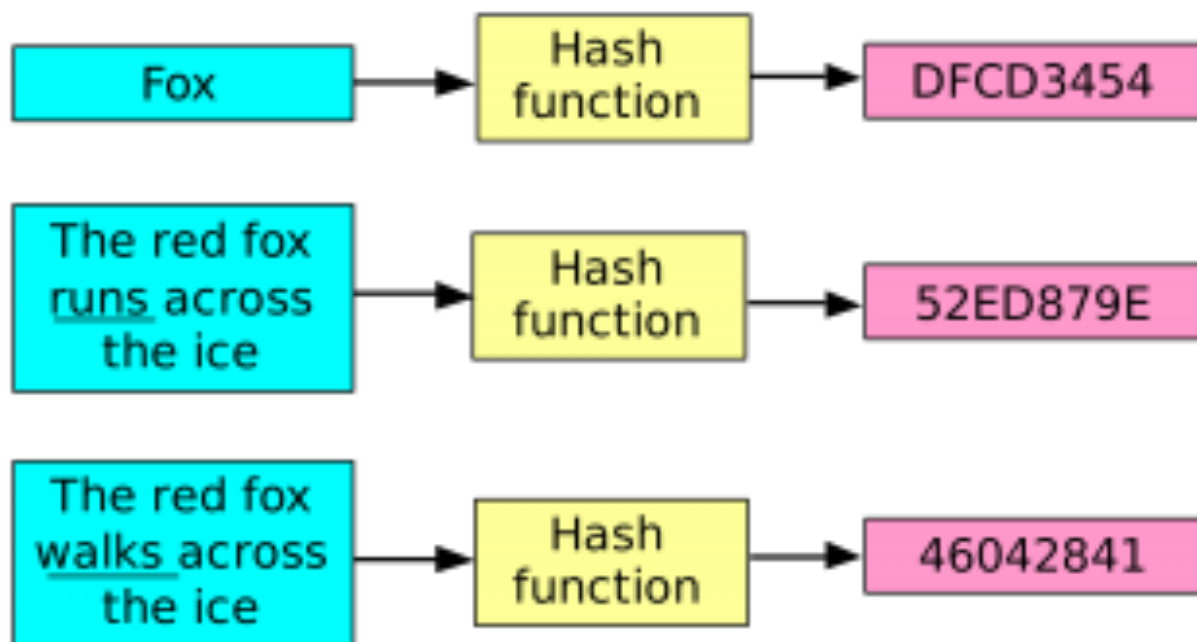
Hashing





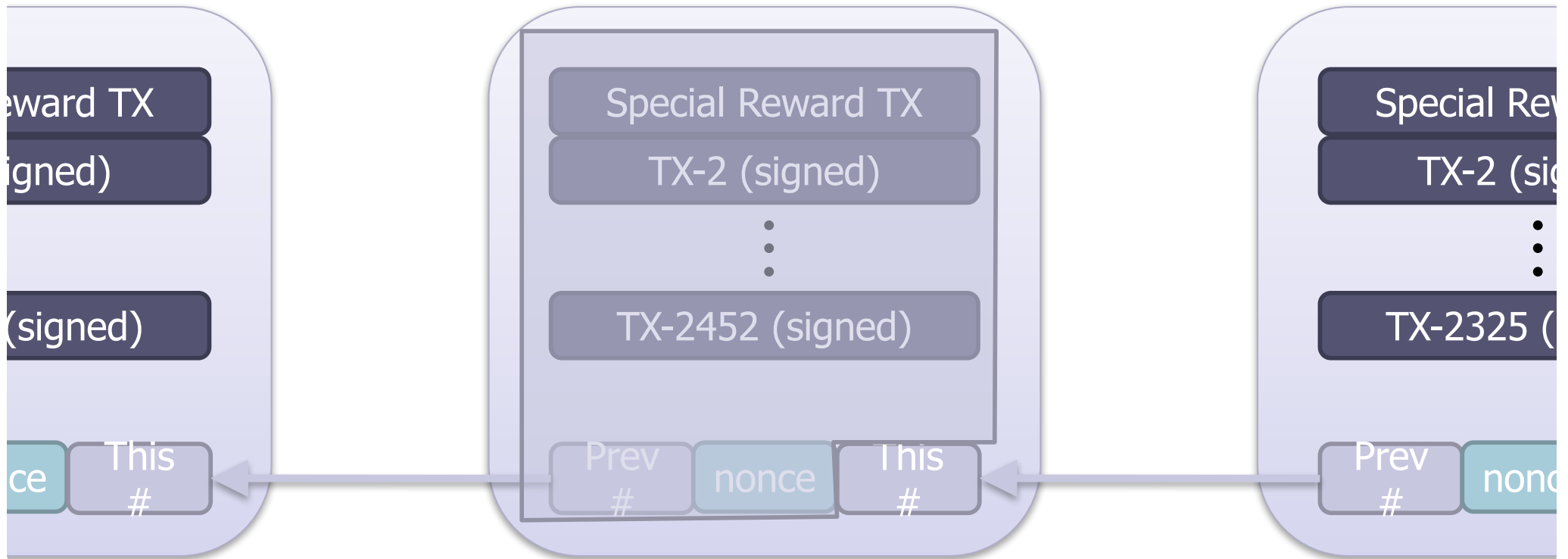
Input

Hash sum



The Big Picture

Bitcoin block



Mining: find **nonce** such that **This #** $< d$

How? By trying different nonces (brute force)

Block:

0 1

Nonce:

2790

Data:

[NCore](#)

Hash:

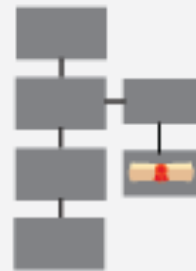
0000c5f693ac77a18ae73ace5df932457fc62e8dfa23c2f3c6d8ebb125ba7843

Mine

Smart Contracts



Option contract written as code into a blockchain.



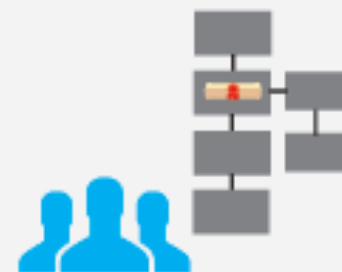
Contract is part of the public blockchain.



Parties involved in the contract are anonymous.



Contract executes itself when the conditions are met.



Regulators use blockchain to keep an eye on contracts.





```
33 partner_1 = contract.storage[I_PARTNER_1]
34 partner_2 = contract.storage[I_PARTNER_2]
35
36 if state == S_PROPOSED and tx.sender == partner_2 and tx.data[0] == partner_1:
37     contract.storage[I_STATE] = S_MARRIED
38
39 else if state == S_MARRIED and tx.sender == partner_1 or tx.sender == partner_2:
40     if tx.data[0] == TX_WITHDRAW:
41         creator = contract.storage[I_WITHDRAW_CREATOR]
42         if creator != 0 and contract.storage[I_WITHDRAW_TO] == tx.data[1] and contract.storage[I_WITHDRAW_AMOUNT] == tx.d
43             mktx(tx.data[1], tx.data[2], 0, 0)
44             contract.storage[I_WITHDRAW_TO] = 0
45             contract.storage[I_WITHDRAW_AMOUNT] = 0
46             contract.storage[I_WITHDRAW_CREATOR] = 0
47         else:
48             contract.storage[I_WITHDRAW_TO] = tx.data[1]
49             contract.storage[I_WITHDRAW_AMOUNT] = tx.data[2]
50             contract.storage[I_WITHDRAW_CREATOR] = tx.sender
51
52     else if tx.data[0] == TX_DIVORCE:
53         creator = contract.storage[I_DIVORCE_CREATOR]
54         if creator != 0 and creator != tx.sender:
55             balance = block.account_balance(contract.address)
56             mktx(partner_1, balance / 2, 0, 0)
57             mktx(partner_2, balance / 2, 0, 0)
58             contract.storage[I_STATE] = S_DIVORCED
```

Perspectives

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- ☞ **(5) The scientist**

(5) The Scientist

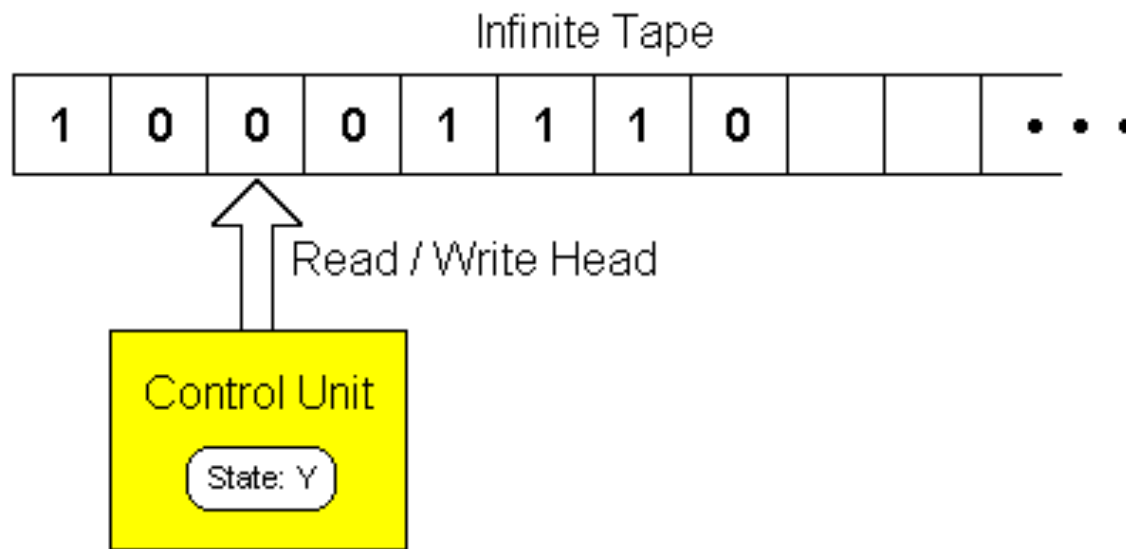
☛ **Conjecture 1: Turing Universality**

☛ **Conjecture 2: P is not NP**

☛ **Theorem 1: Lamport (Consensus) Universality**

☛ **Theorem 2: Consensus Impossibility**

Turing Universality (36)



P vs NP (Nash/GV 50 – Ford 70)

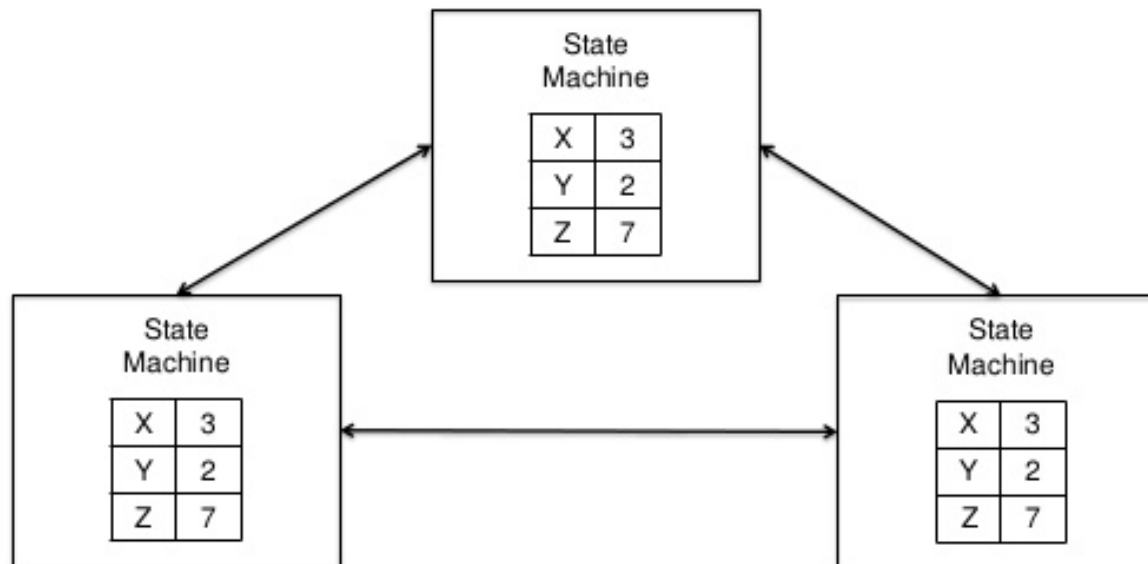
$$? * ? = 91$$

$$7 * 13 = ?$$

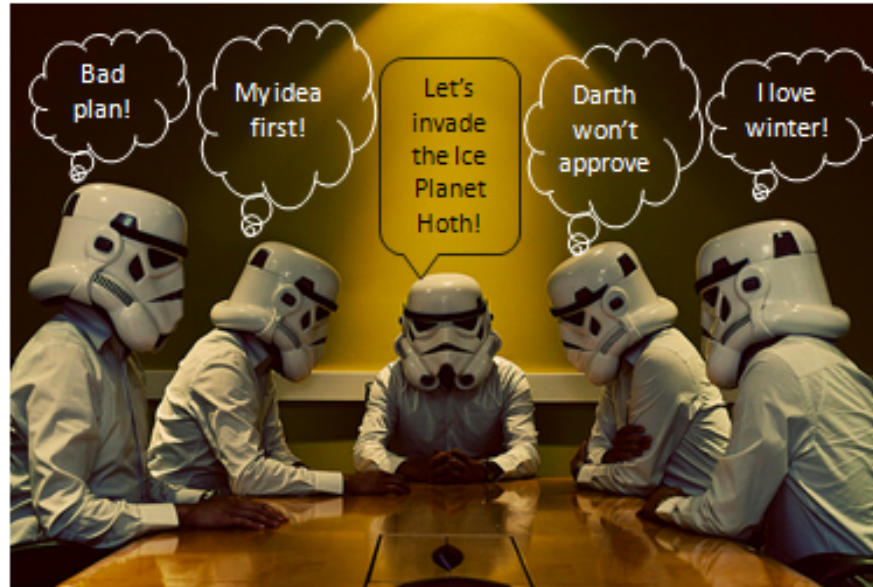
5	3			7				
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8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9

Lamport Universality (78)

Basic consensus



Consensus Universality (78)



Safety: No two nodes must choose different values.

The chosen value must have been proposed by a node.

Liveness: Each node must eventually choose a value.

Every service can be implemented in a highly available manner using Consensus

Consensus Impossibility (84)



Consensus is impossible in an asynchronous system

Perspectives

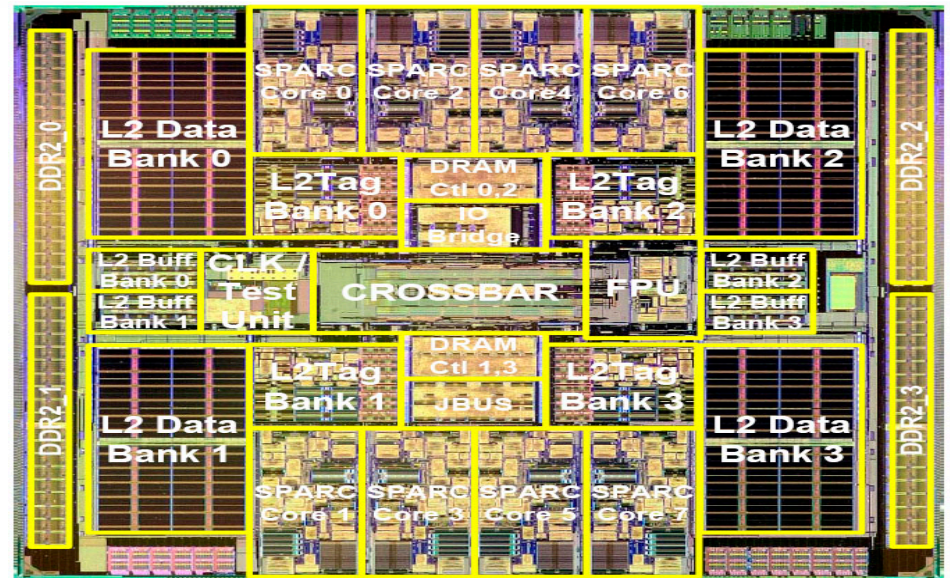
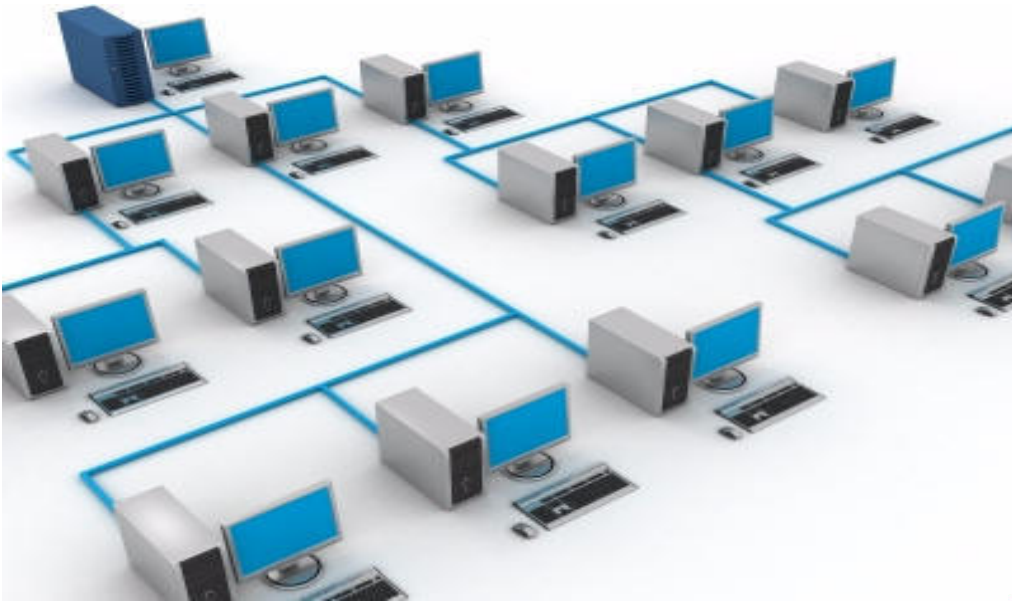
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Payment System



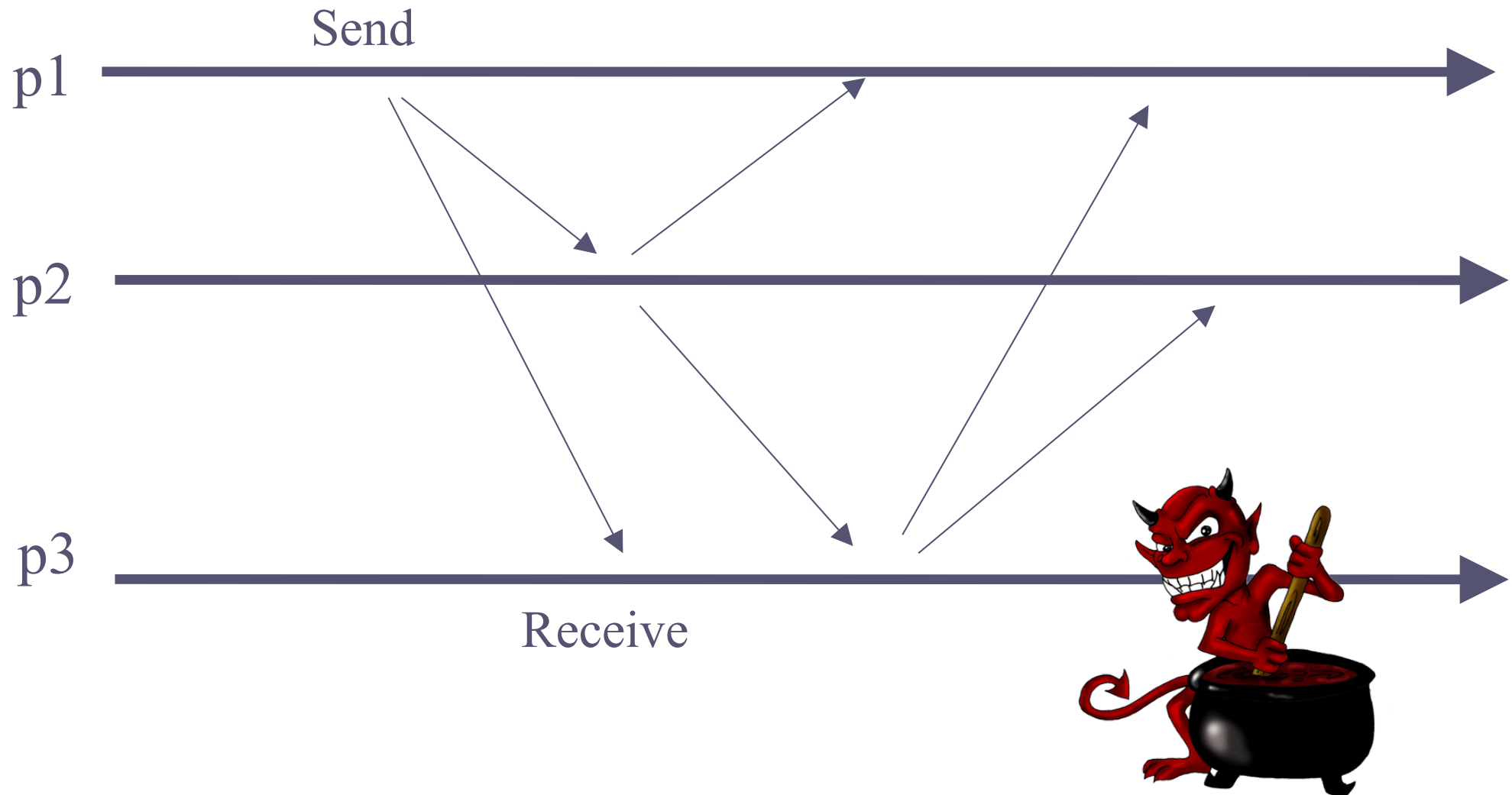
Can we implement a payment system asynchronously?

The infinitely big

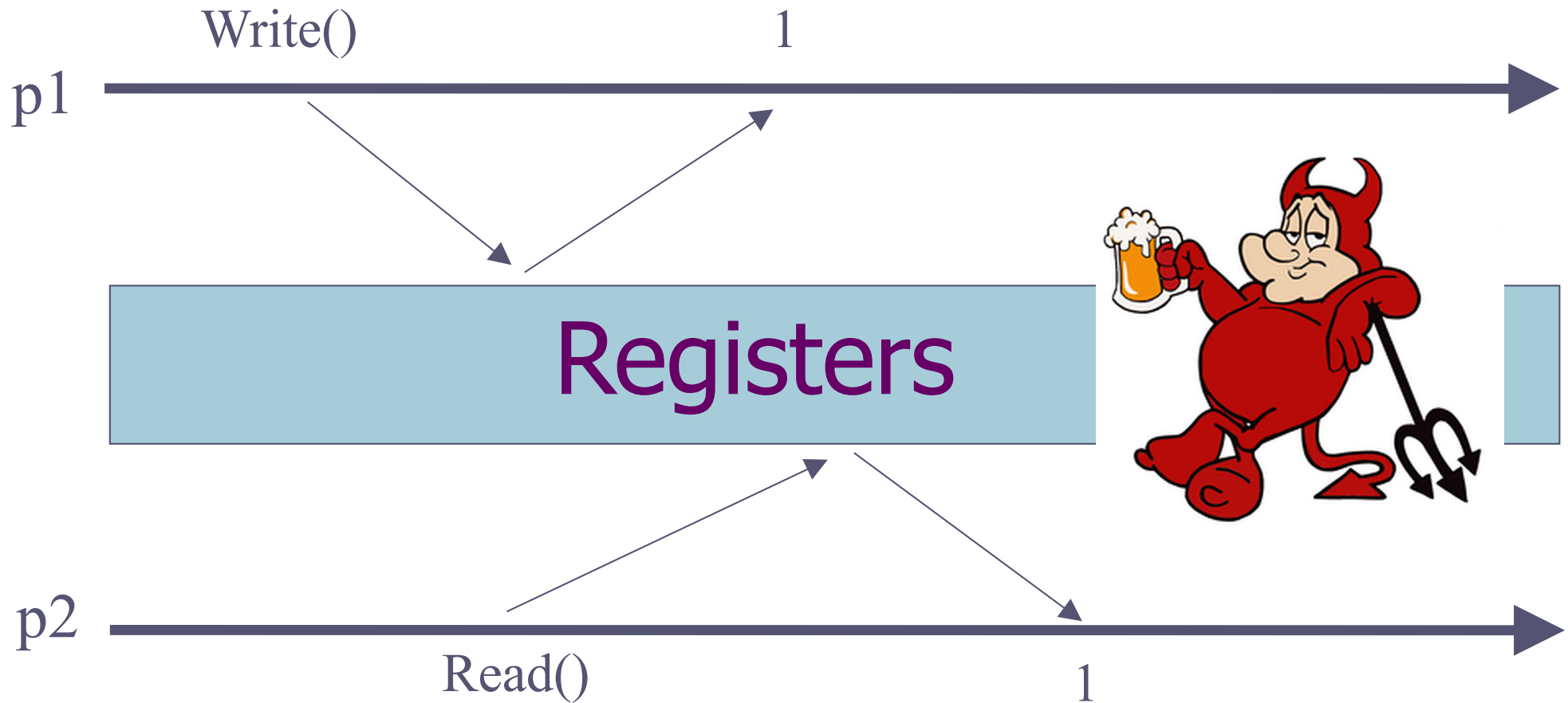


The infinitely small

Message Passing

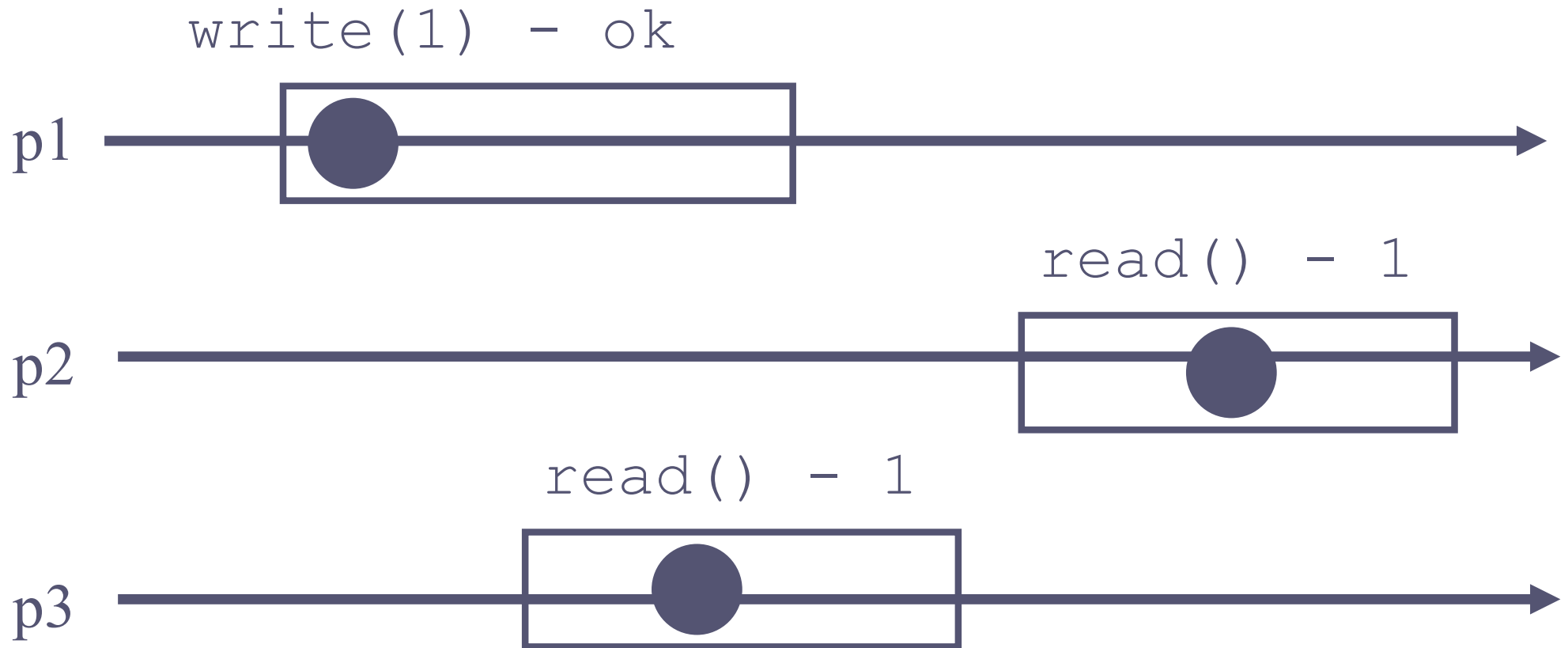


Shared Memory

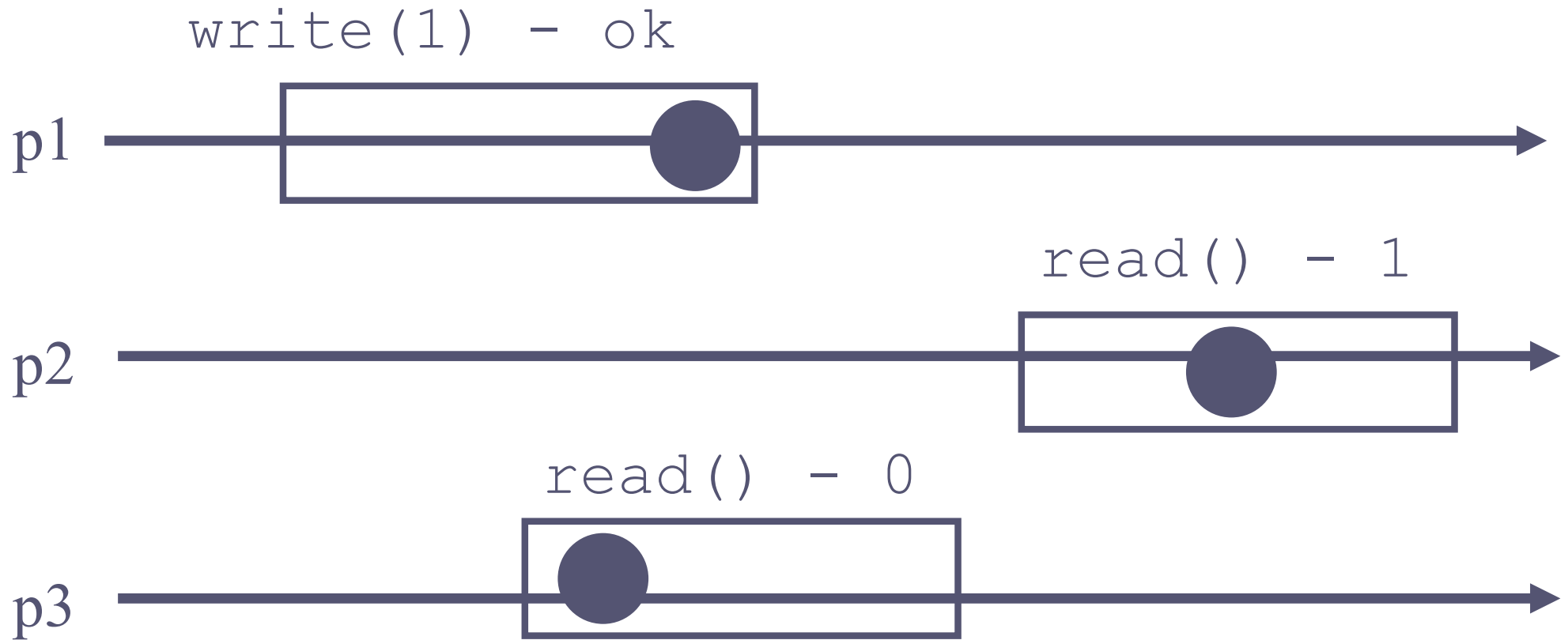


⇔ **Message Passing**

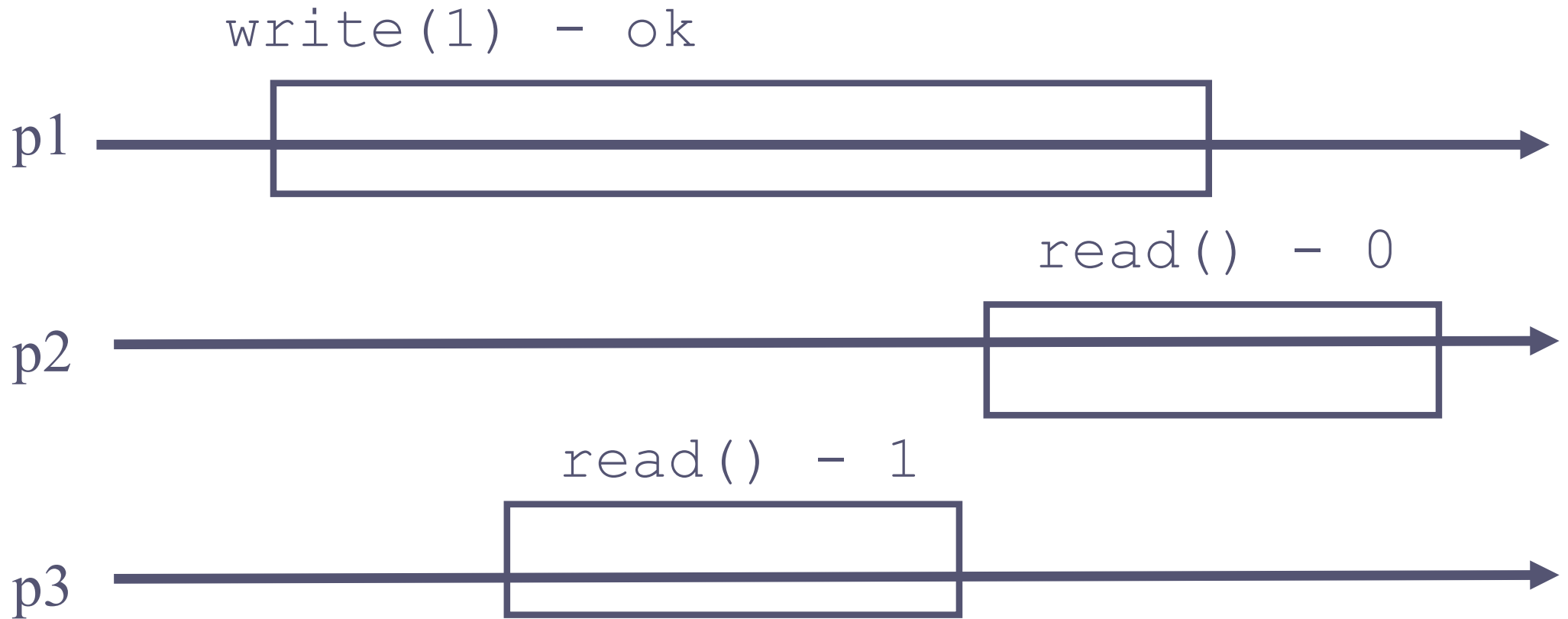
Atomic Shared Memory



Atomic Shared Memory



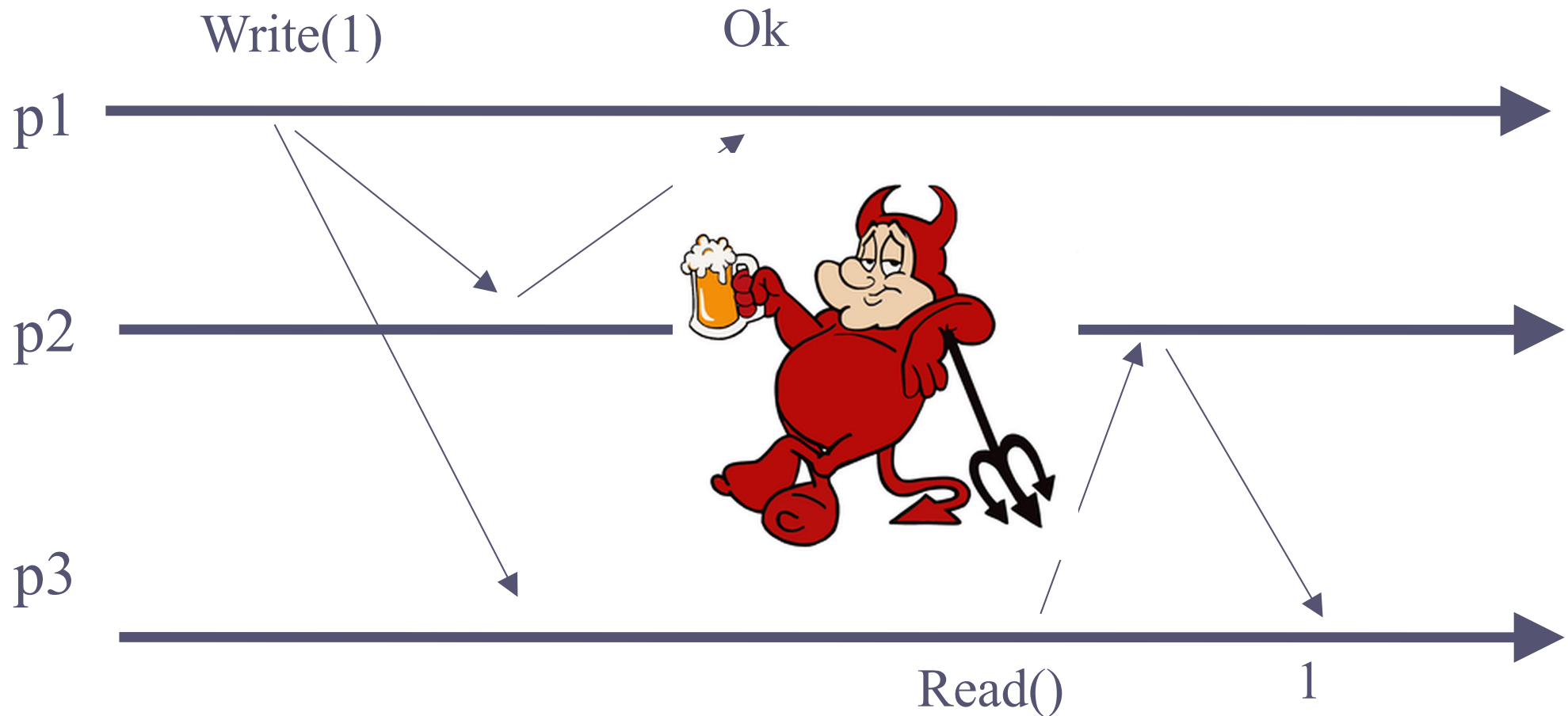
Non-Atomic Shared Memory



Non-Atomic Shared Memory

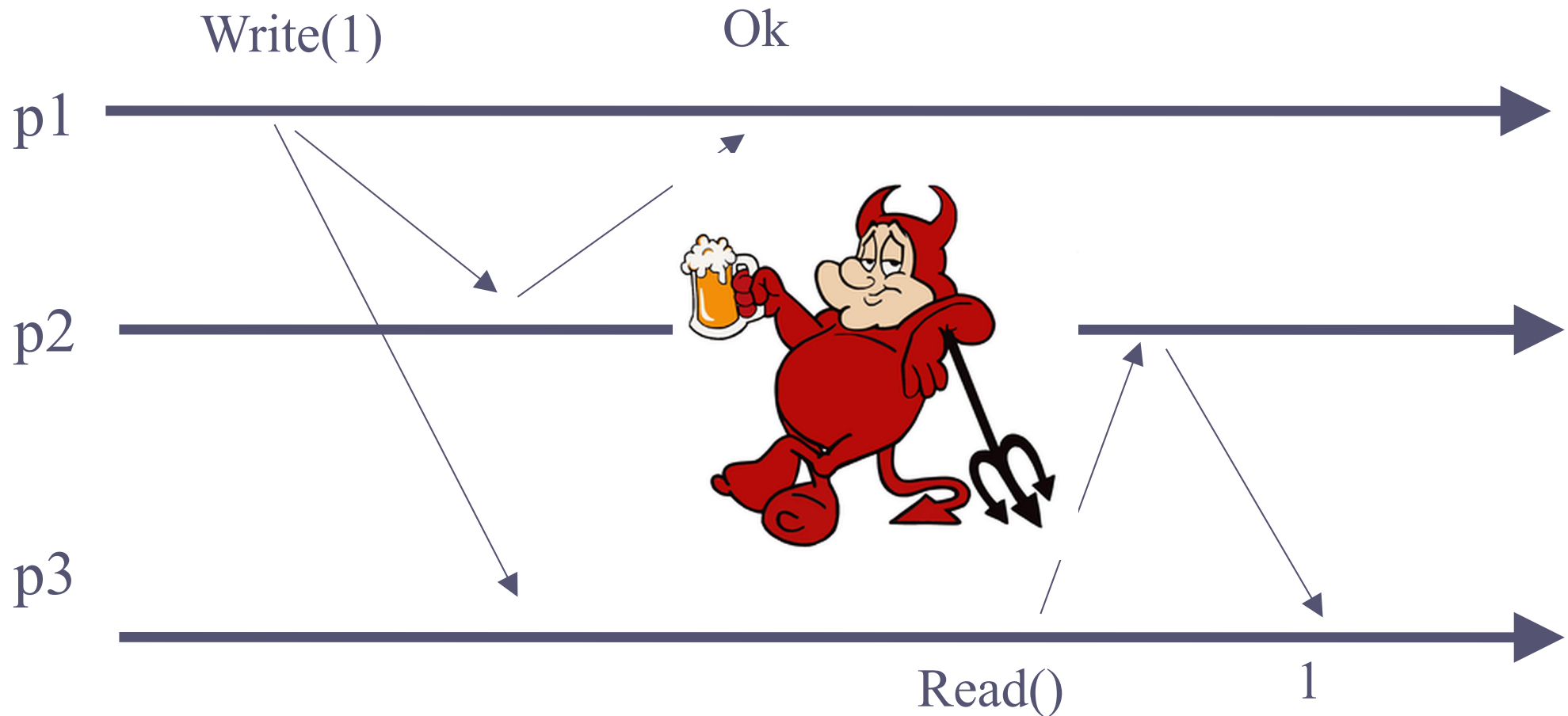


Message Passing \leftrightarrow Shared Memory



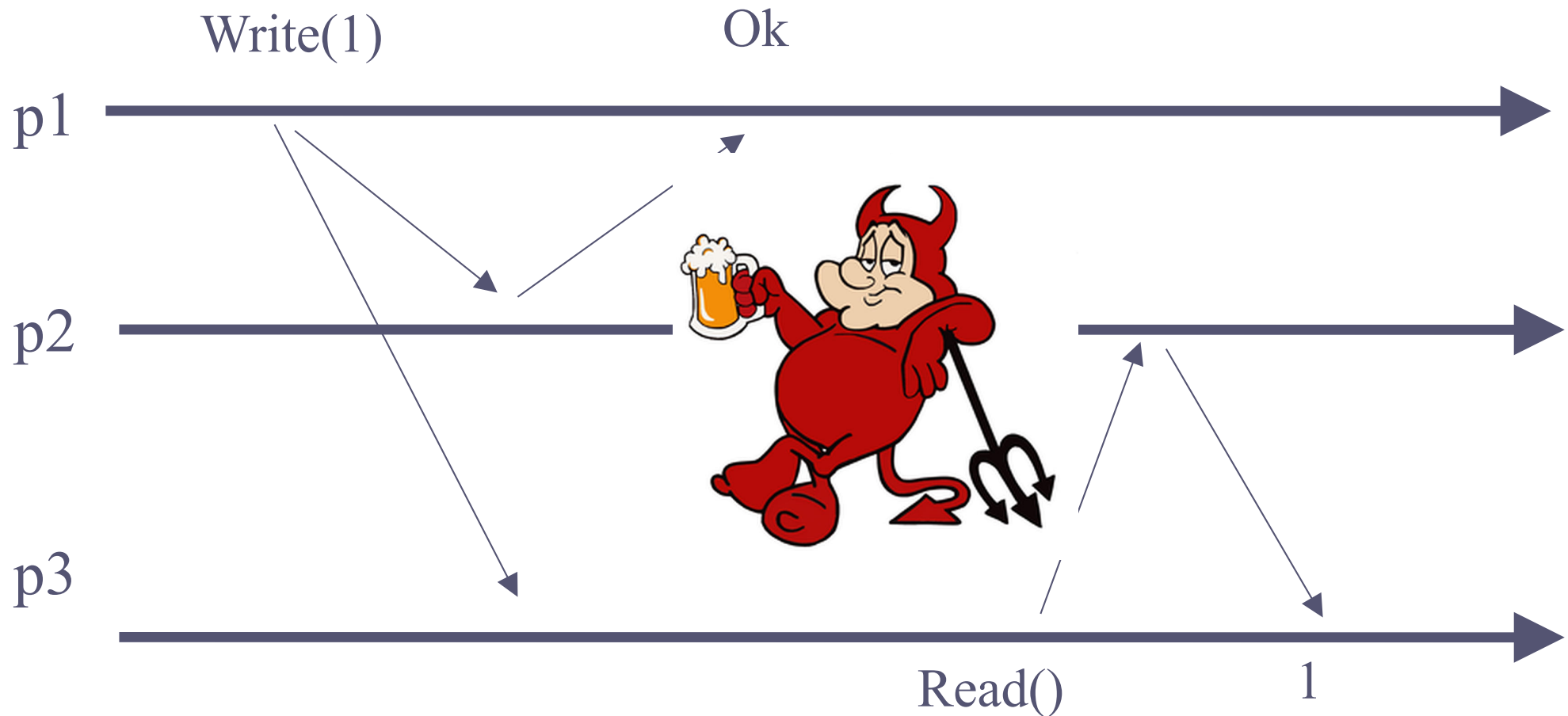
Quorums (asynchrony)

Message Passing \leftrightarrow Shared Memory



Quorums (asynchrony)

Message Passing \leftrightarrow Shared Memory



Quorums (asynchrony)

- ☛ « To understand a distributed computing problem: bring it to shared memory » T. Lannister



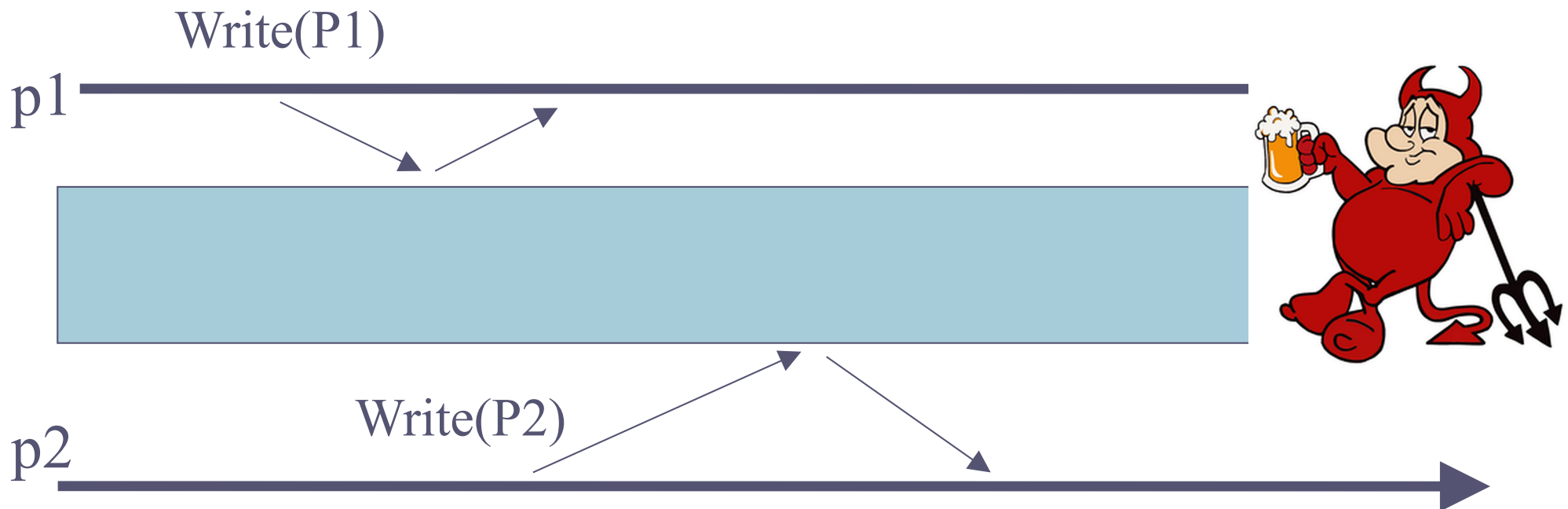
- ☛ « Optimization is the source of all evil » D. Knuth

P vs NP

$$7 * 13 = ?$$

$$? * ? = 91$$

Asynchronous vs Synchronous



Payment System



- Atomicity
- Wait-freedom

Can we implement a payment system asynchronously?

Counter: Specification

- A *counter* has two operations *inc()* and *read()*; it maintains an integer *x* *init to 0*
- *read()*:
 - return(*x*)
- *inc()*:
 - $x := x + 1;$
 - return(ok)

Counter: Algorithm

- The processes share an array of registers
Reg[1,...,N]
- *inc()*:
 - Reg[i].write(Reg[i].read() + 1);
 - return(ok)
- *read()*:
 - sum := 0;
 - for j = 1 to N do
 - sum := sum + Reg[j].read();
 - return(sum)

Counter*: Specification

- *Counter** has, in addition, operation *dec()*
- *dec()*:
 - if $x > 0$ then $x := x - 1$; return(ok)
 - else return(no)

Can we implement Counter*
asynchronously?

2-Consensus with Counter*

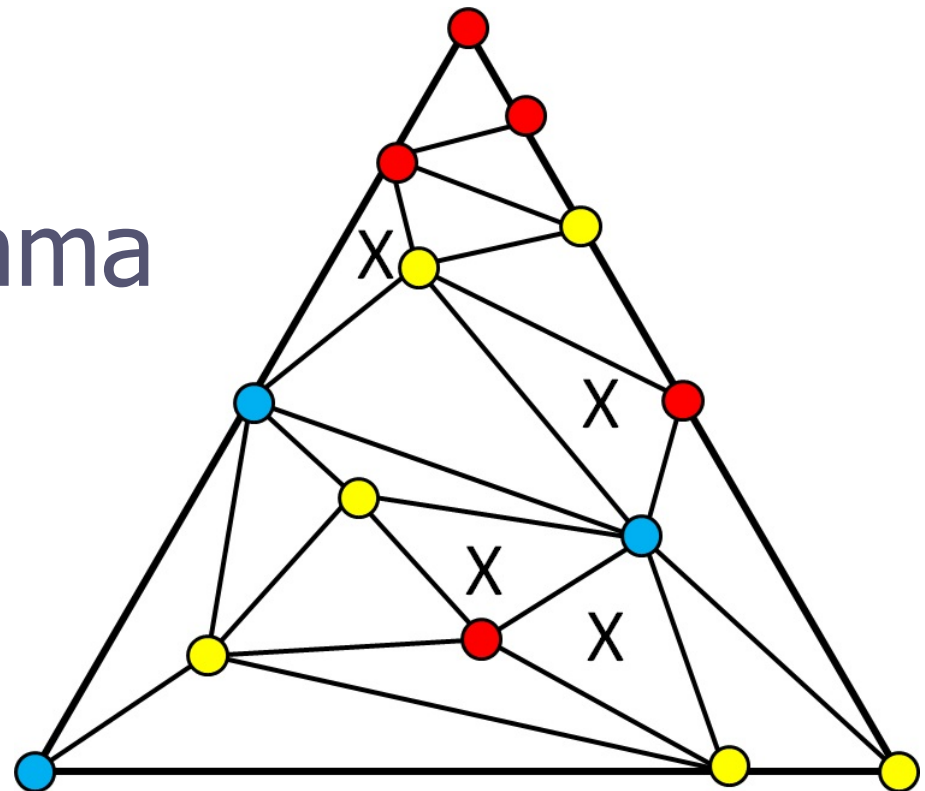
- Registers R0 and R1 and Counter* C - initialized to 1
- Process pI:
 - propose(vI)
 - RI.write(vI)
 - res := C.dec()
 - if(res = ok) then
 - ✓ return(vI)
 - ✓ else return(R{1-I}.read())

Impossibility [FLP85,LA87]

- **Theorem:** no *asynchronous* algorithm implements *consensus* among two processes using *registers*
- **Corollary:** no asynchronous algorithm implements Counter* among two processes using *registers*

- **Theorem:** no *asynchronous* algorithm implements *set-agreement* using *registers*

Sperner's Lemma



The **consensus number** of an object is the maximum number of processes than can solve consensus with it

Group →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	
Period ↓	1																		2
	1 H																		2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne	
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	
6	55 Cs	56 Ba	57 La *	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn	
7	87 Fr	88 Ra	89 Ac *	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og	
				* 58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu		
				* 90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr		

Payment Object (PO): Specification

- ☛ $\text{Pay}(a,b,x)$: transfer amount x from a to b if $a > x$ (return ok; else return no)
- ☛ NB. Only the owner of a invokes $\text{Pay}(a,*,*)$

- **Questions:** can PO be implemented asynchronously?
what is the consensus number of PO?

Payment Object (PO): Specification

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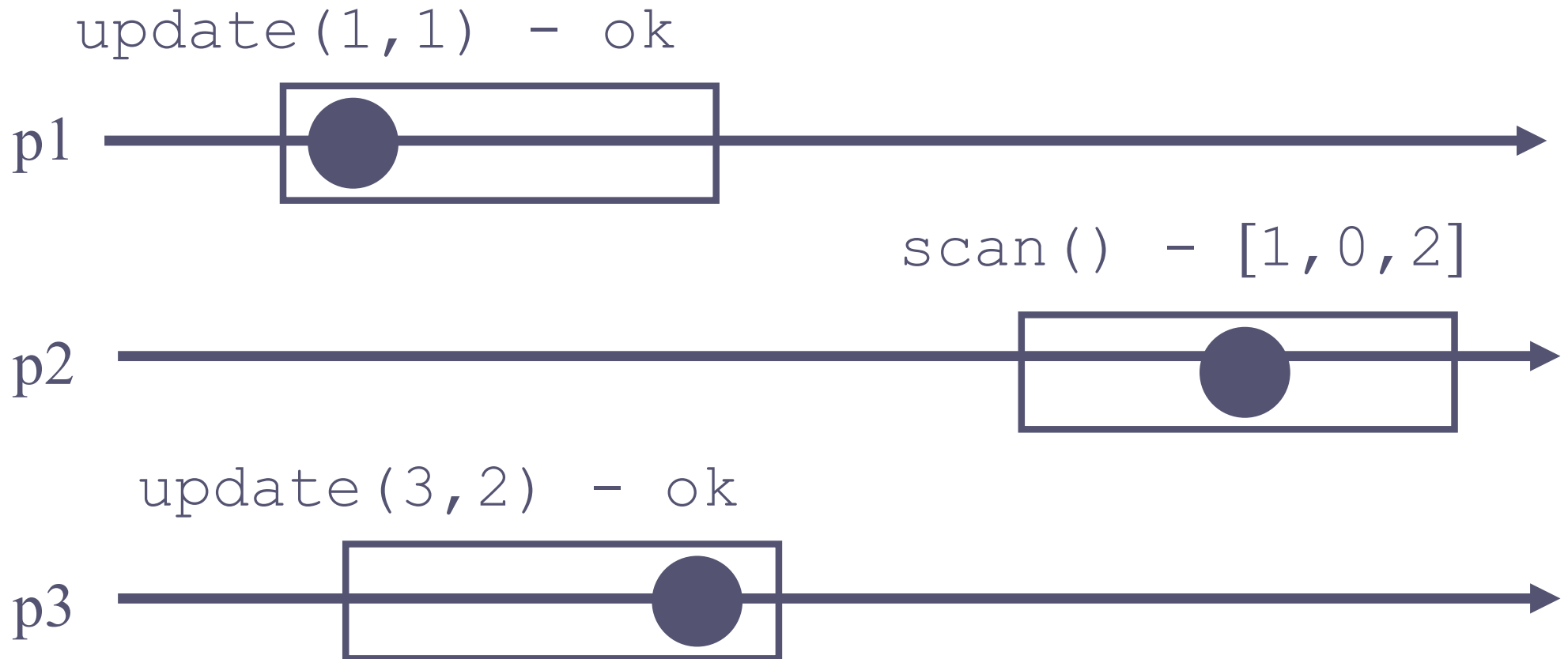
Snapshot: Specification

- A *snapshot* has operations *update()* and *scan()*; it maintains an array x of size N
- *scan()*:
 - return(x)
- *update(i, v)*:
 - $x[i] := v$;
 - return(ok)

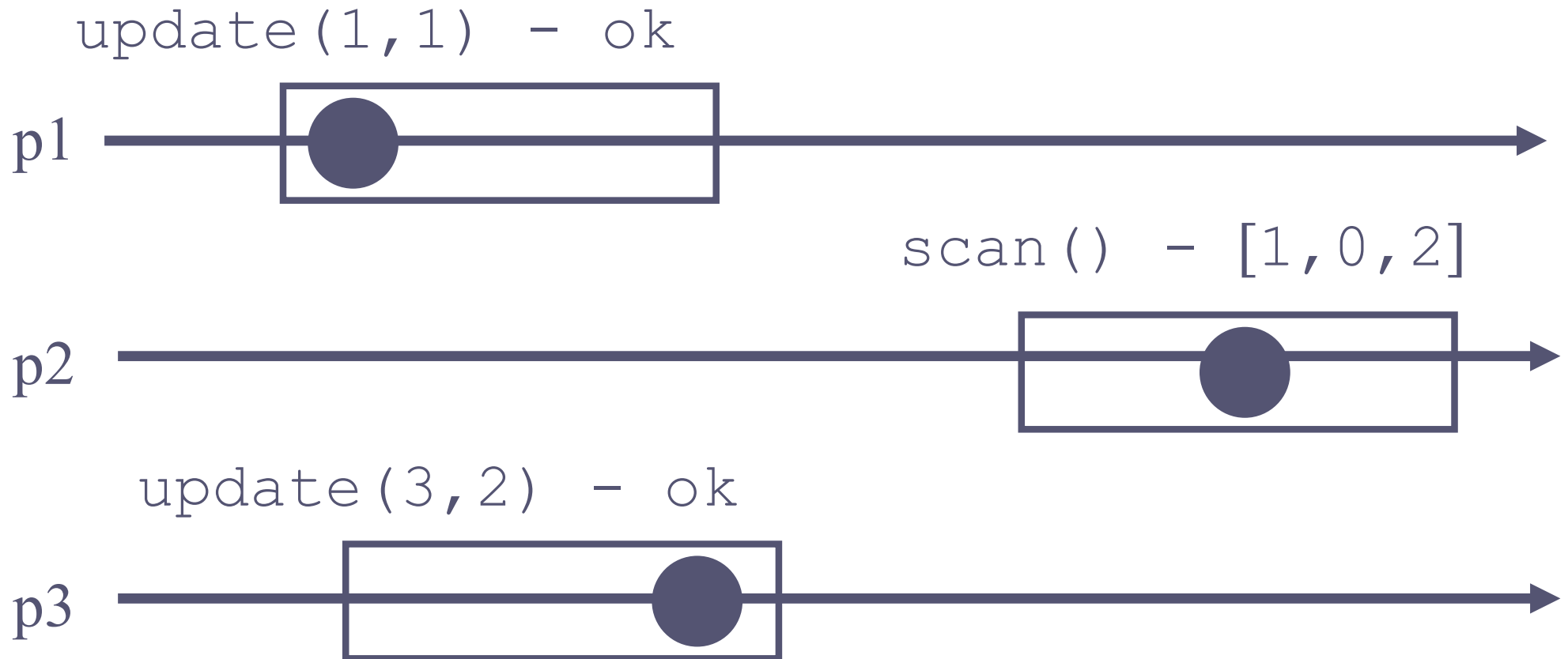
Algorithm?

- The processes share one array of N registers
Reg[1,...,N]
- *scan()*:
 - for j = 1 to N do
 - x[j] := Reg[j].read();
 - return(x)
- *update(i,v)*:
 - Reg[i].write(v); return(ok)

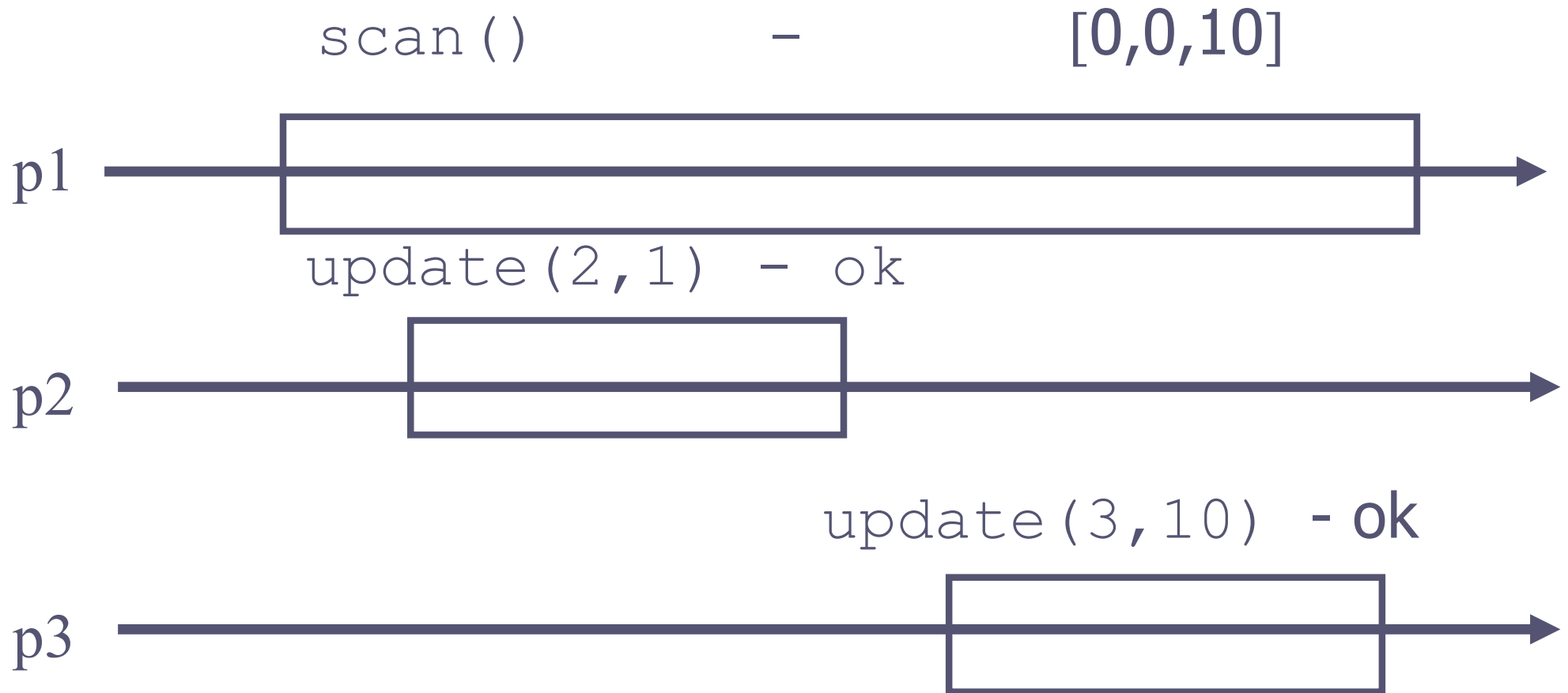
Atomicity?



Atomicity?



Atomicity?



Key idea for atomicity

- To *scan*, a process keeps reading the entire snapshot (i.e., *collecting*), until two arrays are the same

Key idea for wait-freedom

- To update, scan then write the value and the scan
- To *scan*, a process keeps collecting and returns a collect if it did not change, or some collect returned by a concurrent *scan*

The Payment Object: Algorithm

- Every process stores the sequence of its outgoing payments in its snapshot location
- To ***pay***, the process scans, computes its current balance: if bigger than the transfer, updates and returns ok, otherwise returns no
- To ***read***, scan and return the current balance

PO can be implemented Asynchronously

Consensus number of PO is 1

Consensus number of PO(k) is k

(5) The Scientist

- ☛ **Conjecture 1: Turing Universality**
- ☛ **Conjecture 2: P is not NP**
- ☛ **Theorem 1: Lamport (Consensus) Universality**
- ☛ **Theorem 2: Consensus Impossibility**
- ☛ **Theorem 3: $PO < Consensus$**

Payment System (AT2)

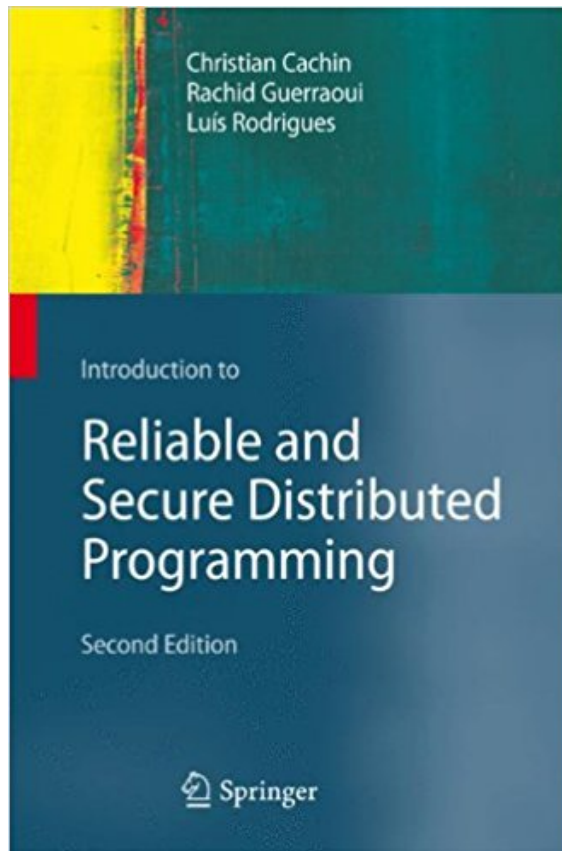
• AT2_S

• AT2_D

• AT2_R

- Number of lines of code: one order of magnitude less
- Latency: seconds (at most)

References



**ALGORITHMS
FOR CONCURRENT
SYSTEMS** Rachid Guerraoui
Petr Kuznetsov

