

# Distributed Algorithms

## Reliable Broadcast

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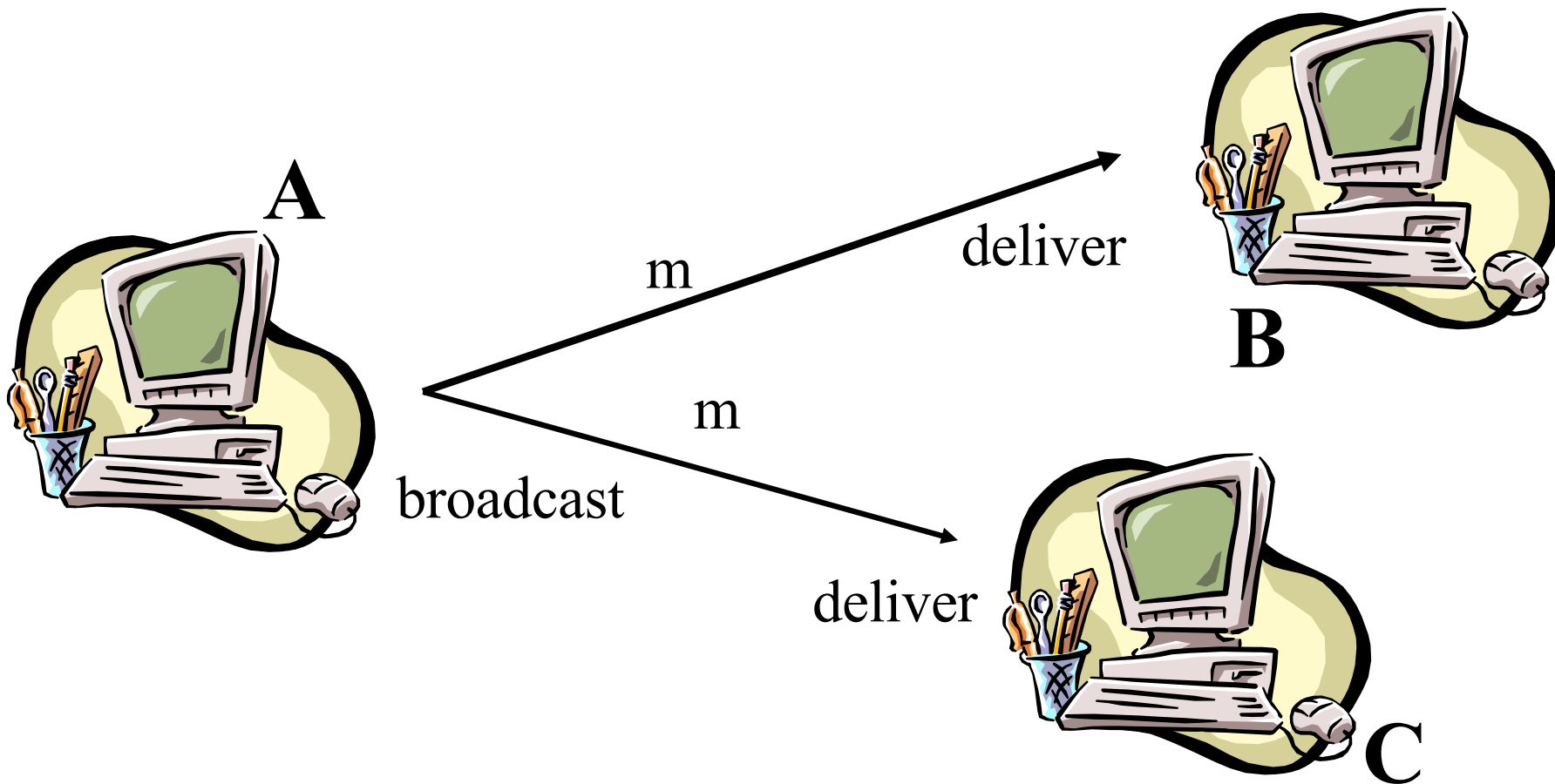


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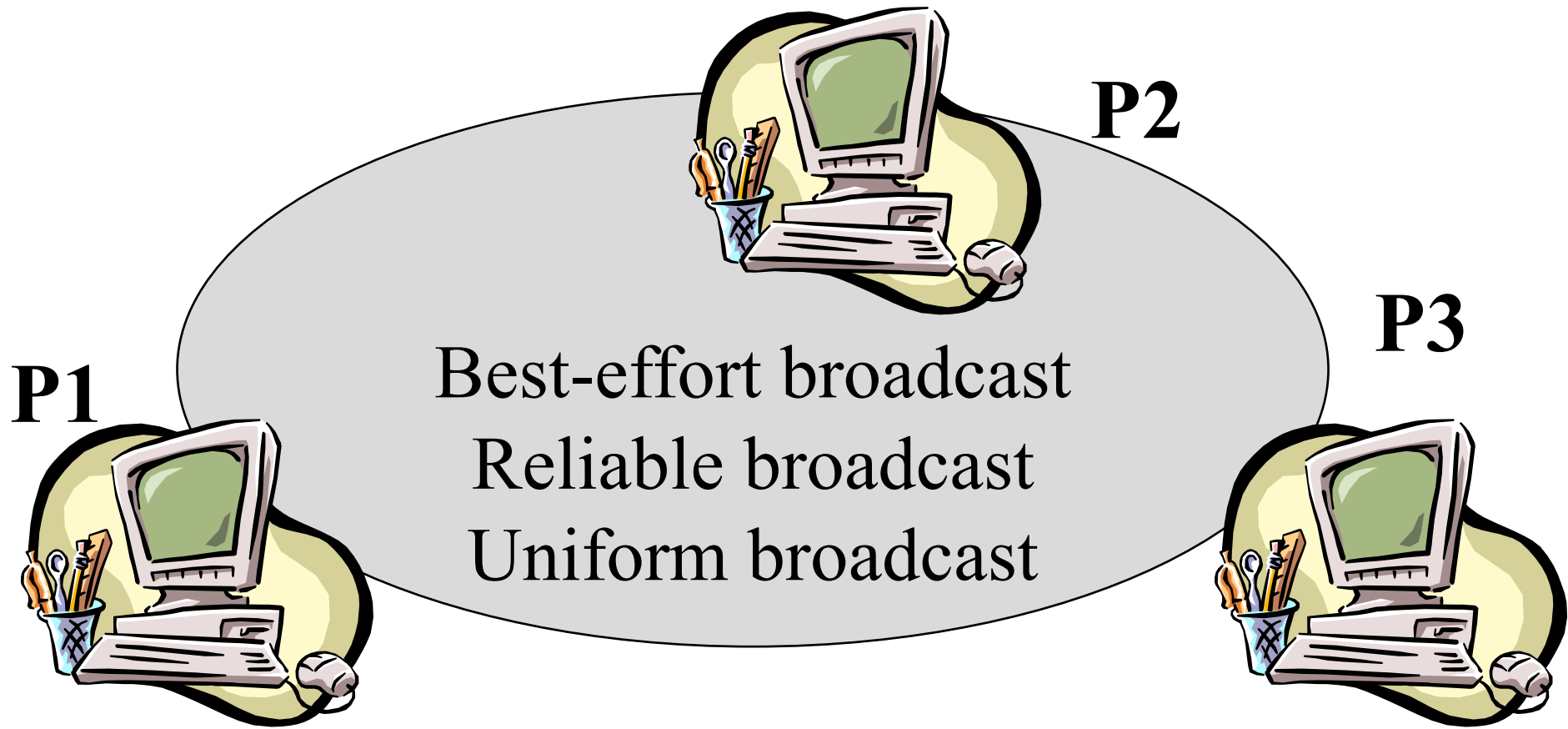
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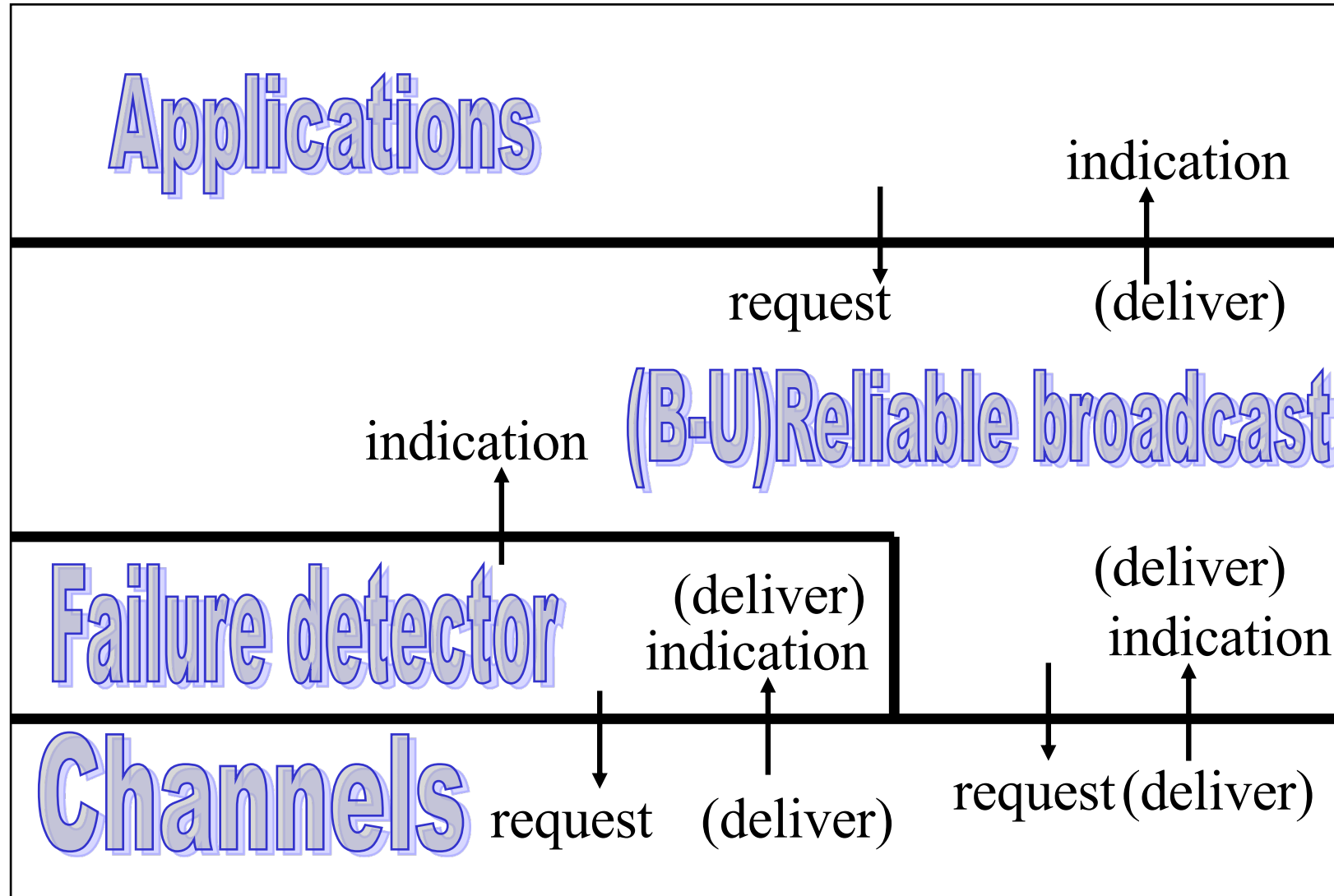
# Broadcast



# Broadcast abstractions



# Modules of a process



# Intuition

- Broadcast is useful for instance in applications where some processes subscribe to events published by other processes (e.g., stocks)
- The subscribers might require some **reliability** *guarantees* from the broadcast service (we say sometimes *quality of service* – *QoS*) that the underlying network does not provide

# Overview

- We shall consider three forms of reliability for a broadcast primitive
- **(1) *Best-effort broadcast***
- **(2) *(Regular) reliable broadcast***
- **(3) *Uniform (reliable) broadcast***
- We shall give first ***specifications*** and then ***algorithms***

# Best-effort broadcast (beb)

## • *Events*

• Request: <bebBroadcast, m>

• Indication: <bebDeliver, src, m>

• *Properties: BEB1, BEB2, BEB3*

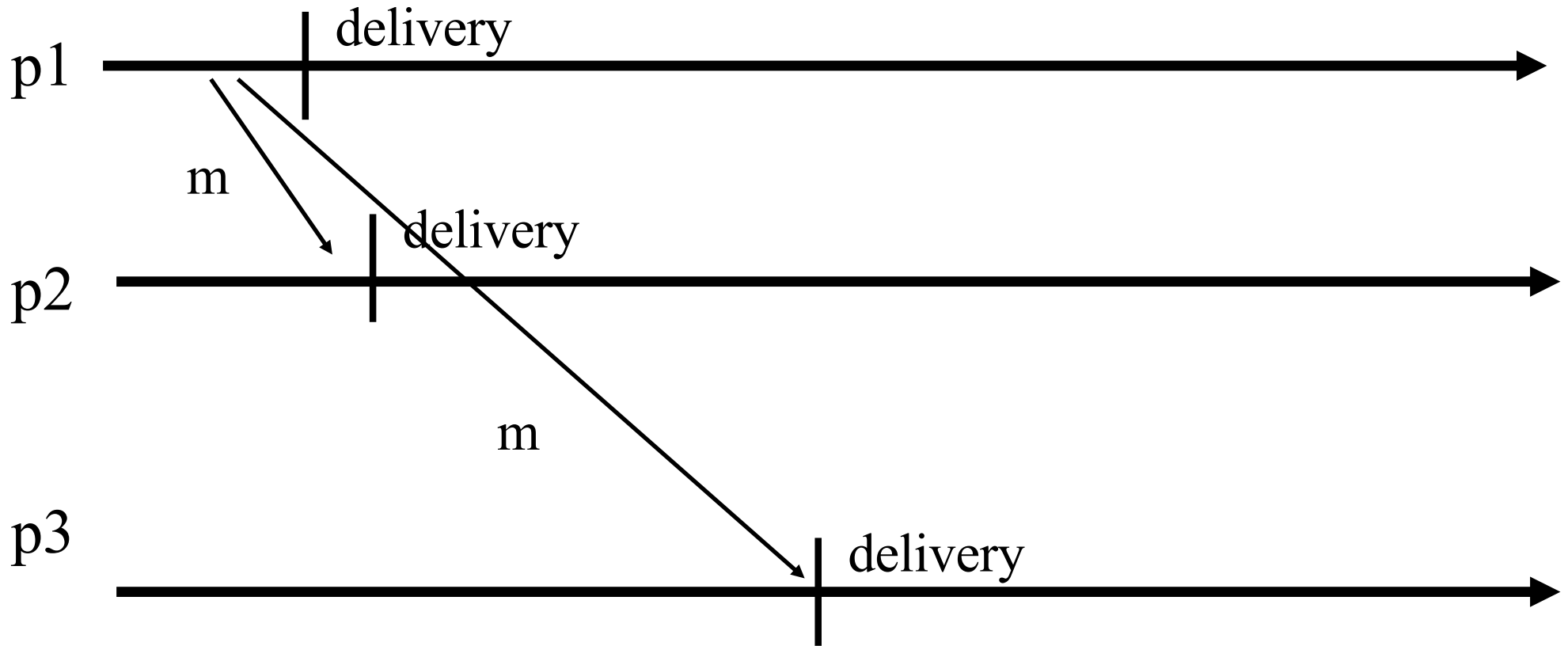
# Best-effort broadcast (beb)

## • *Properties*

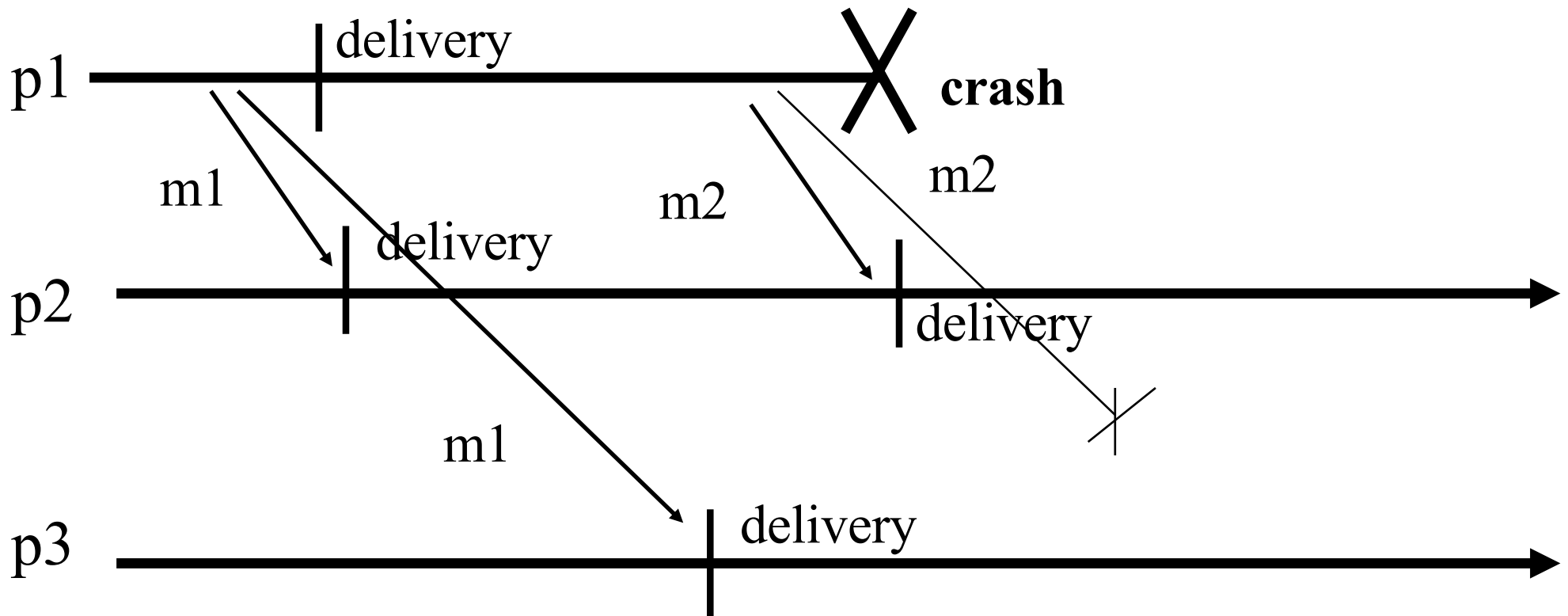
- ***BEB1. Validity.*** If  $p_i$  and  $p_j$  are correct, then every message broadcast by  $p_i$  is eventually delivered by  $p_j$
- ***BEB2. No duplication:*** No message is delivered more than once
- ***BEB3. No creation:*** No message is delivered unless it was broadcast



# Best-effort broadcast



# Best-effort broadcast



# Reliable broadcast (rb)

## • *Events*

• Request: `<rbBroadcast, m>`

• Indication: `<rbDeliver, src, m>`

• *Properties: RB1, RB2, RB3, RB4*

# Reliable broadcast (rb)

## • *Properties*

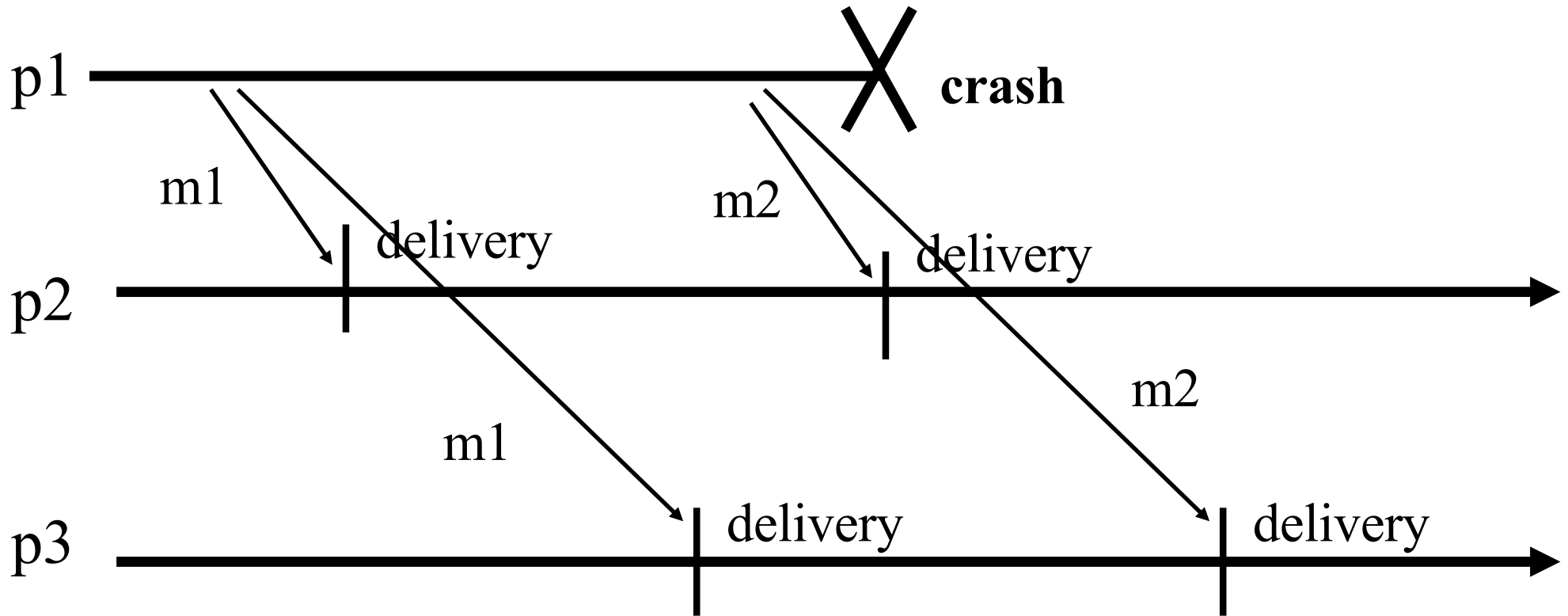
• ***RB1 = BEB1.***

• ***RB2 = BEB2.***

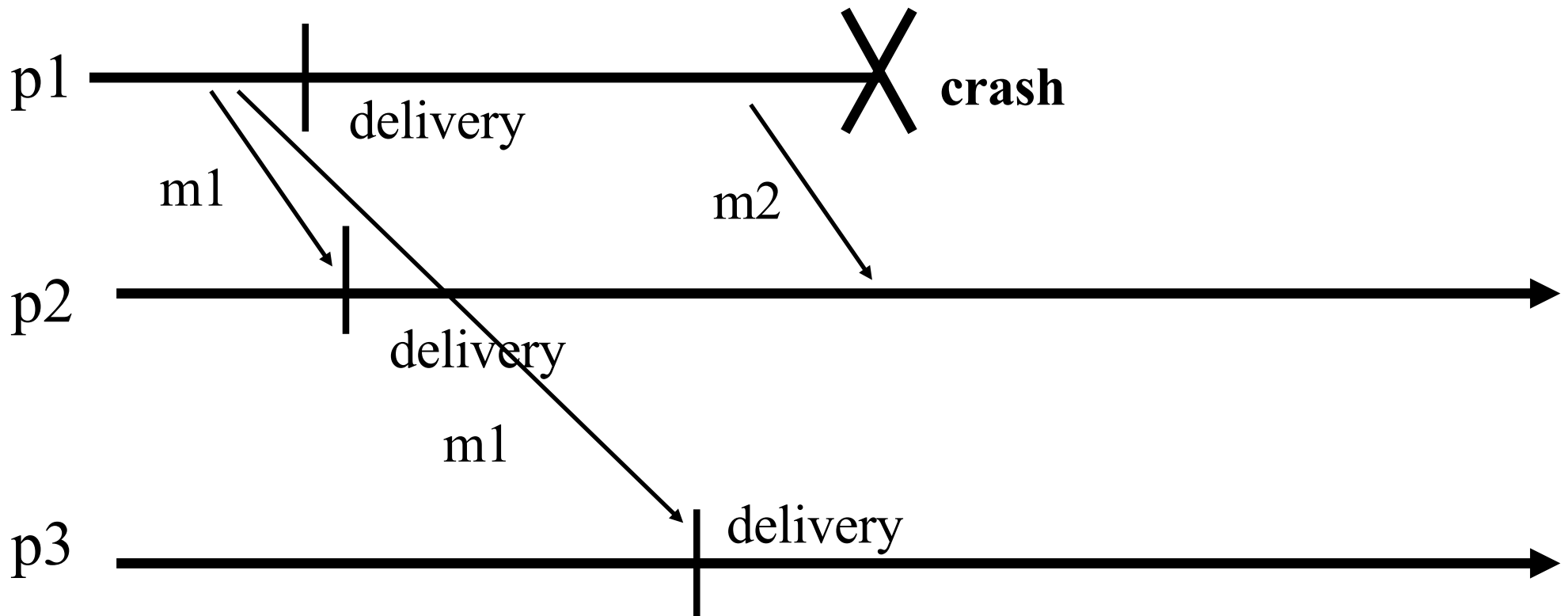
• ***RB3 = BEB3.***

• ***RB4. Agreement:*** For any message  $m$ , if any correct process delivers  $m$ , then every correct process delivers  $m$

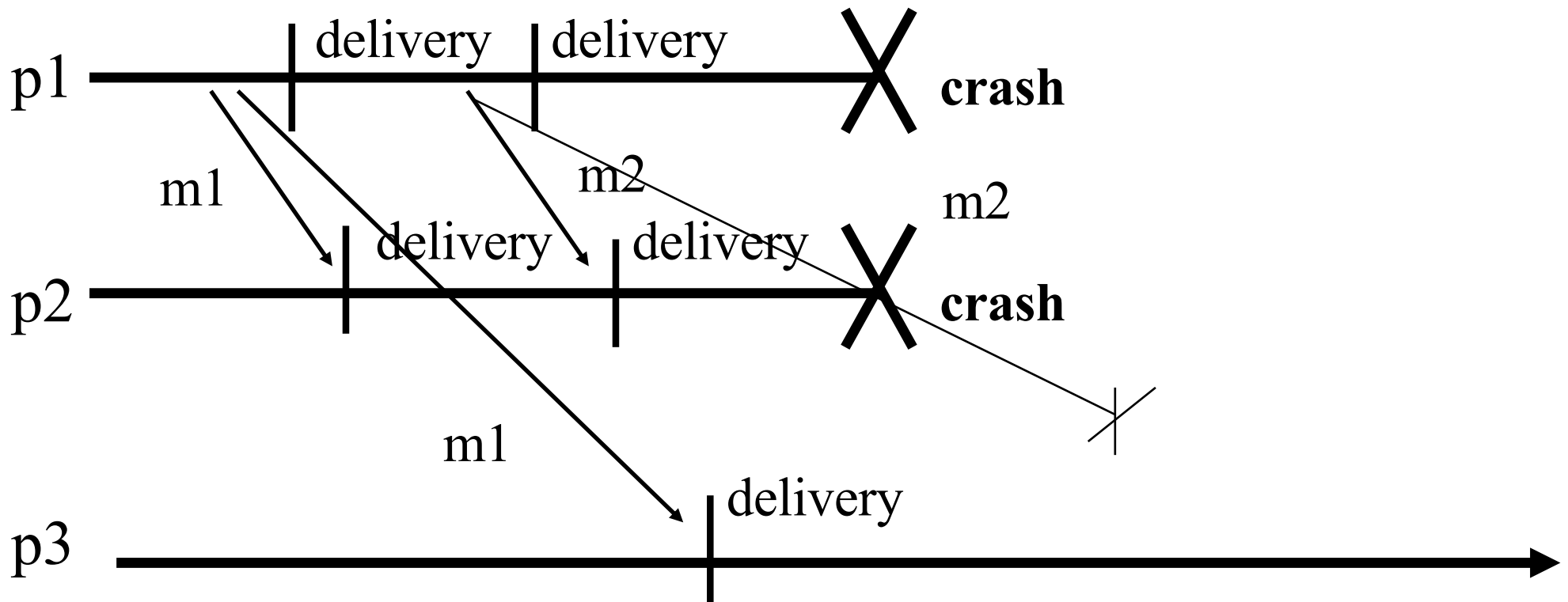
# Reliable broadcast



# Reliable broadcast



# Reliable broadcast



# Uniform broadcast (urb)

## • *Events*

• Request: <urbBroadcast, m>

• Indication: <urbDeliver, src, m>

• *Properties: URB1, URB2, URB3, URB4*



# Uniform broadcast (urb)

## • *Properties*

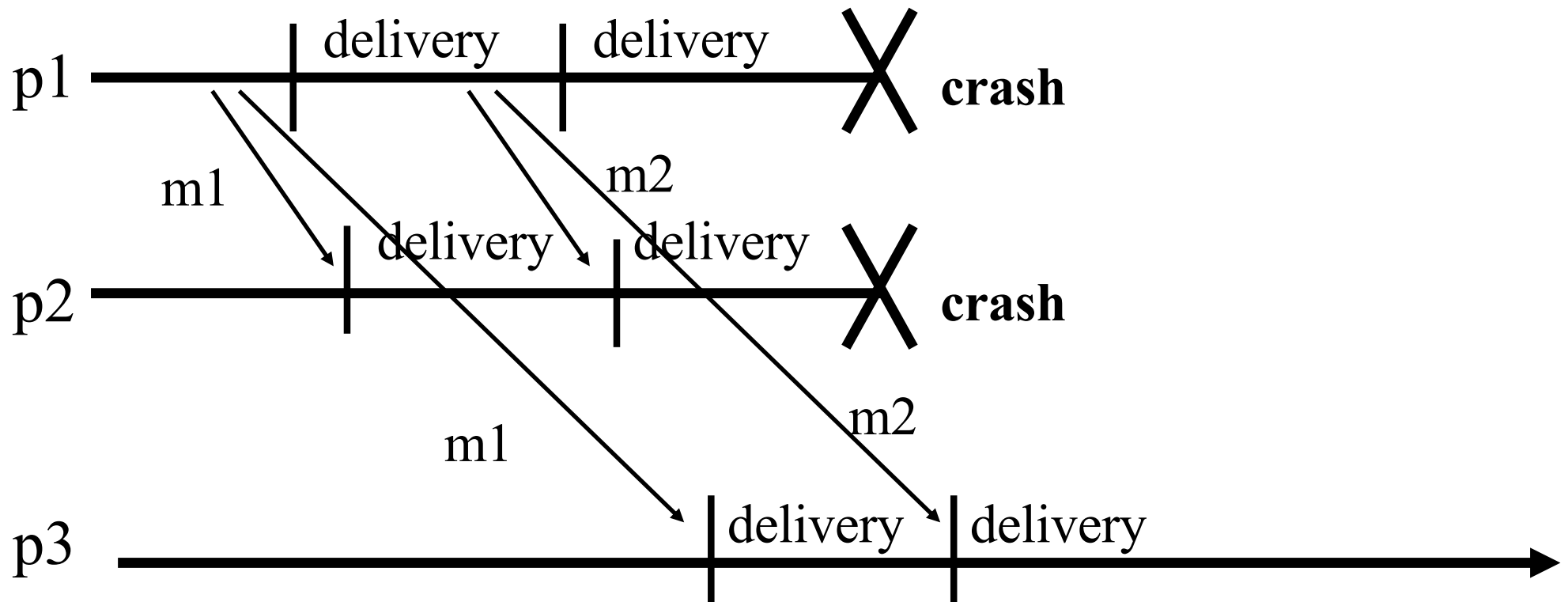
• ***URB1 = BEB1.***

• ***URB2 = BEB2.***

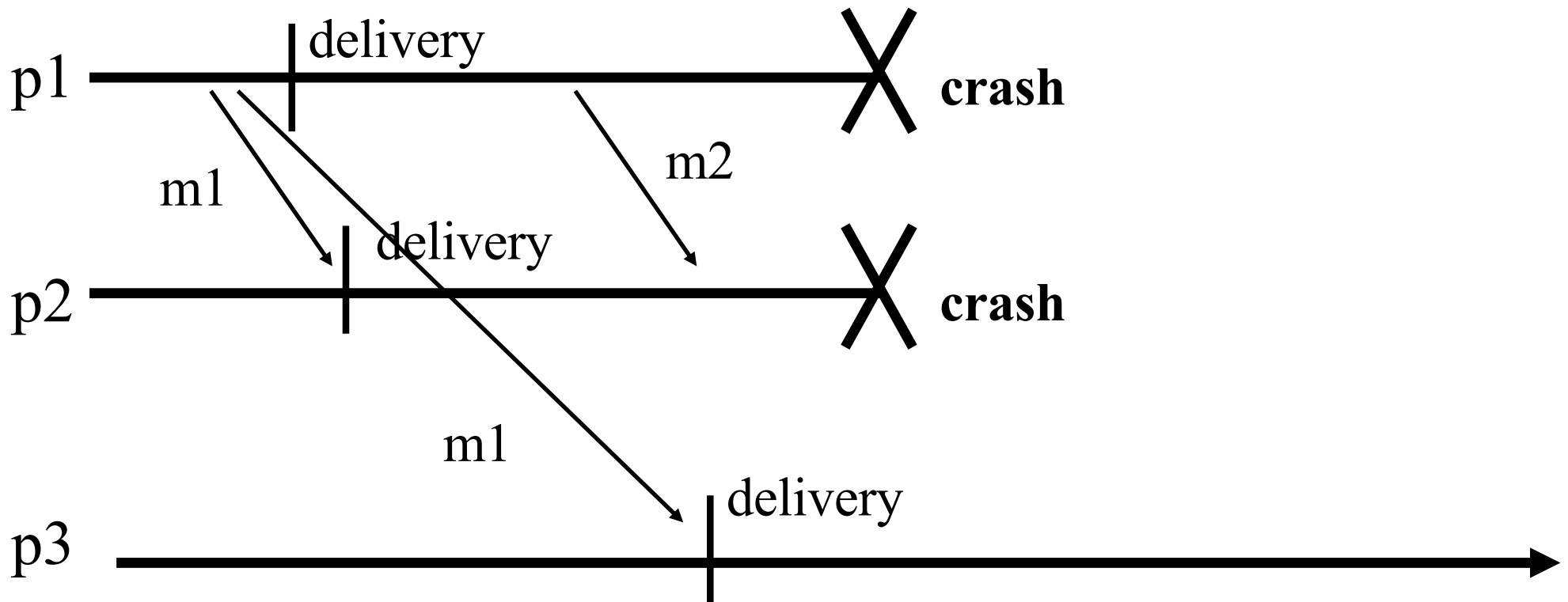
• ***URB3 = BEB3.***

• ***URB4. Uniform Agreement:*** For any message  $m$ , if any process delivers  $m$ , then every correct process delivers  $m$

# Uniform reliable broadcast



# Uniform reliable broadcast



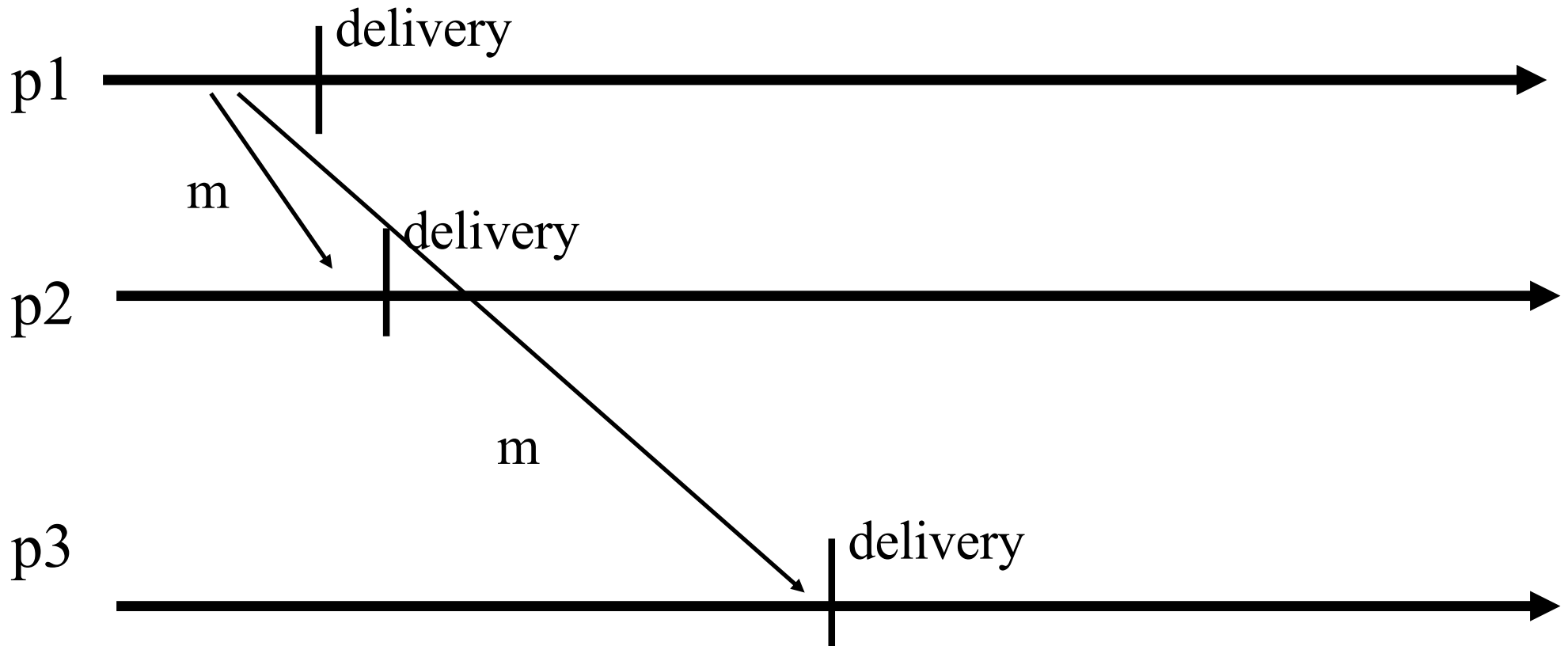
# Overview

- We consider three forms of reliability for a broadcast primitive
- **(1) *Best-effort broadcast***
- **(2) *(Regular) reliable broadcast***
- **(3) *Uniform (reliable) broadcast***
- We give first *specifications* and then ***algorithms***

# Algorithm (beb)

- **Implements:** BestEffortBroadcast (beb).
- **Uses:** PerfectLinks (pp2p).
- **upon event** < bebBroadcast, m > **do**
  - **forall**  $p_i \in S$  **do**
    - **trigger** < pp2pSend,  $p_i$ , m >;
- **upon event** < pp2pDeliver,  $p_i$ , m > **do**
  - **trigger** < bebDeliver,  $p_i$ , m >;

# Algorithm (beb)

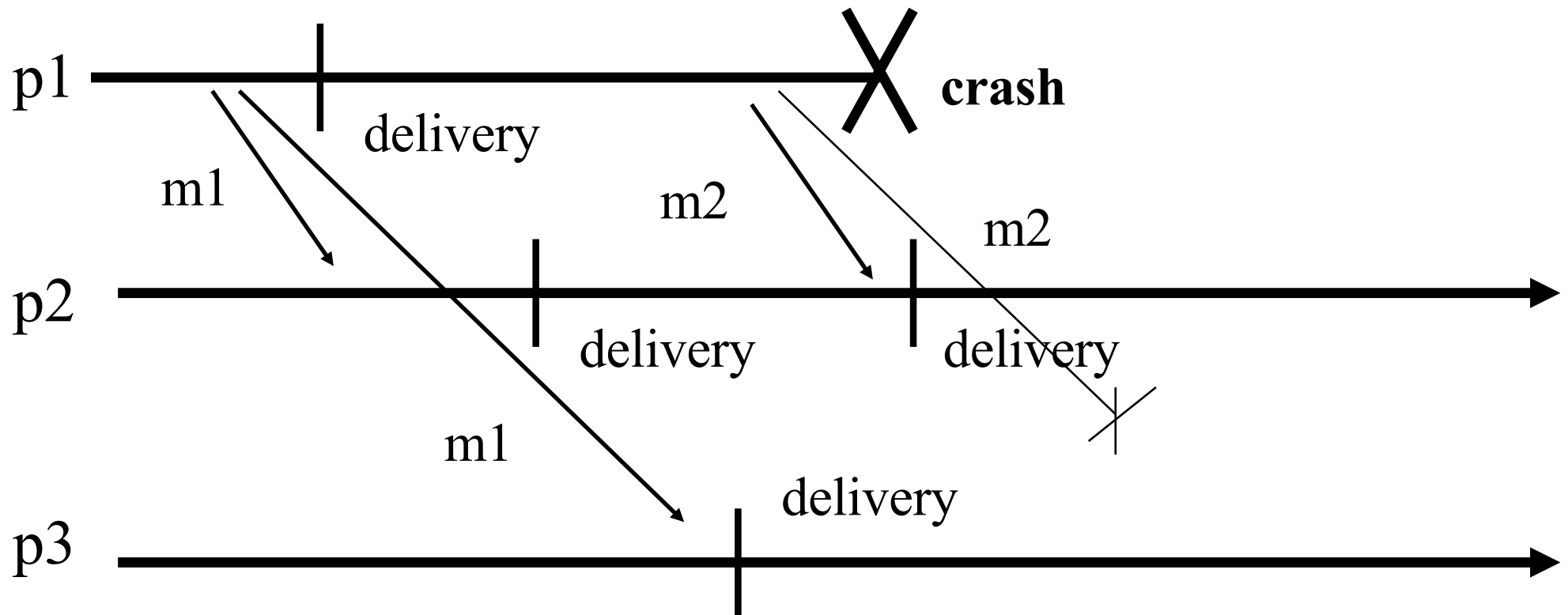


# Algorithm (beb)

## • *Proof (sketch)*

- ***BEB1. Validity:*** By the validity property of perfect links and the very facts that (1) the sender sends the message to all and (2) every correct process that pp2pDelivers a message bebDelivers it
- ***BEB2. No duplication:*** By the no duplication property of perfect links
- ***BEB3. No creation:*** By the no creation property of perfect links

# Algorithm (beb)





# Algorithm (rb)

- ☞ **Implements:** ReliableBroadcast (rb).
- ☞ **Uses:**
  - ☞ BestEffortBroadcast (beb).
  - ☞ PerfectFailureDetector (P).
- ☞ **upon event** < Init > **do**
  - ☞ delivered :=  $\emptyset$ ;
  - ☞ correct := S;
  - ☞ **forall**  $p_i \in S$  **do** from[ $p_i$ ] :=  $\emptyset$ ;

# Algorithm (rb – cont'd)

- **upon event** < rbBroadcast, m > **do**
  - delivered := delivered U {m};
  - **trigger** < rbDeliver, self, m >;
  - **trigger** < bebBroadcast, [Data,self,m] >;

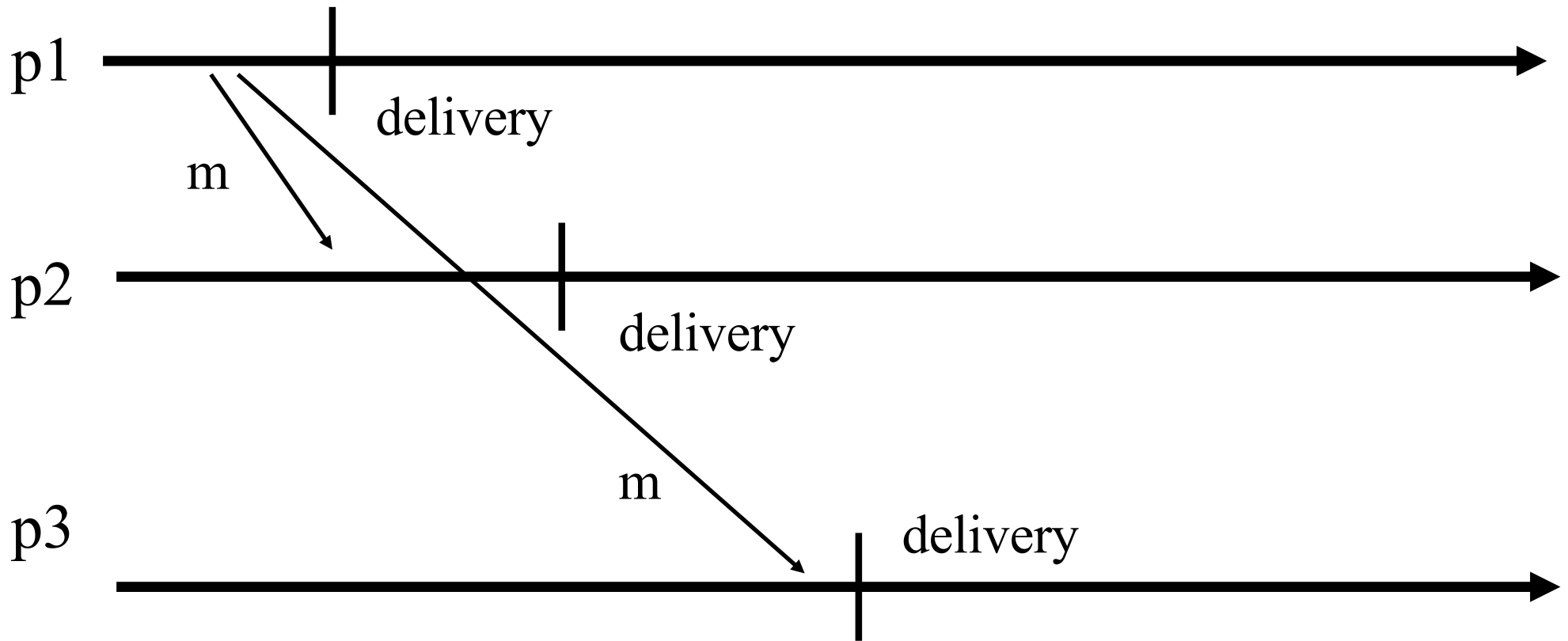
# Algorithm (rb – cont'd)

- **upon event**  $\langle \text{crash}, p_i \rangle$  **do**
  - $\text{correct} := \text{correct} \setminus \{p_i\};$
  - **forall**  $[p_j, m] \in \text{from}[p_i]$  **do**
    - **trigger**  $\langle \text{bebBroadcast}, [\text{Data}, p_j, m] \rangle;$

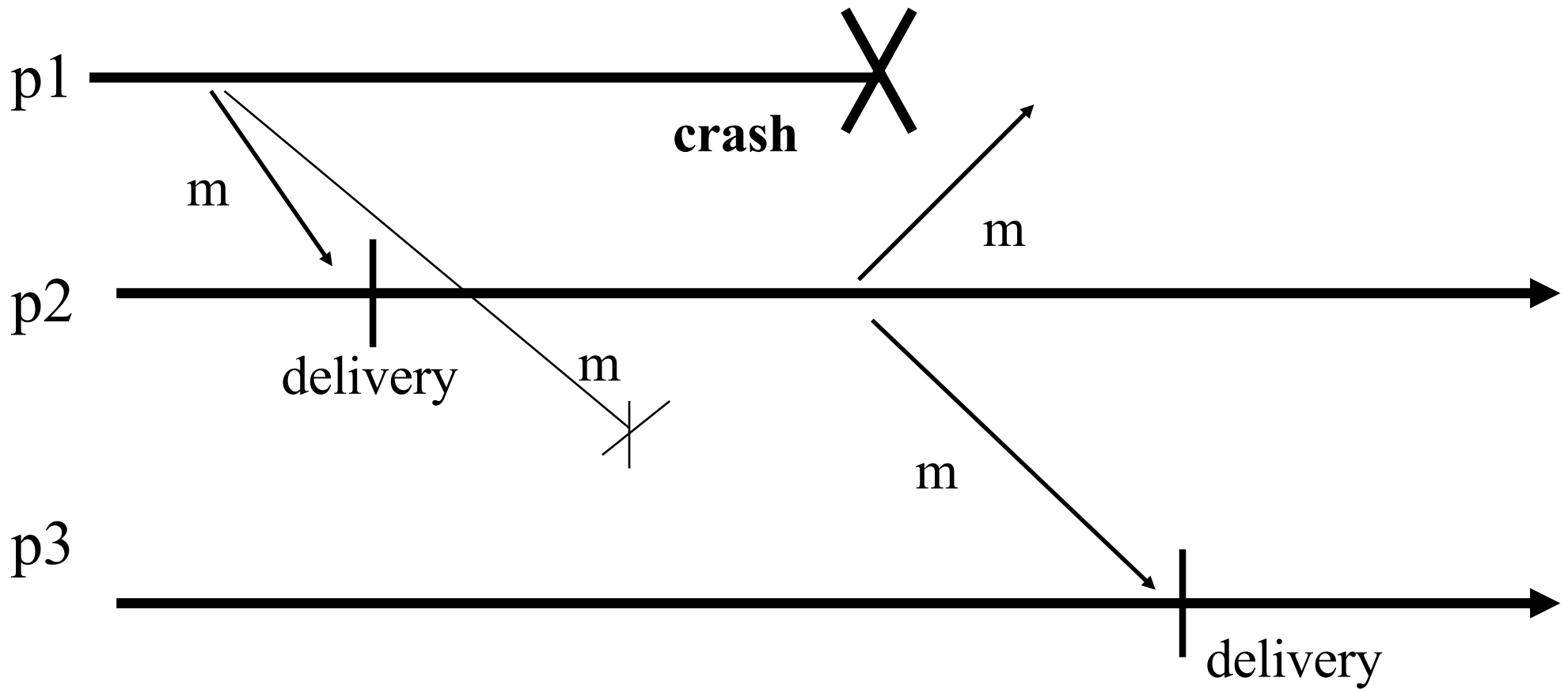
# Algorithm (rb – cont'd)

- ☛ **upon event**  $\langle \text{bebDeliver}, p_i, [\text{Data}, p_j, m] \rangle$  **do**
  - ☛ **if**  $m \notin \text{delivered}$  **then**
    - ☛  $\text{delivered} := \text{delivered} \cup \{m\};$
    - ☛ **trigger**  $\langle \text{rbDeliver}, p_j, m \rangle;$
    - ☛ **if**  $p_i \notin \text{correct}$  **then**
      - ☛ **trigger**  $\langle \text{bebBroadcast}, [\text{Data}, p_j, m] \rangle;$
  - ☛ **else**
    - ☛  $\text{from}[p_i] := \text{from}[p_i] \cup \{[p_j, m]\};$

# Algorithm (rb)



# Algorithm (rb)



# Algorithm (rb)

## • *Proof (sketch)*

- **RB1. RB2. RB3:** as for the 1st algorithm
- **RB4. Agreement:** Assume some correct process  $p_i$   $rbDelivers$  a message  $m$   $rbBroadcast$  by some process  $p_k$ . If  $p_k$  is correct, then by property BEB1, all correct processes  $bebDeliver$  and then  $rebDeliver$   $m$ . If  $p_k$  crashes, then by the completeness property of  $P$ ,  $p_i$  detects the crash and  $bebBroadcasts$   $m$  to all. Since  $p_i$  is correct, then by property BEB1, all correct processes  $bebDeliver$  and then  $rebDeliver$   $m$ .

# Algorithm (urb)

- ☞ **Implements:** uniformBroadcast (urb).
- ☞ **Uses:**
  - ☞ BestEffortBroadcast (beb).
  - ☞ PerfectFailureDetector (P).
- ☞ **upon event** < Init > **do**
  - ☞ correct := S;
  - ☞ delivered := forward :=  $\emptyset$ ;
  - ☞ ack[Message] :=  $\emptyset$ ;



# Algorithm (urb – cont'd)

- **upon event**  $\langle \text{crash}, p_i \rangle$  **do**
  - $\text{correct} := \text{correct} \setminus \{p_i\};$
  
- **upon event**  $\langle \text{urbBroadcast}, m \rangle$  **do**
  - $\text{forward} := \text{forward} \cup \{[self, m]\};$
  - **trigger**  $\langle \text{bebBroadcast}, [Data, self, m] \rangle;$

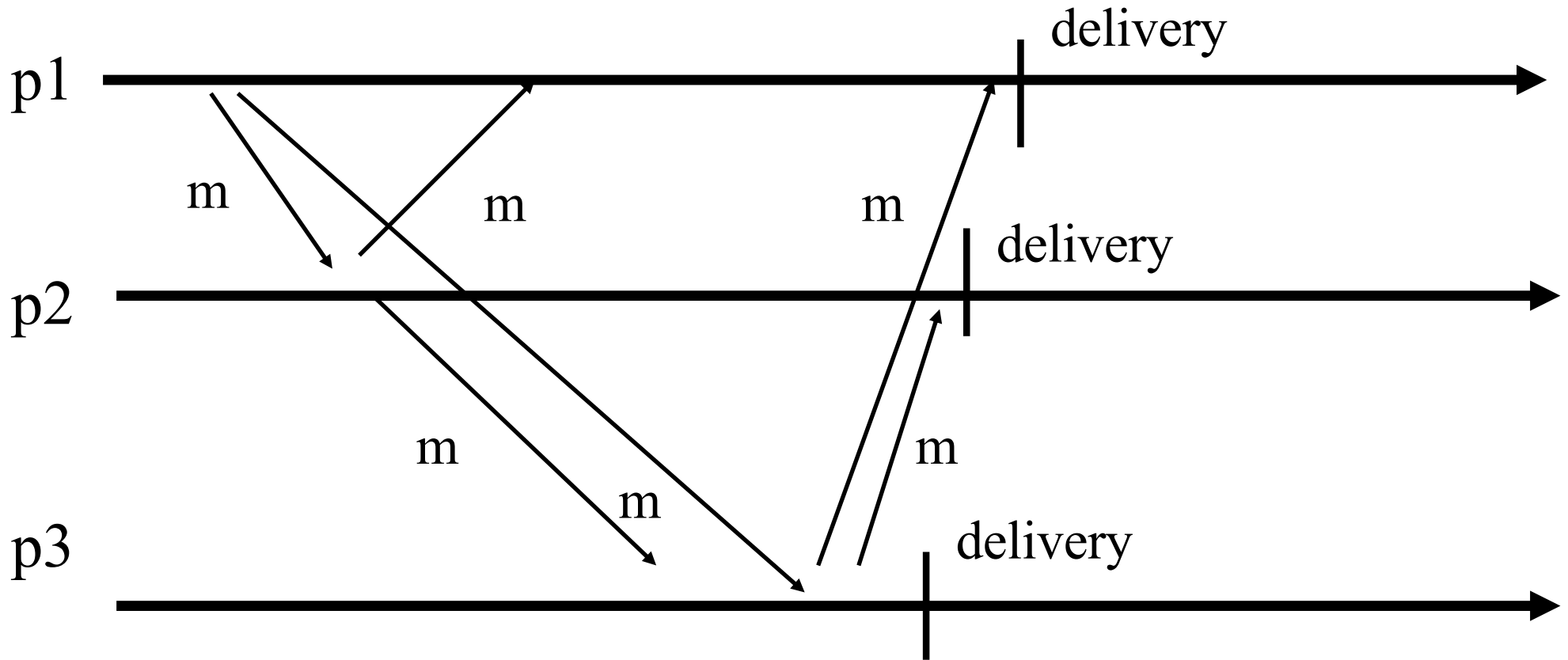
# Algorithm (urb – cont'd)

- **upon event**  $\langle \text{bebDeliver}, p_i, [\text{Data}, p_j, m] \rangle$  **do**
  - $\text{ack}[m] := \text{ack}[m] \cup \{p_i\};$
  - **if**  $[p_j, m] \notin \text{forward}$  **then**
    - $\text{forward} := \text{forward} \cup \{[p_j, m]\};$
    - **trigger**  $\langle \text{bebBroadcast}, [\text{Data}, p_j, m] \rangle;$

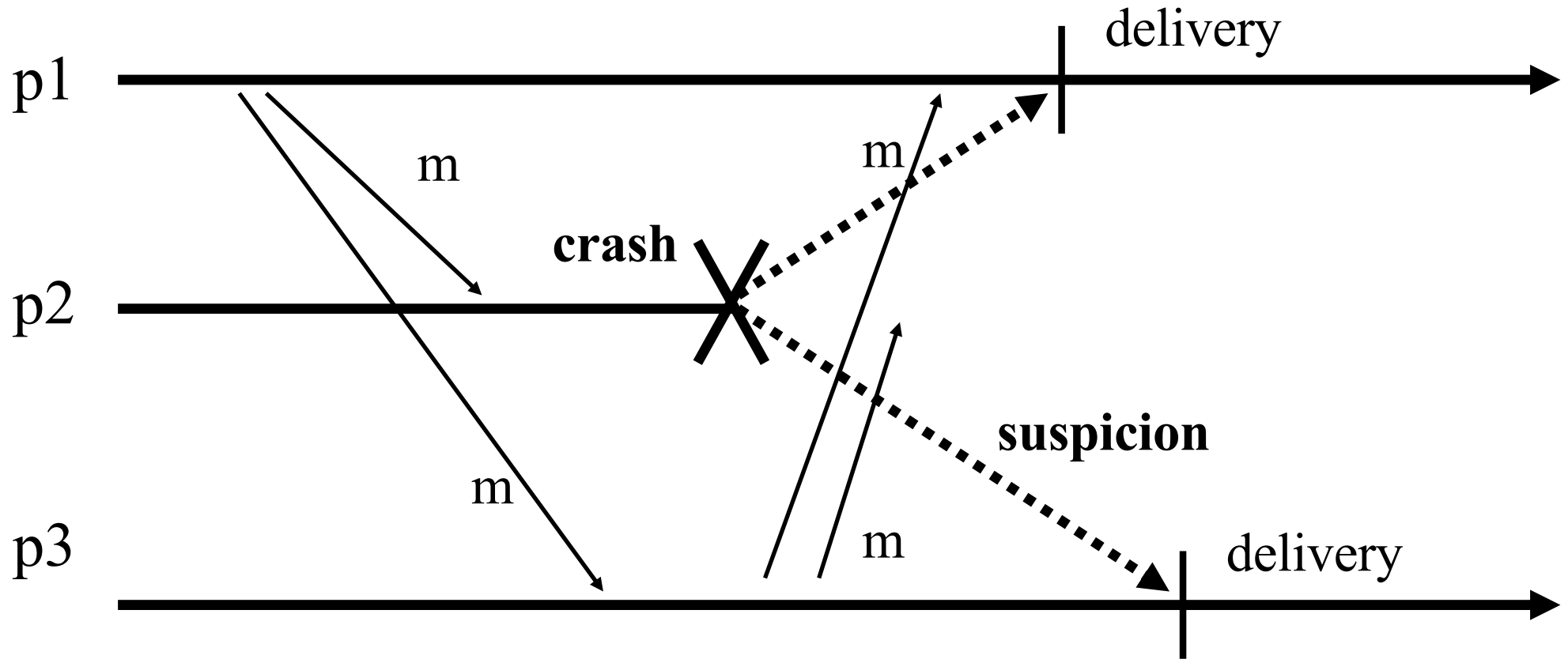
# Algorithm (urb – cont'd)

- **upon event** (for any  $[p_j, m] \in \text{forward}$ )  
 $\langle \text{correct} \subseteq \text{ack}[m] \rangle$  **and**  $\langle m \notin \text{delivered} \rangle$  **do**
  - $\text{delivered} := \text{delivered} \cup \{m\};$
  - **trigger**  $\langle \text{urbDeliver}, p_j, m \rangle;$

# Algorithm (urb)



# Algorithm (urb)



# Algorithm (urb)

## • *Proof (sketch)*

- **URB2. URB3:** follow from BEB2 and BEB3
- **Lemma:** *If a correct process  $p_i$  bebDelivers a message  $m$ , then  $p_i$  eventually urbDelivers  $m$ .*
- Any process that bebDelivers  $m$  bebBroadcasts  $m$ . By the completeness property of the failure detector and property BEB1, there is a time at which  $p_i$  bebDelivers  $m$  from every correct process and hence urbDelivers  $m$ .

# Algorithm (urb)

## • *Proof (sketch)*

- **URB1. Validity:** If a correct process  $p_i$  urbBroadcasts a message  $m$ , then  $p_i$  eventually bebBroadcasts and bebDelivers  $m$ : by our lemma,  $p_i$  urbDelivers  $m$ .
- **URB4. Agreement:** Assume some process  $p_i$  urbDelivers a message  $m$ . By the algorithm and the completeness and accuracy properties of the failure detector, every correct process bebDelivers  $m$ . By our lemma, every correct process will urbDeliver  $m$ .