

# Concurrent Algorithms (Overview)

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***In short***

***This course is about the principles  
of robust concurrent computing***

# Today

• *Logistics*

• *Motivation*

• *Content*

# ***WARNING***

- This course is different from the course :  
**Distributed Algorithms**
- shared memory vs message passing
- It does make a lot of sense to take both

# This course

- *Theoretical but no specific theoretical background is required*
- *Exercices throughout the semester*
- *Mid term + Final exam + Bonus project*

*New York Times, 8 May 2004:* Major chip manufacturers announced what is perceived as a major paradigm shift in computing:

***Multiprocessors vs faster processors***

Major chip manufacturers have announced a major paradigm shift:

Intel ... [has] decided to focus its development efforts on «dual core» processors ... with two engines instead of one, allowing for greater efficiency because the processor workload is essentially shared.

Moore (65-75): the number of transistors on the same chip doubles every two years

***But***

Dennard (74): the frequency can double every year without doubling energy



The clock speed of a processor cannot be increased without overheating

***But***

More and more processors can fit in the same space

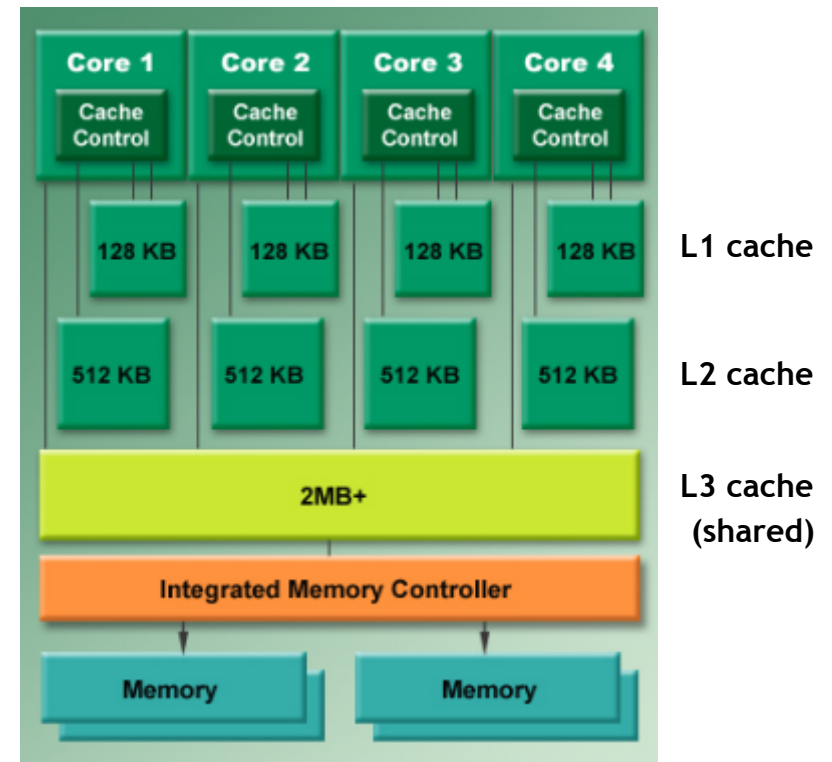
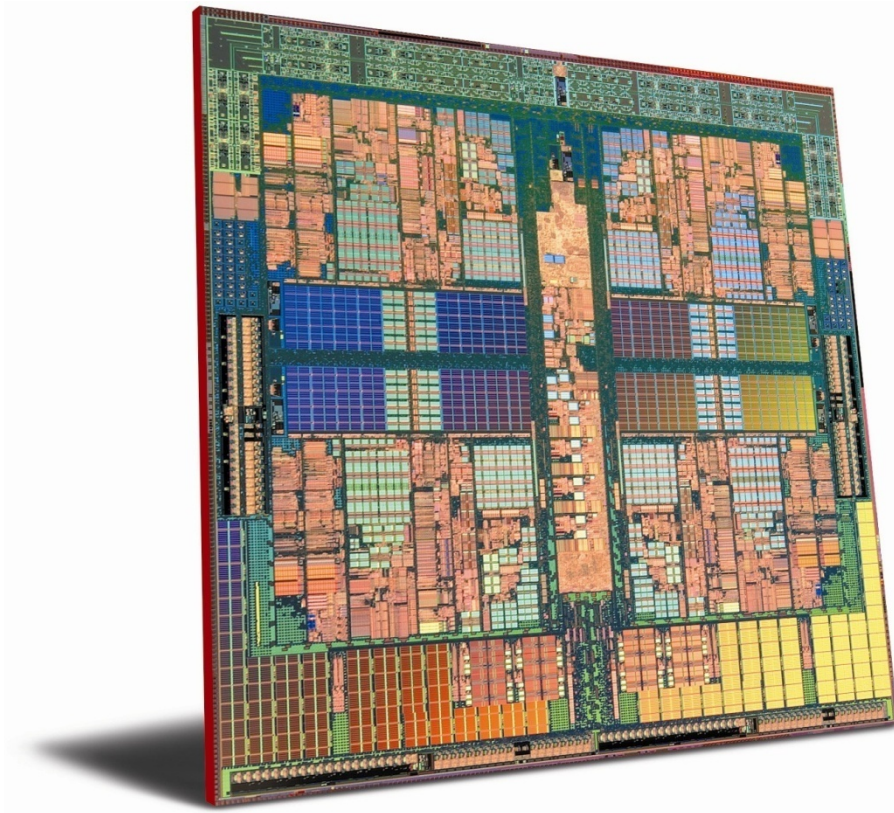
# ***Multicores **are** almost everywhere***

- ☞ **Dual-core** commonplace in laptops
- ☞ **Quad-core** in desktops
- ☞ **Dual quad-core** in servers
- ☞ **All major chip manufacturers produce multicore CPUs**
  - **SUN Niagara** (8 cores, 32 threads)
  - **Intel Xeon** (4 cores)
  - **AMD Opteron** (4 cores)

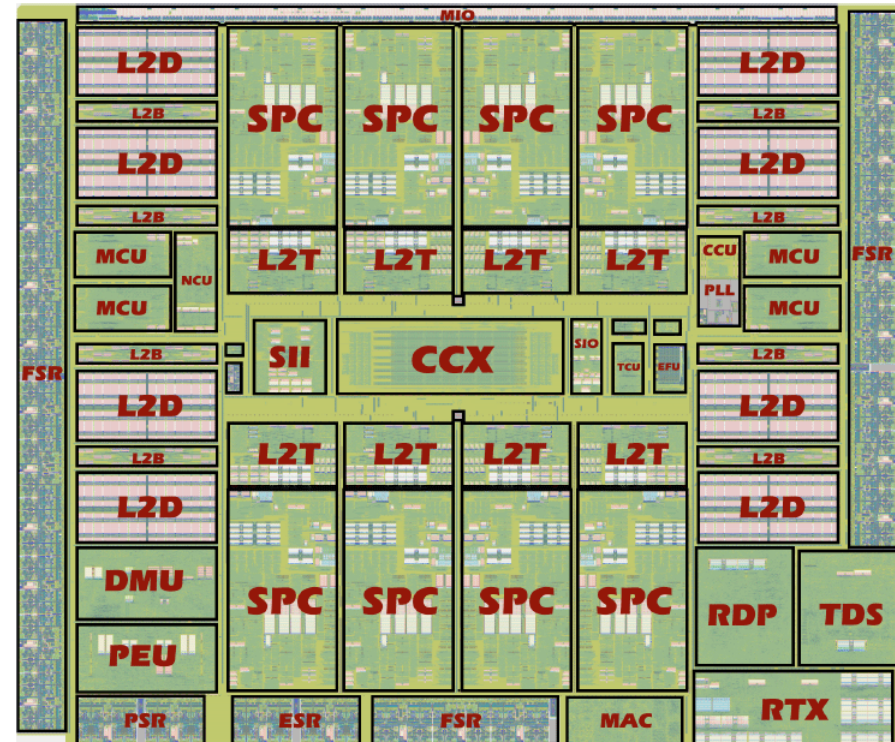
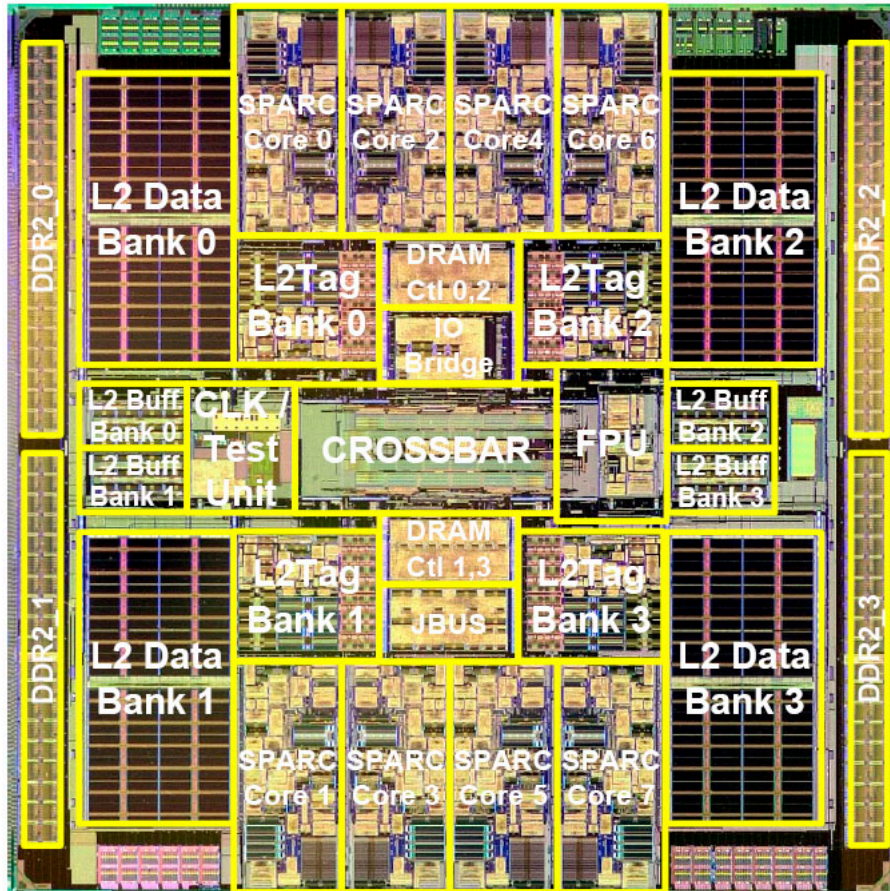
# ***Multicores **are** almost everywhere***

- ☞ **Quad-core** in laptops
- ☞ **Octa-core** in desktops
- ☞ **2\*12 cores** in servers
- ☞ **All major chip manufacturers produce multicore CPUs**
  - **Oracle Sparc** (32 cores, 256 threads)
  - **Intel Xeon** (12-16 cores)
  - **AMD Opteron** (12-16 cores)

# AMD Opteron (4 cores)



# SUN's Niagara CPU2 (8 cores)



- |                             |  |
|-----------------------------|--|
| CCX – Crossbar              | L2T – L2 tag arrays                        |
| CCU – Clock control         | MCU – Memory controller                    |
| DMU/PEU – PCI Express       | MIO – Miscellaneous I/O                    |
| EFU – Efuse for redundancy  | PSR – PCI Express SERDES                   |
| ESR – Ethernet SERDES       | RDP/TDS/RTX/MAC – Ethernet                 |
| FSR – FBD SERDES            | SII/SIO – I/O data path to and from memory |
| L2B – L2 write-back buffers | SPC – SPARC cores                          |
| L2D – L2 data arrays        | TCU – Test and control unit                |

# ***Multiprocessors***

- ▮ Multiple hardware processors: each executes a series of processes (software constructs) modeling sequential programs
- ▮ Multicore architecture: multiple processors are placed on the same chip

# ***Principles of an architecture***

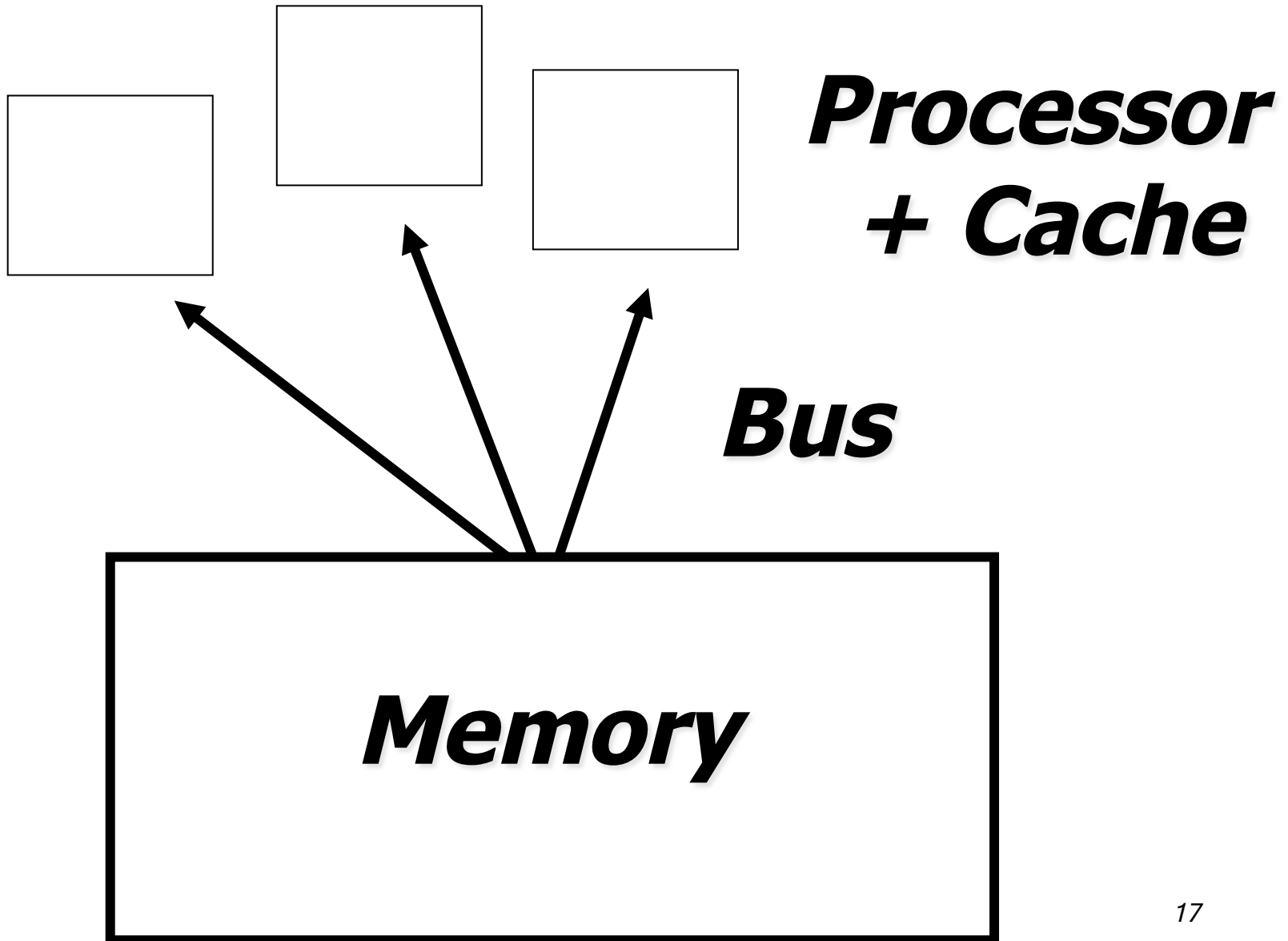
- ▬ Two fundamental components that ***fall apart***: ***processors*** and ***memory***
- ▬ The Interconnect links the processors with the memory:
  - ▬ - ***SMP*** (symmetric): bus (a tiny Ethernet)
  - ▬ - ***NUMA*** (network): point-to-point network

# *Cycles*

- The basic unit of time is the *cycle*: time to execute an instruction
- This changes with technology but the relative cost of instructions (local vs memory) does not



# Simple view



# ***Hardware synchronization objects***

- The basic unit of communication is the *read* and *write* to the memory (through the cache)
- More sophisticated objects are typically provided and, as we will see, necessary: C&S, T&S, LL/SC

# ***The free ride is over***

- Cannot rely on CPUs getting faster in every generation
- Utilizing more than one CPU core requires concurrency

# ***The free ride is over***

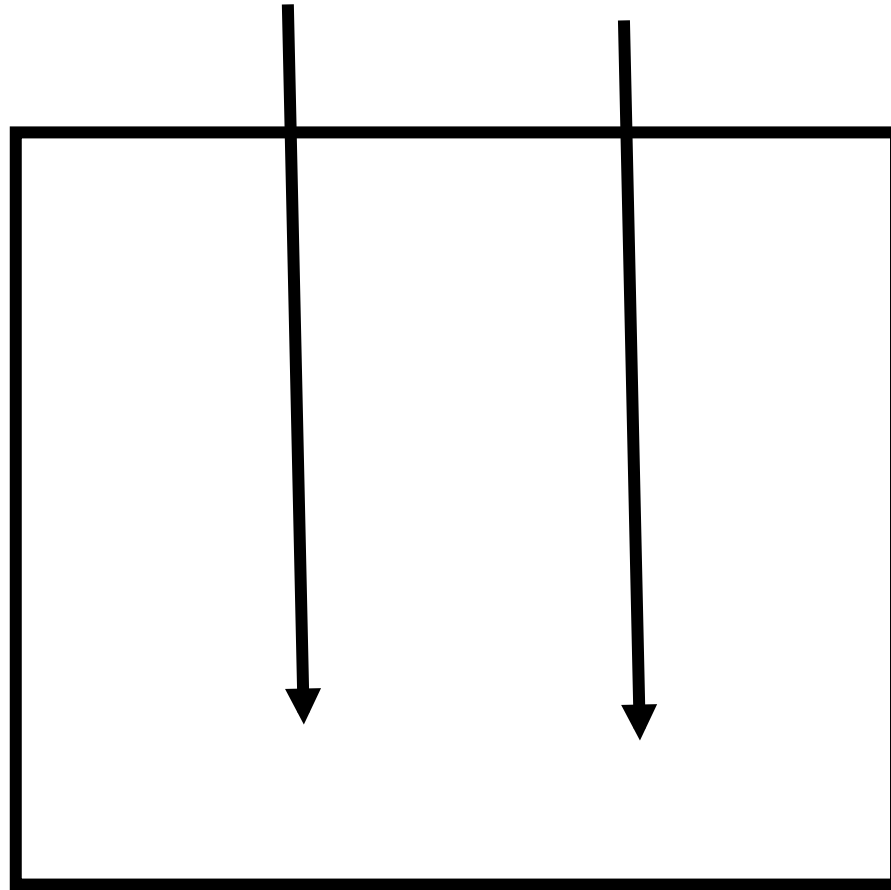
- ☞ One of the biggest software challenges:  
**exploiting concurrency**
  - Every programmer will have to deal with it
  - Concurrent programming is hard to get right

Speed will be achieved by having several processors work on independent parts of a task

***But***

the processors would occasionally need to pause and synchronize

# Concurrent processes



**Shared object**

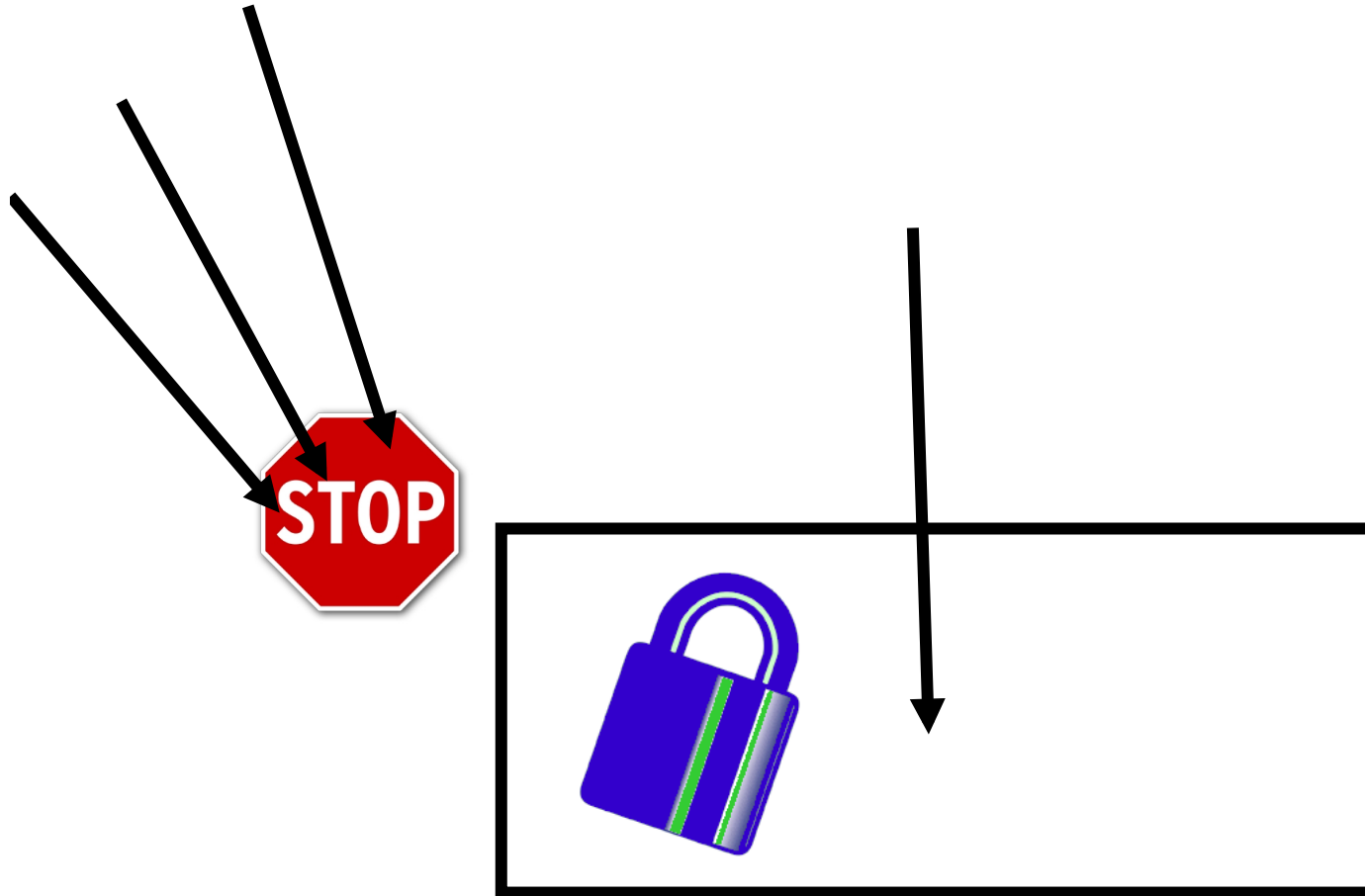
# Counter

```
public class Counter

private int c = 0;

public long getAndIncrement()
{
return c++;
}
```

# Locking (mutual exclusion)



**Locked object**



# Implicit use of a lock

```
public class SynchronizedCounter {
    private int c = 0;
    public synchronized void increment() {
        c++;
    }
    public synchronized void getAndincrement()
{
        return c++;
    }
    public synchronized int value() {
        return c;
    }
}
```

# Locking with `compare&swap()`

- A ***Compare&Swap*** object maintains a value  $x$ , init to  $\perp$ , and  $y$ ;
- It provides one operation: ***c&s(old,new);***
  - ✓ Sequential spec:
    - `c&s(old,new)`  
{ $y := x$ ; if  $x = \text{old}$  then  $x := \text{new}$ ; return( $y$ )}

# Locking with compare&swap()

```
lock() {  
  repeat until  
  unlocked = this.c&s(unlocked,locked)  
}
```

```
unlock() {  
    this.c&s(locked,unlocked)  
}
```

# Locking with test&set()

- A **Test&Set** object maintains binary values  $x$ , init to 0, and  $y$ ;
- It provides one operation:  **$t\&s()$** 
  - ✓ Sequential spec:
  - ✓  $t\&s() \{y := x; x := 1; \text{return}(y);\}$

# Locking with test&set()

```
lock() {  
  repeat until (0 = this.t&s());  
}
```

```
unlock() {  
  this.setState(0);  
}
```

# Locking with test&set()

```
lock() {  
  while (true)  
  {  
    repeat until (0 = this.getState());  
    if 0 = (this.t&s()) return(true);  
  }  
}
```

```
unlock() {  
  this.setState(0);  
}
```

# Explicit use of a lock

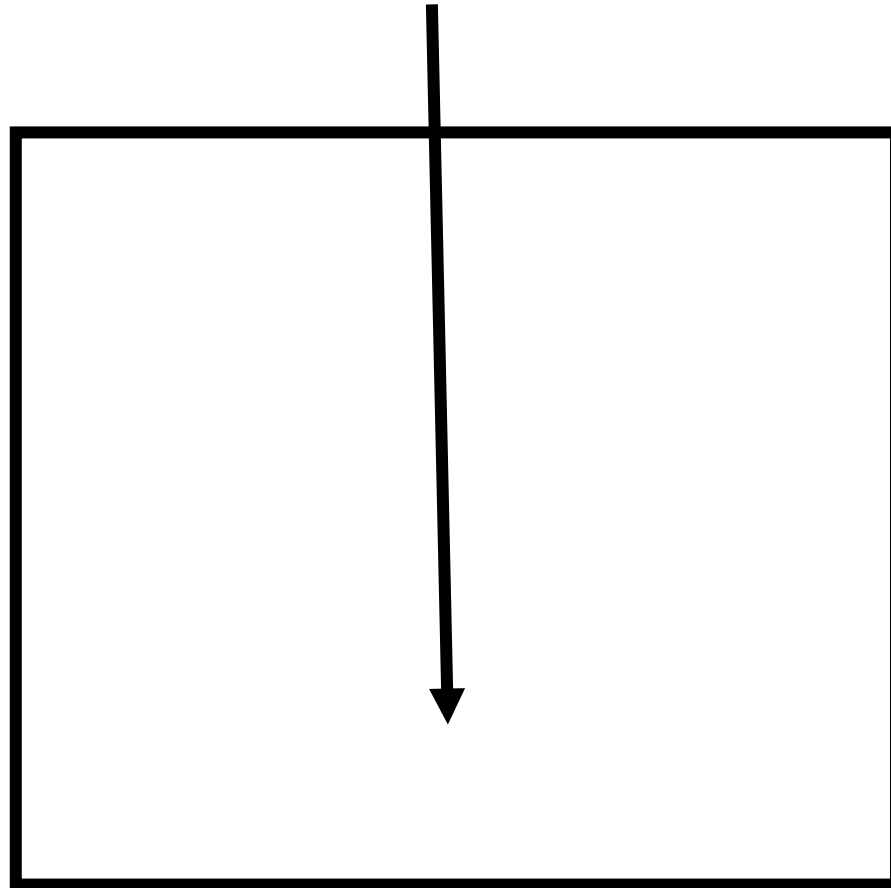
```
Lock l = ...;  
    l.lock();  
    try {  
// access the resource protected by this lock  
    } finally {  
        l.unlock();  
    }
```

# Locking (mutual exclusion)

- **Difficult:** 50% of the bugs reported in Java come from the mis-use of « synchronized »
- **Fragile:** a process holding a lock prevents all others from progressing
- **Slow:** the act of locking itself impacts performance



**Locked object**



**One process at a time**

# Processes are asynchronous

- *Page faults*
- *Pre-emptions*
- *Failures*
- *Cache misses, ...*

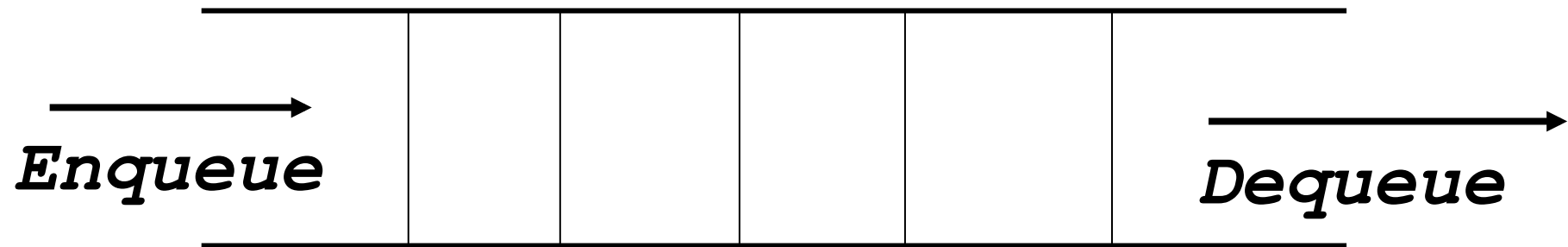
# Processes are asynchronous

- A cache miss can delay a process by ten instructions
- A page fault by few millions
- An os preemption by hundreds of millions...

***Coarse grained locks => slow***

***Fine grained locks => errors***

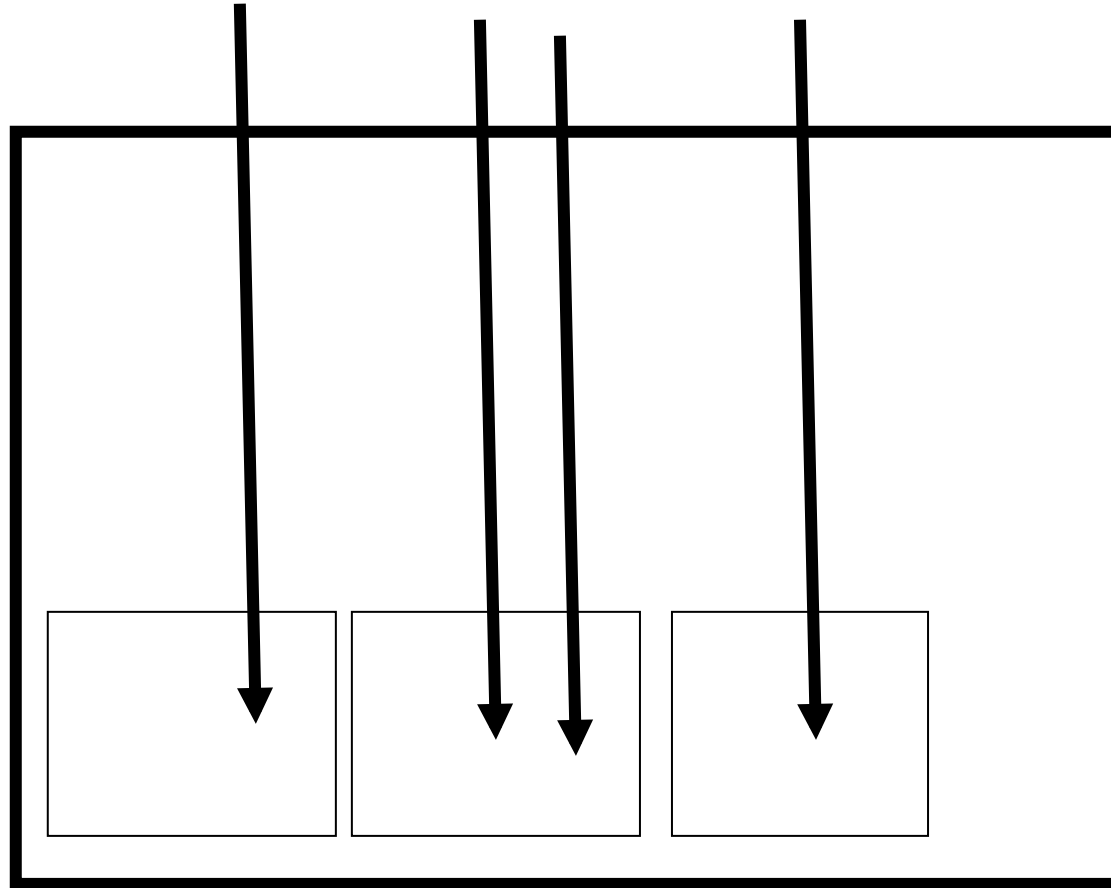
# *Double-ended queue*



# Processes are asynchronous

- *Page faults, pre-emptions, failures, cache misses, ...*
- A process can be delayed by millions of instructions ...

# Alternative to locking?



# Wait-free atomic objects

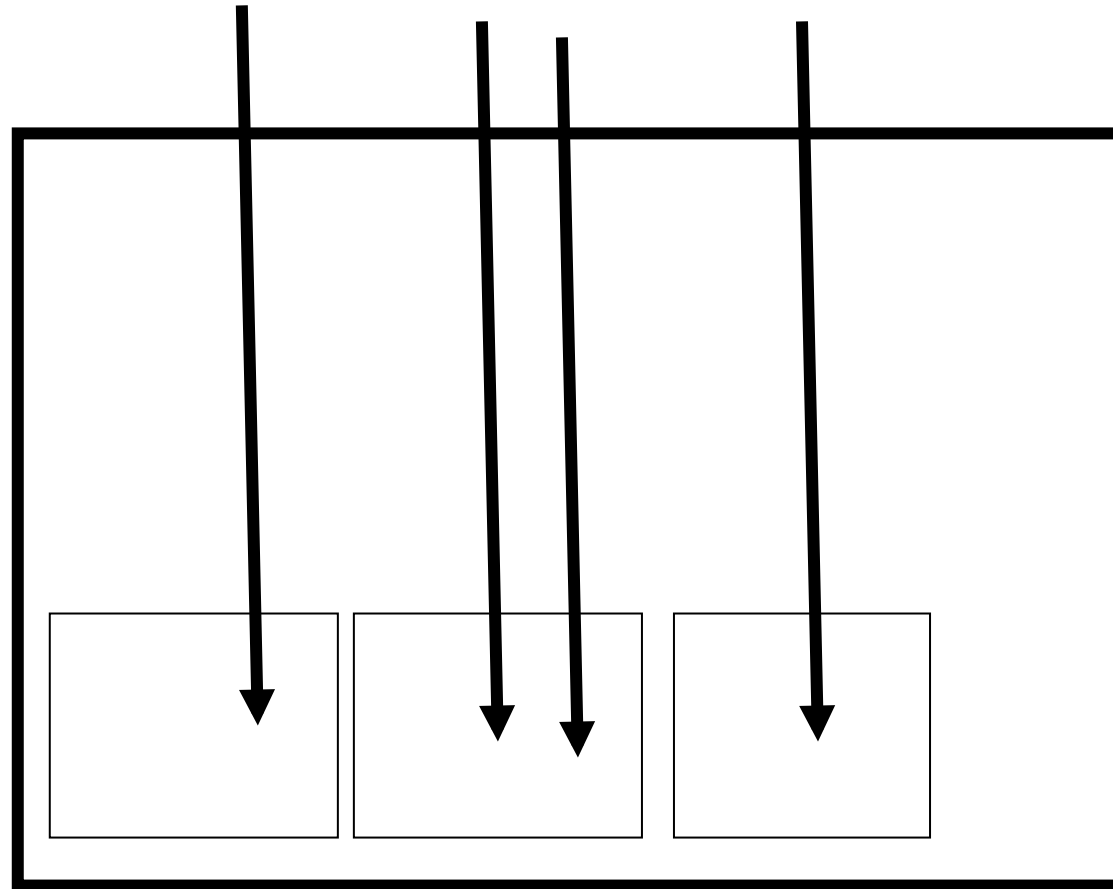
- ***Wait-freedom:*** every process that invokes an operation eventually returns from the invocation (robust ... unlike locking)
- ***Atomicity:*** every operation appears to execute instantaneously (as if the object was locked...)



# In short

This course shows how to  
***wait-free*** implement high-level  
***atomic*** objects out of primitive base objects

# Concurrent processes



**Shared object**

# Roadmap

- *Model*
  - *Processes and objects*
  - *Atomicity and wait-freedom*
- *Examples*
- *Content*

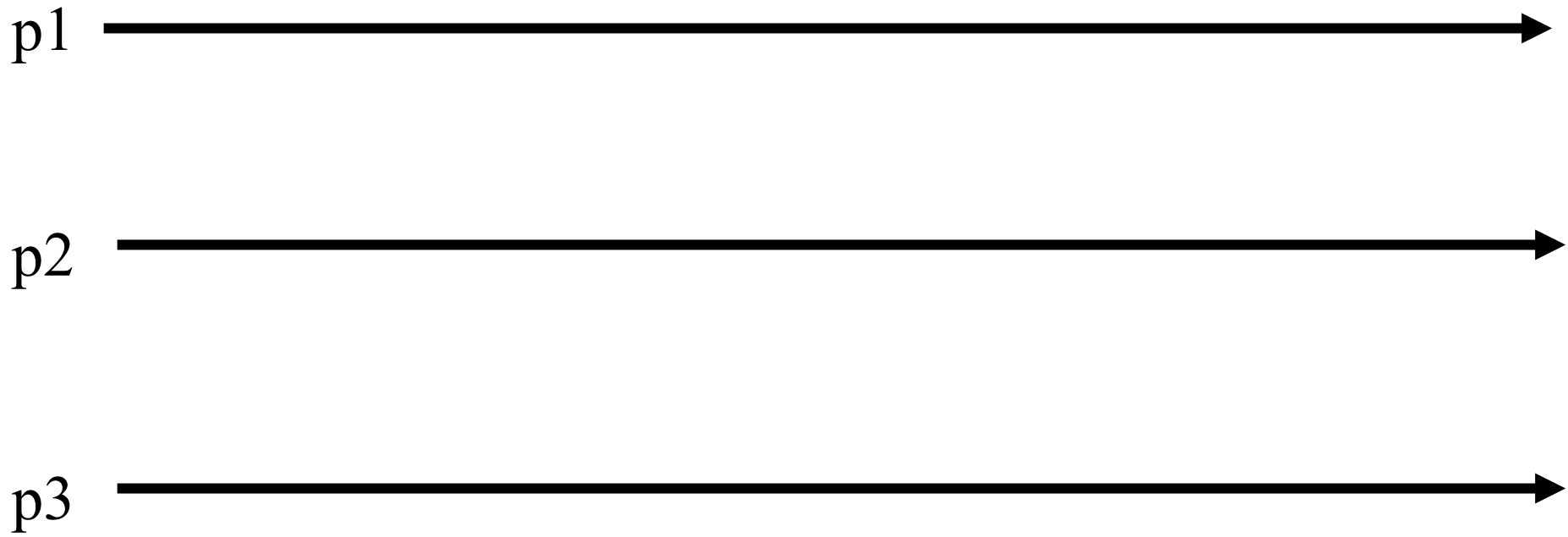
# Processes

- We assume a finite set of processes
- Processes are denoted by  $p_1, \dots, p_N$  or  $p, q, r$
- Processes have unique identities and know each other (unless explicitly stated otherwise)

# Processes

- Processes are *sequential* units of computations
- Unless explicitly stated otherwise, we make no assumption on process (relative) speed

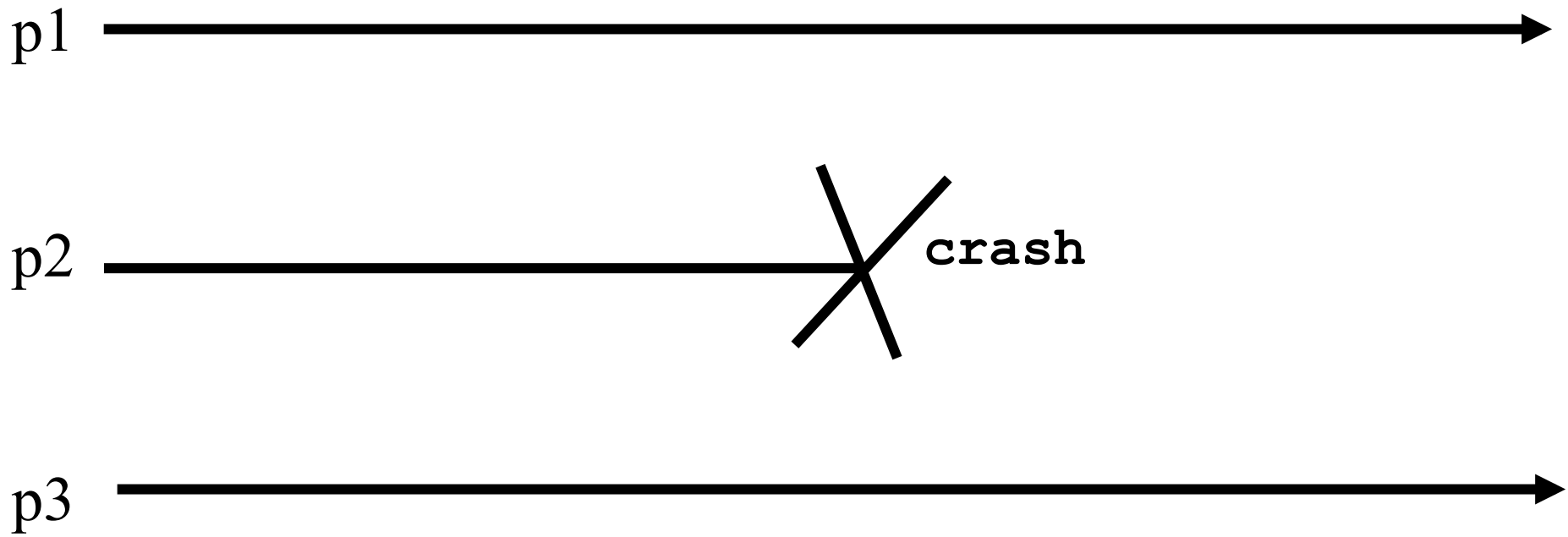
# Processes



# Processes

- A process either executes the algorithm assigned to it or crashes
- A process that crashes does not recover (in the context of the considered computation)
- A process that does not crash in a given execution (computation or run) is called correct (in that execution)

# Processes

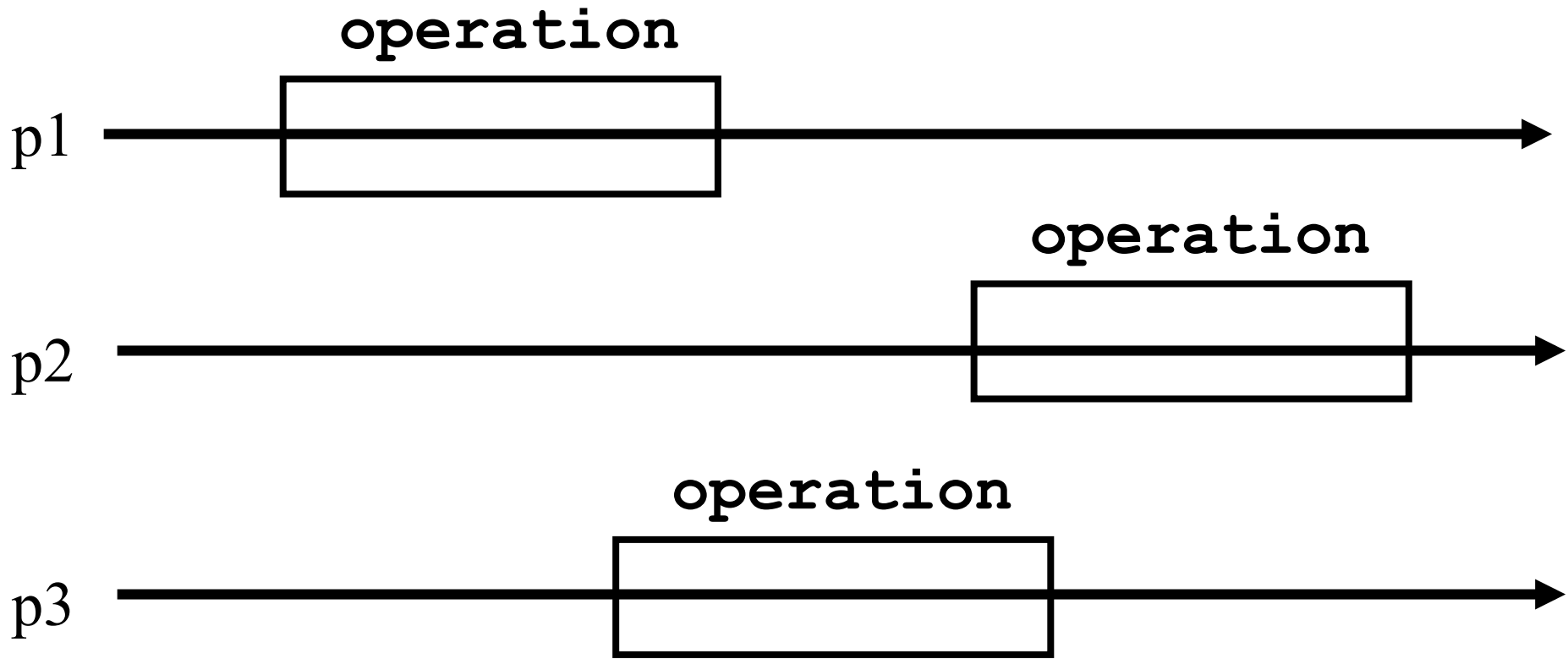




# On objects and processes

- Processes execute local computation or access shared objects through their ***operations***
- Every operation is expected to return a reply

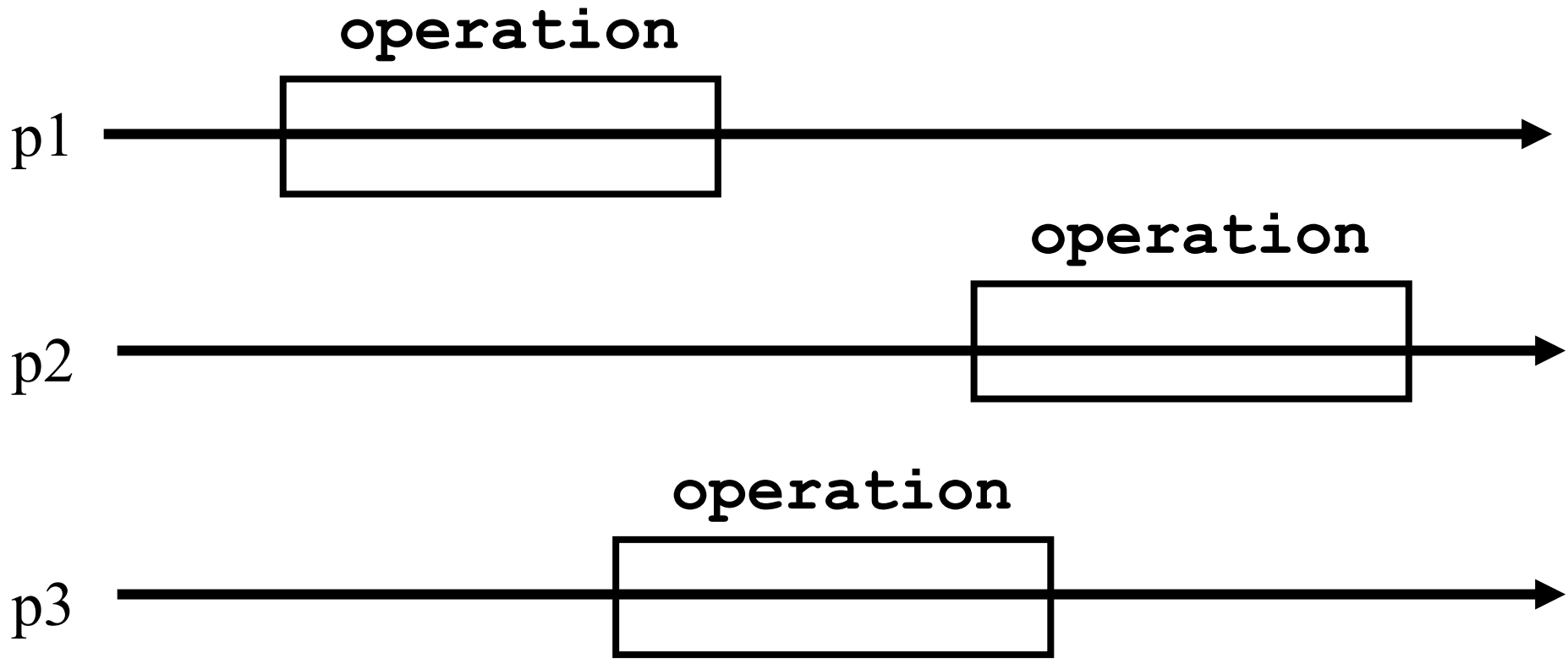
# Processes



# On objects and processes

- ***Sequentiality*** means here that, after invoking an operation  $op1$  on some object  $O1$ , a process does not invoke a new operation (on the same or on some other object) until it receives the reply for  $op1$
- ***Remark.*** Sometimes we talk about operations when we should be talking about operation invocations

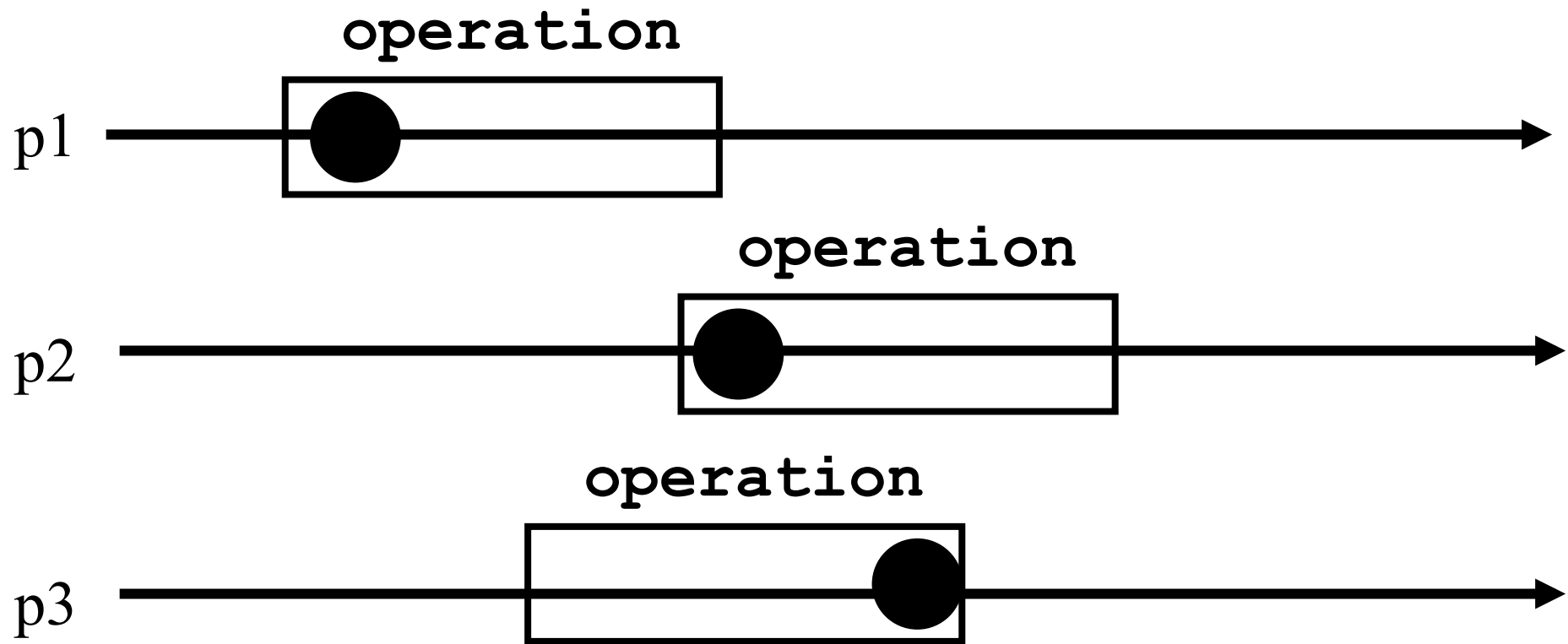
# Processes



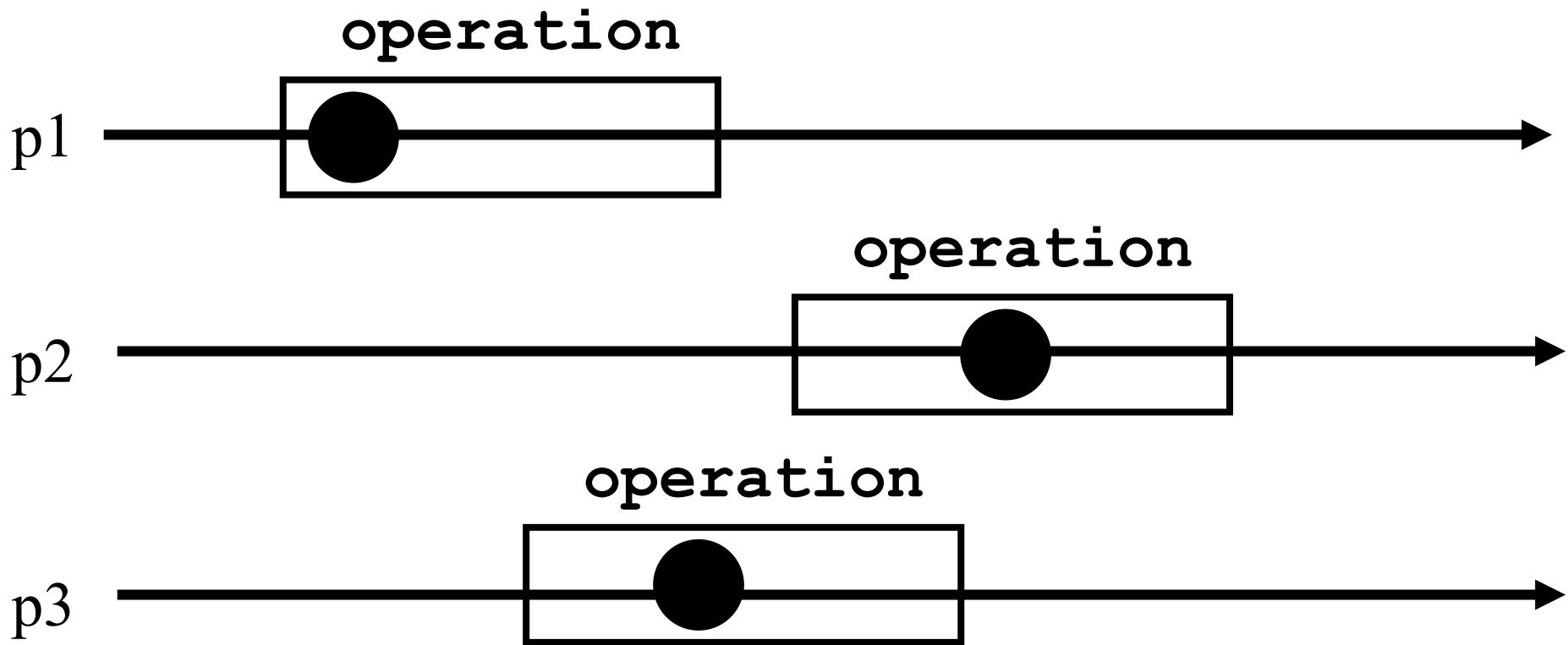
# Atomicity

- Every operation appears to execute at some indivisible point in time (called linearization point) between the invocation and reply time events

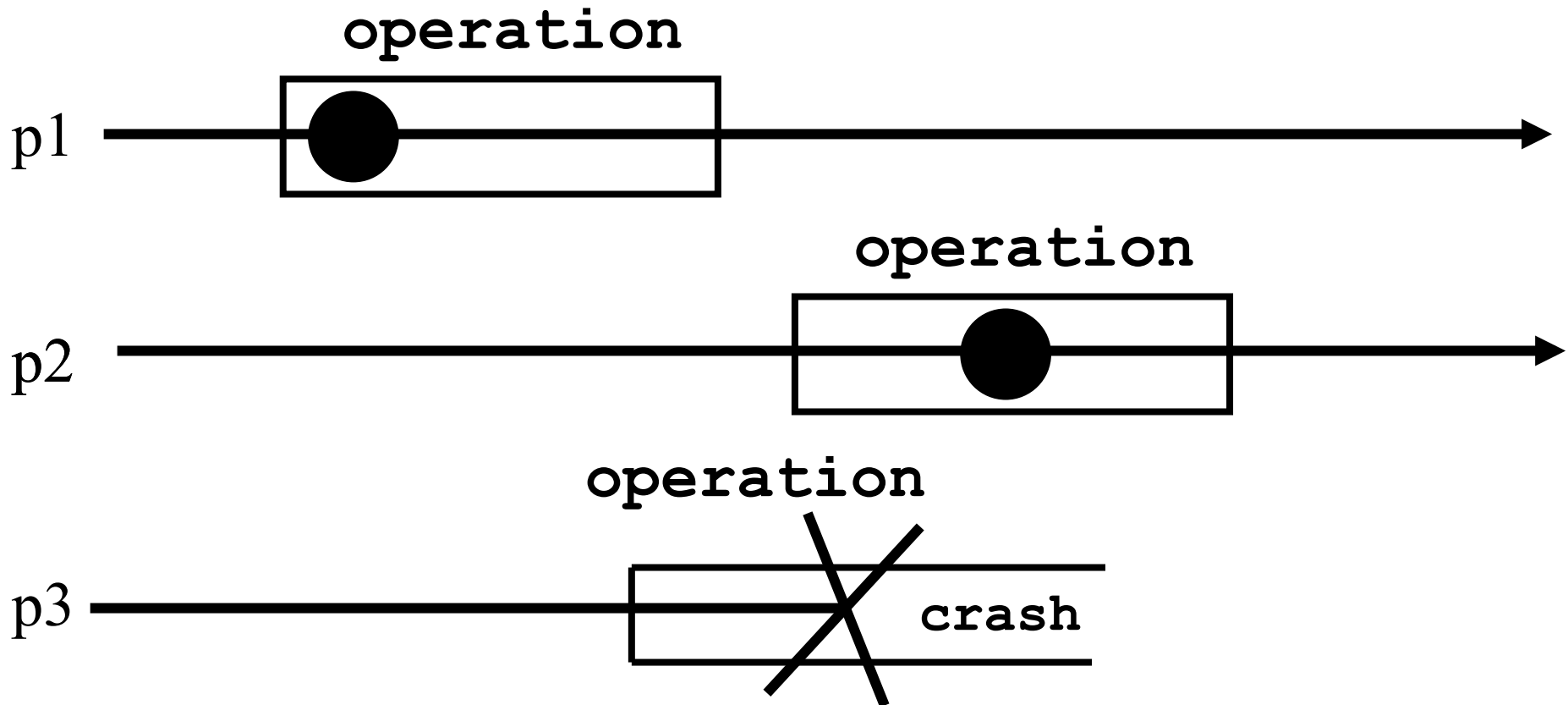
# Atomicity



# Atomicity

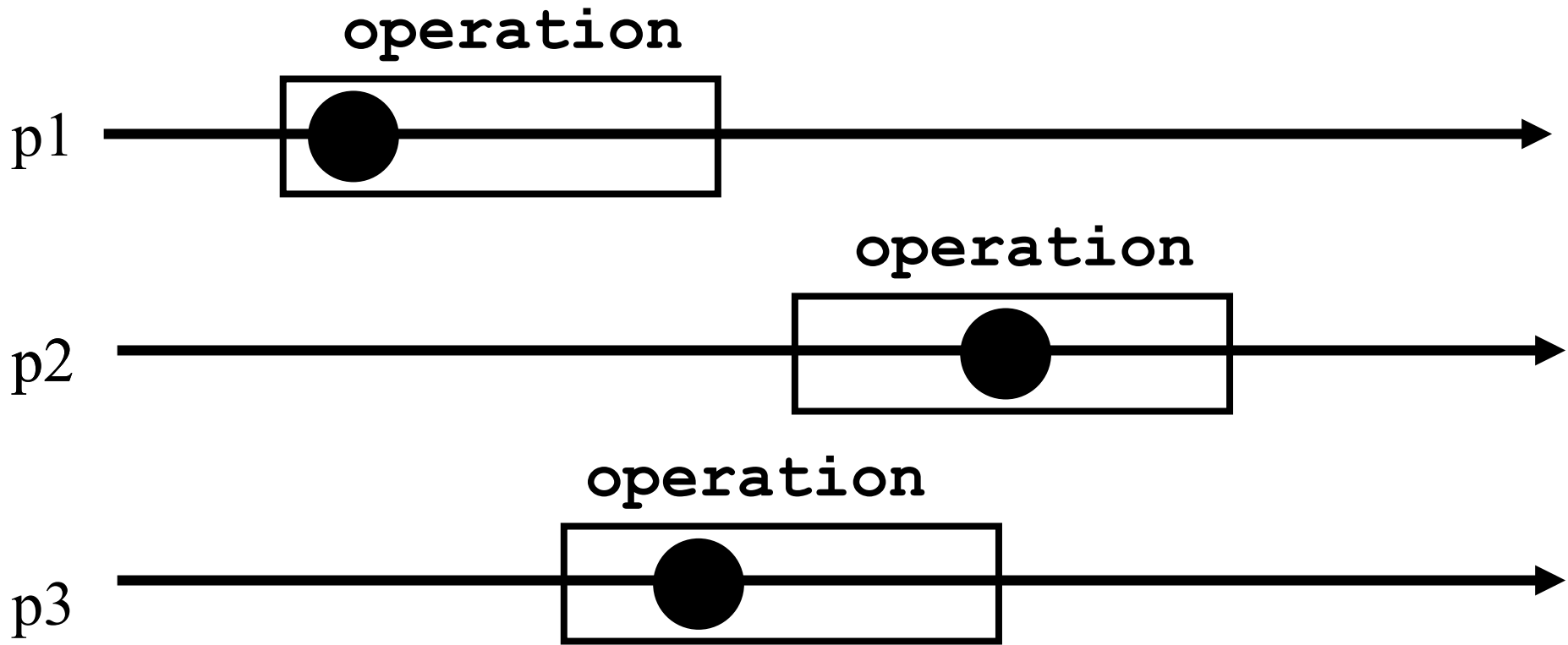


# Atomicity (the crash case)

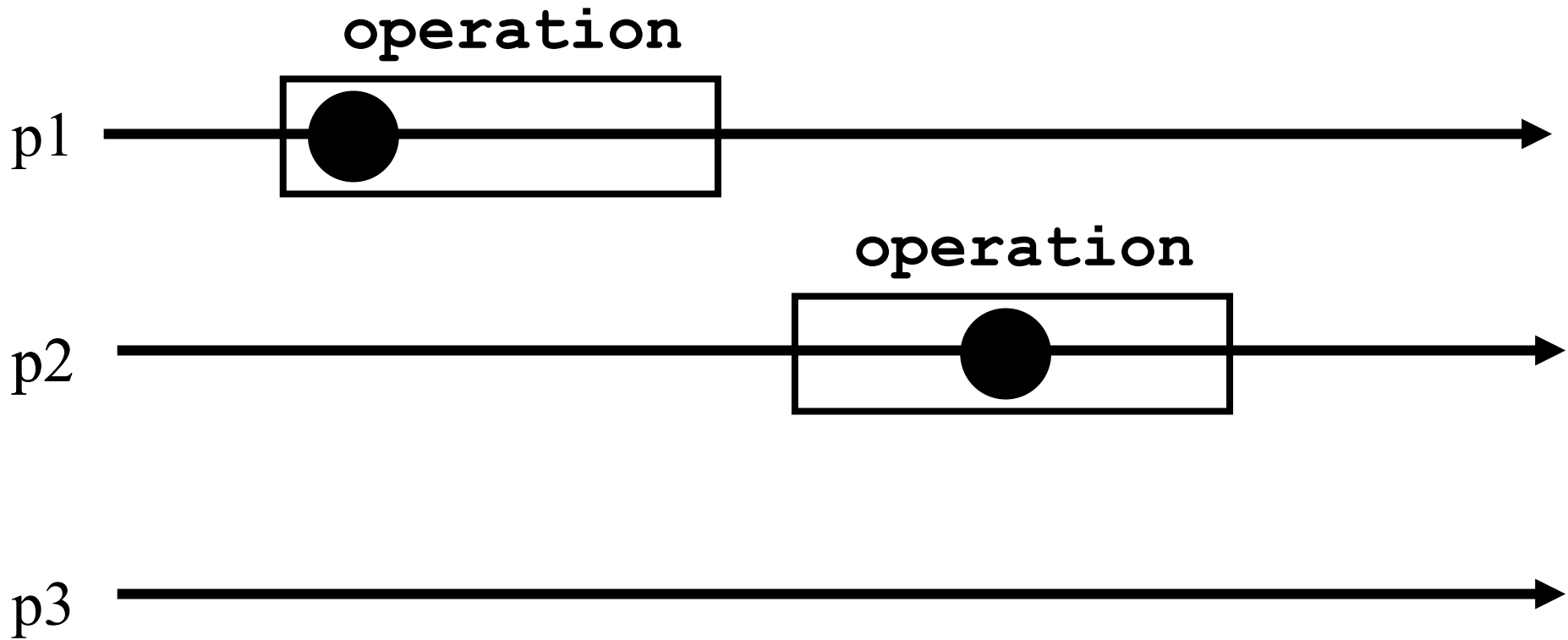




# Atomicity (the crash case)



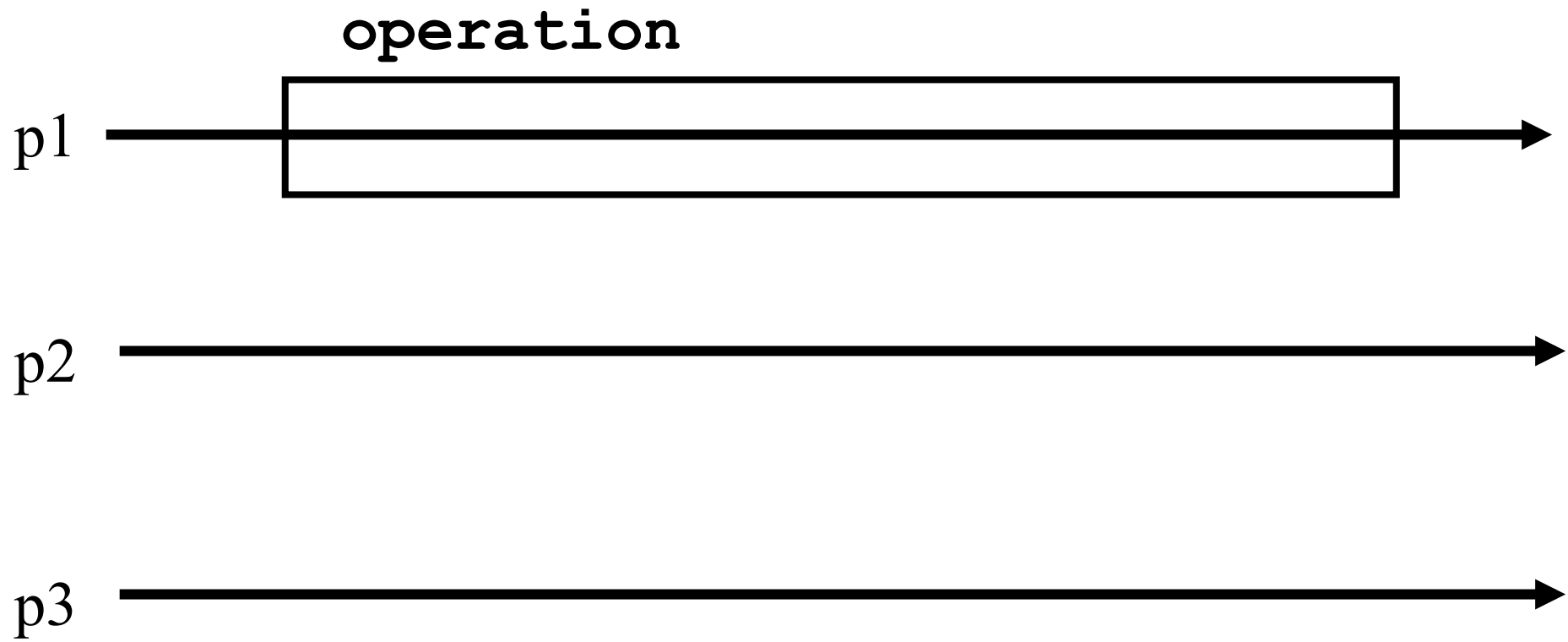
# Atomicity (the crash case)



# Wait-freedom

- Any correct process that invokes an operation eventually gets a reply, no matter what happens to the other processes (crash or very slow)

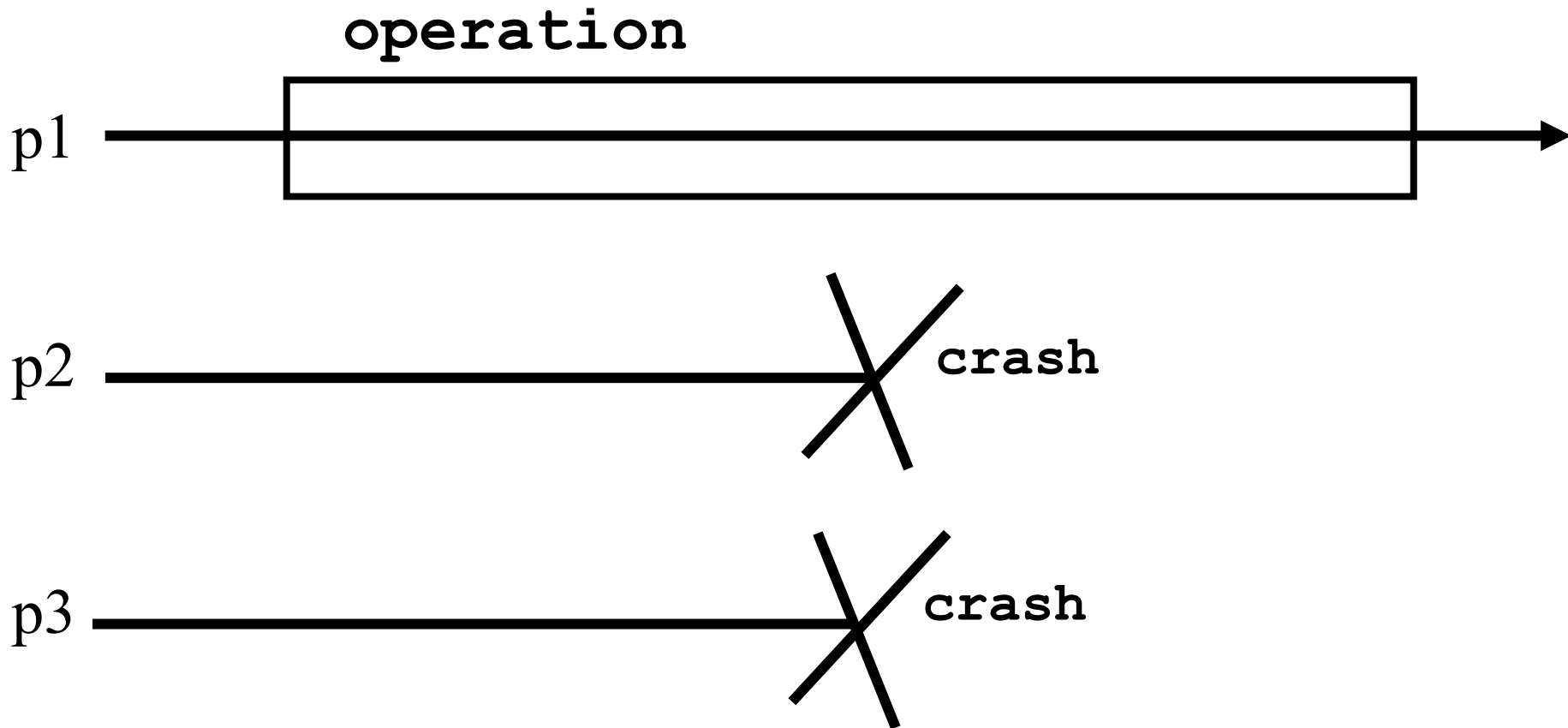
# Wait-freedom



# Wait-freedom

- ☛ Wait-freedom conveys the robustness of the implementation
- ☛ With a wait-free implementation, a process gets replies despite the crash of the  $n-1$  other processes
- ☛ Note that this precludes implementations based on locks (mutual exclusion)

# Wait-freedom



# Roadmap

- *Model*
  - *Processes and objects*
  - *Atomicity and wait-freedom*
- *Examples*
- *Content*

# Motivation

- Most synchronization primitives (problems) can be precisely expressed as atomic objects (implementations)
- Studying how to ensure robust synchronization boils down to studying wait-free atomic object implementations



# Example 1

- The reader/writer synchronization problem corresponds to the *register* object
- Basically, the processes need to read or write a shared data structure such that the value read by a process at a time  $t$ , is the last value written before  $t$

# ***Register***

- ▣ A ***register*** has two operations: ***read()*** and ***write()***
- ▣ We assume that a ***register*** contains an integer for presentation simplicity, i.e., the value stored in the ***register*** is an integer, denoted by  $x$  (initially 0)

# ***Sequential specification***

- Sequential specification

- ***read()***

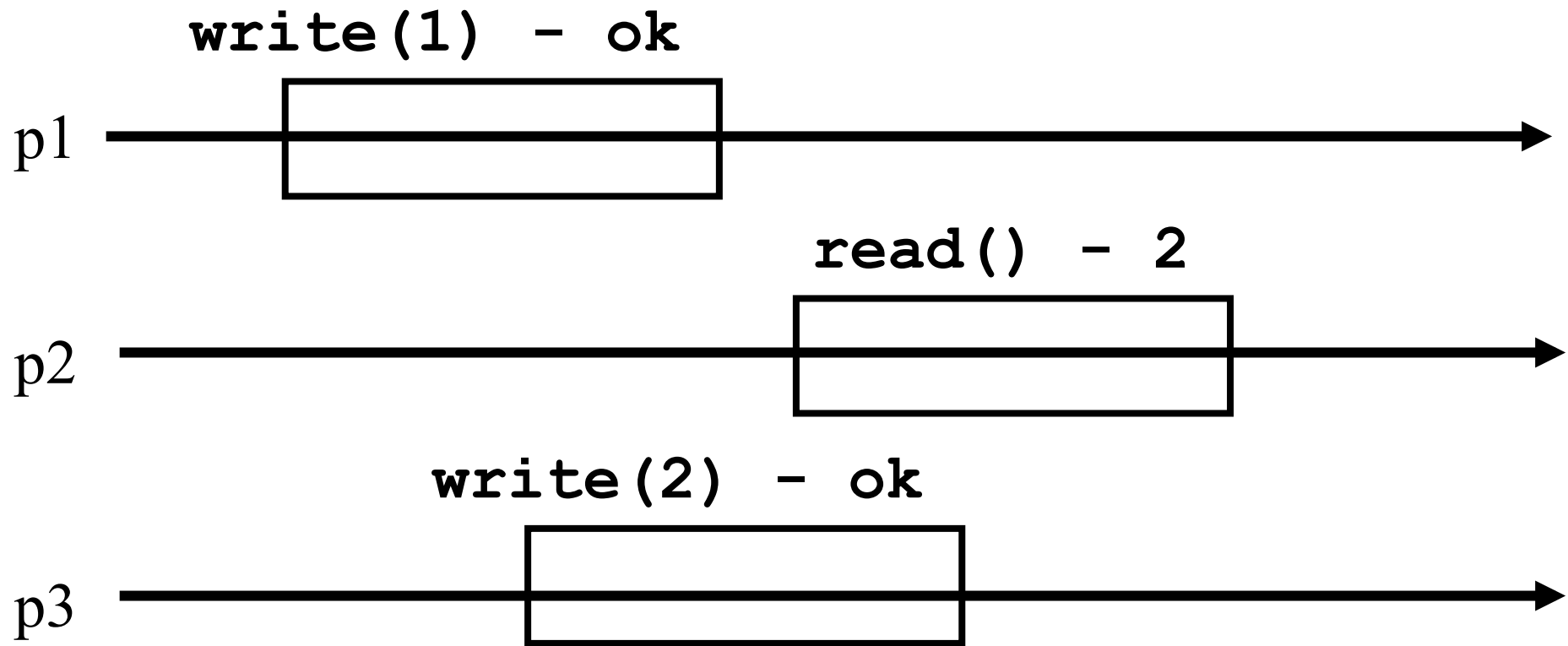
- return(x)

- ***write(v)***

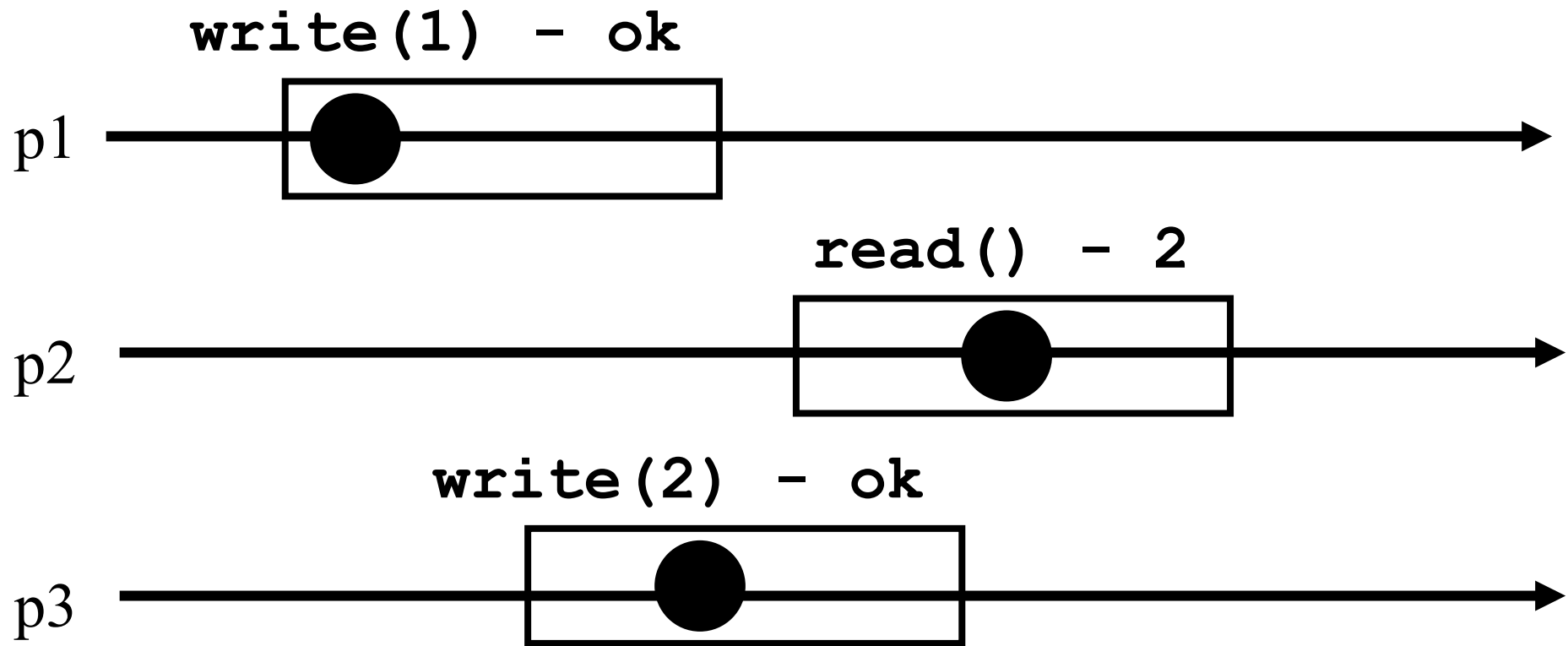
- $x \leftarrow v;$

- return(ok)

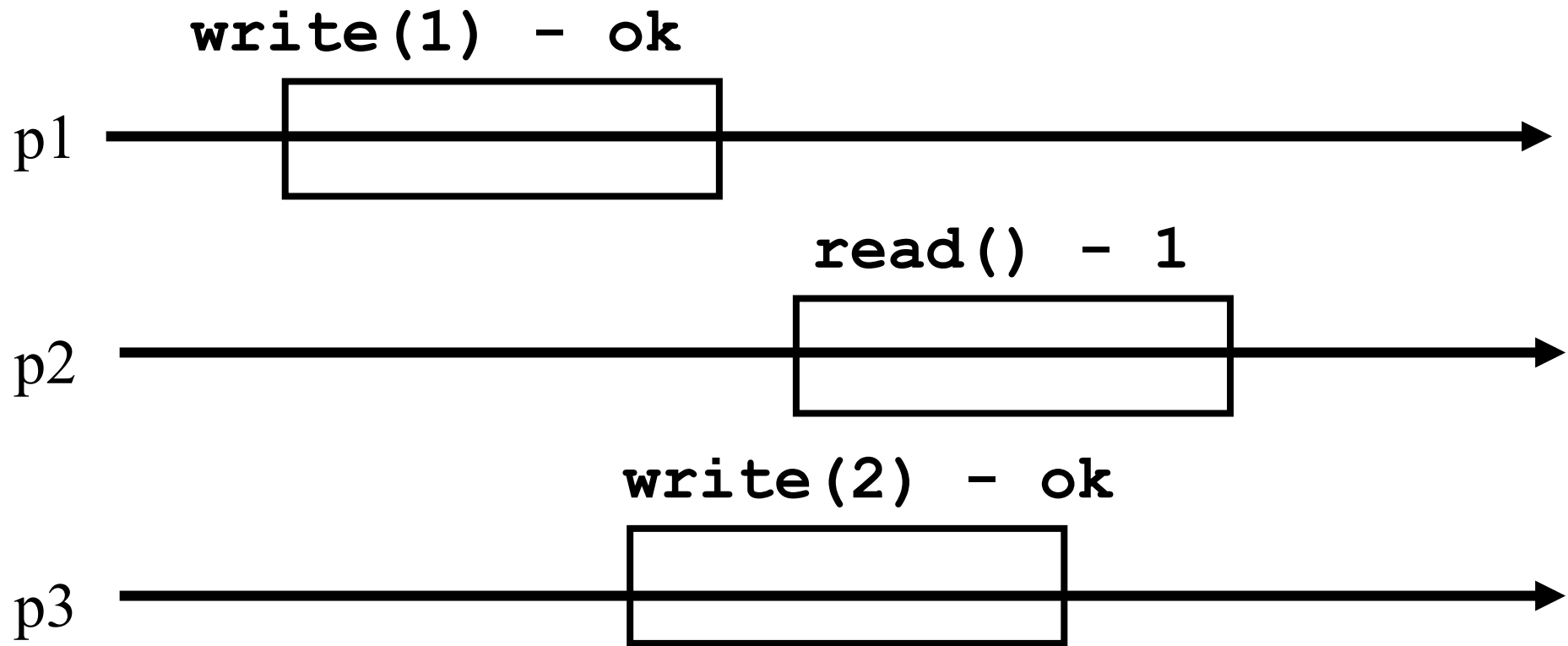
# Atomicity?



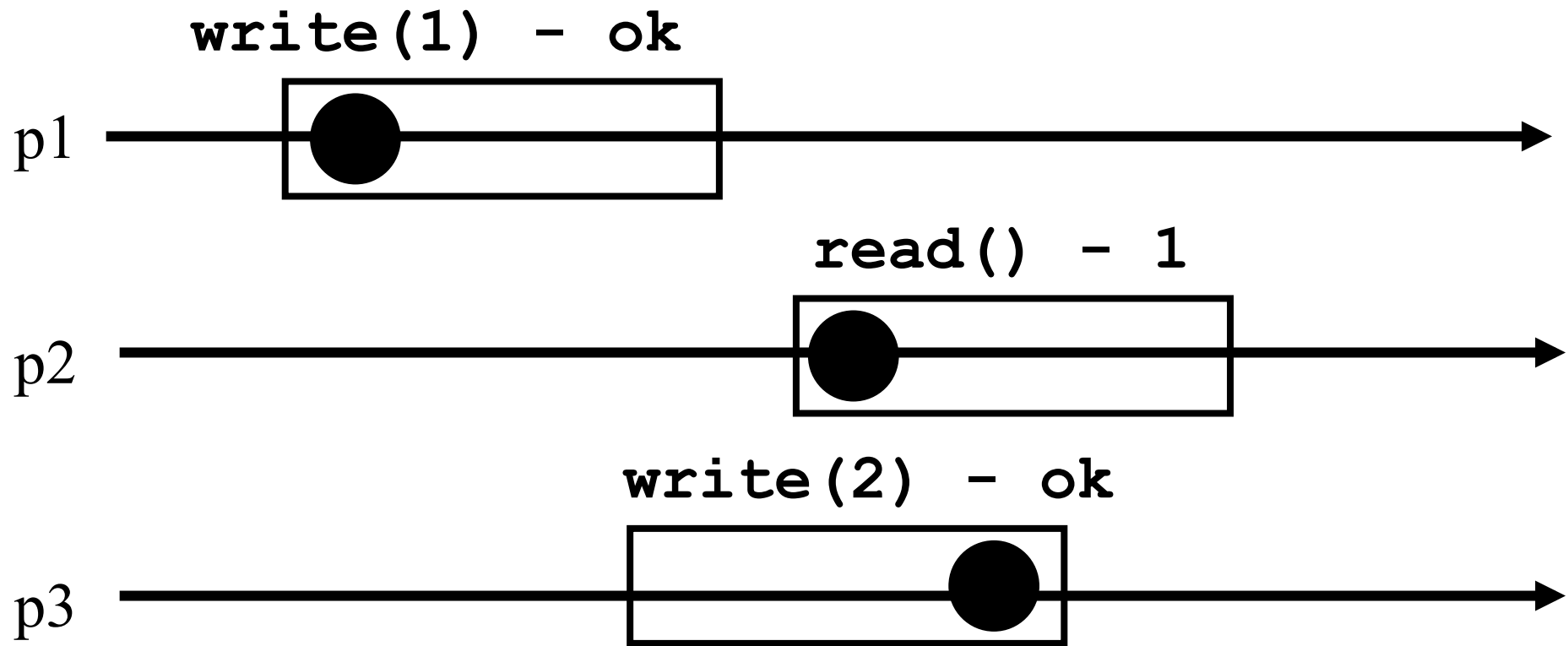
# Atomicity?



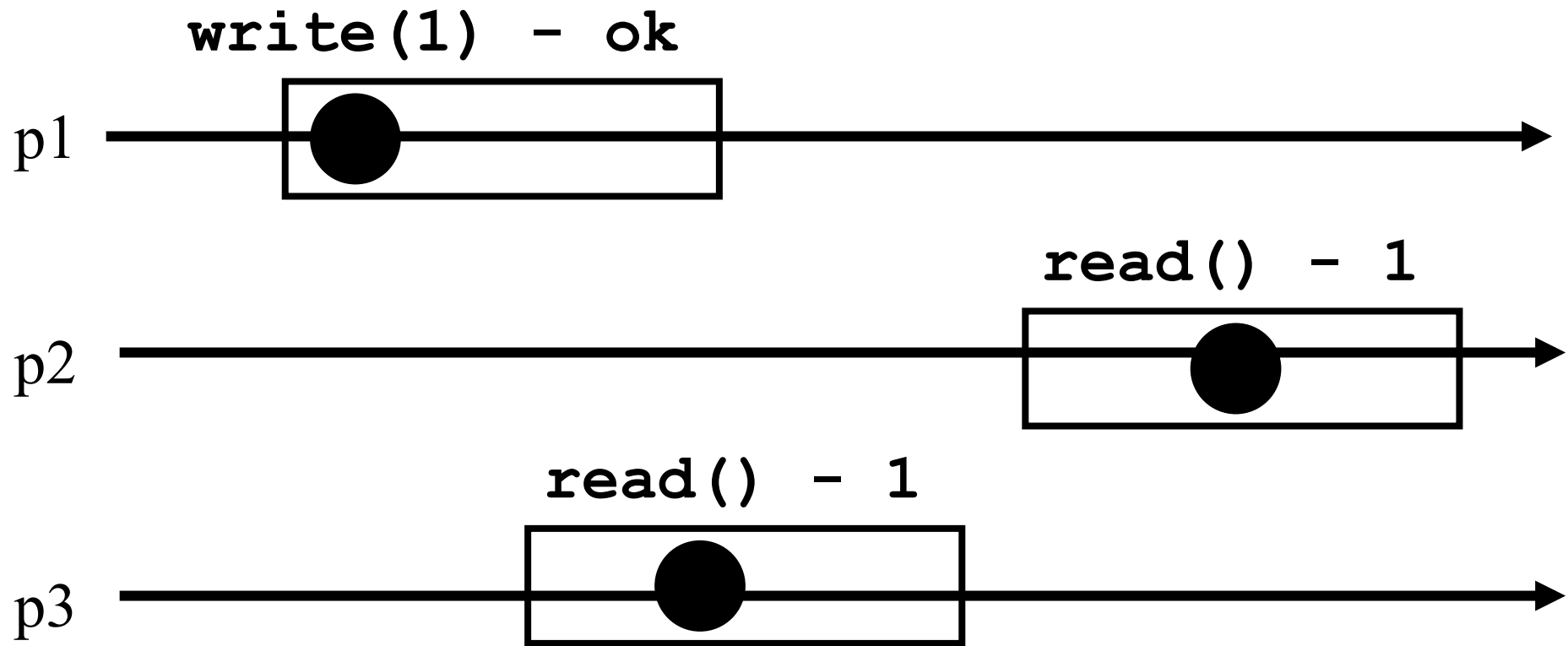
# Atomicity?



# Atomicity?

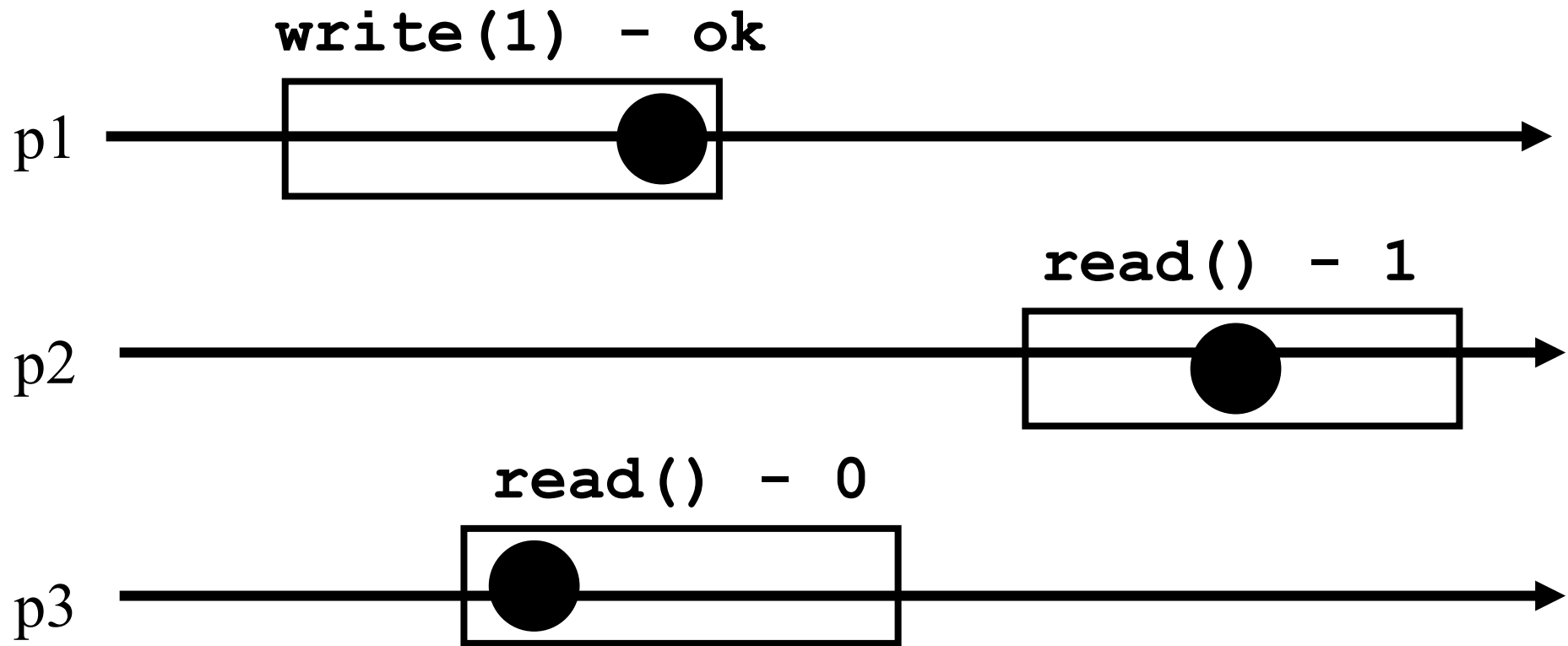


# Atomicity?

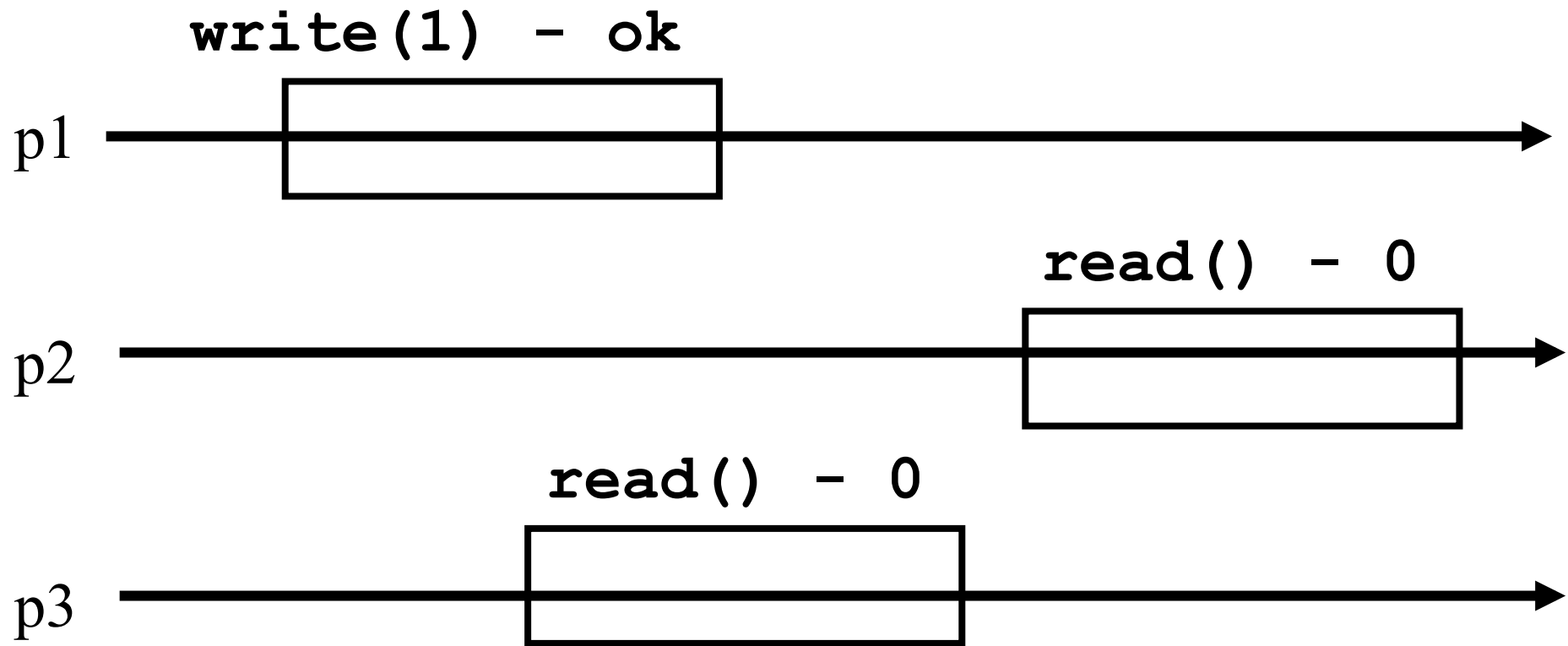




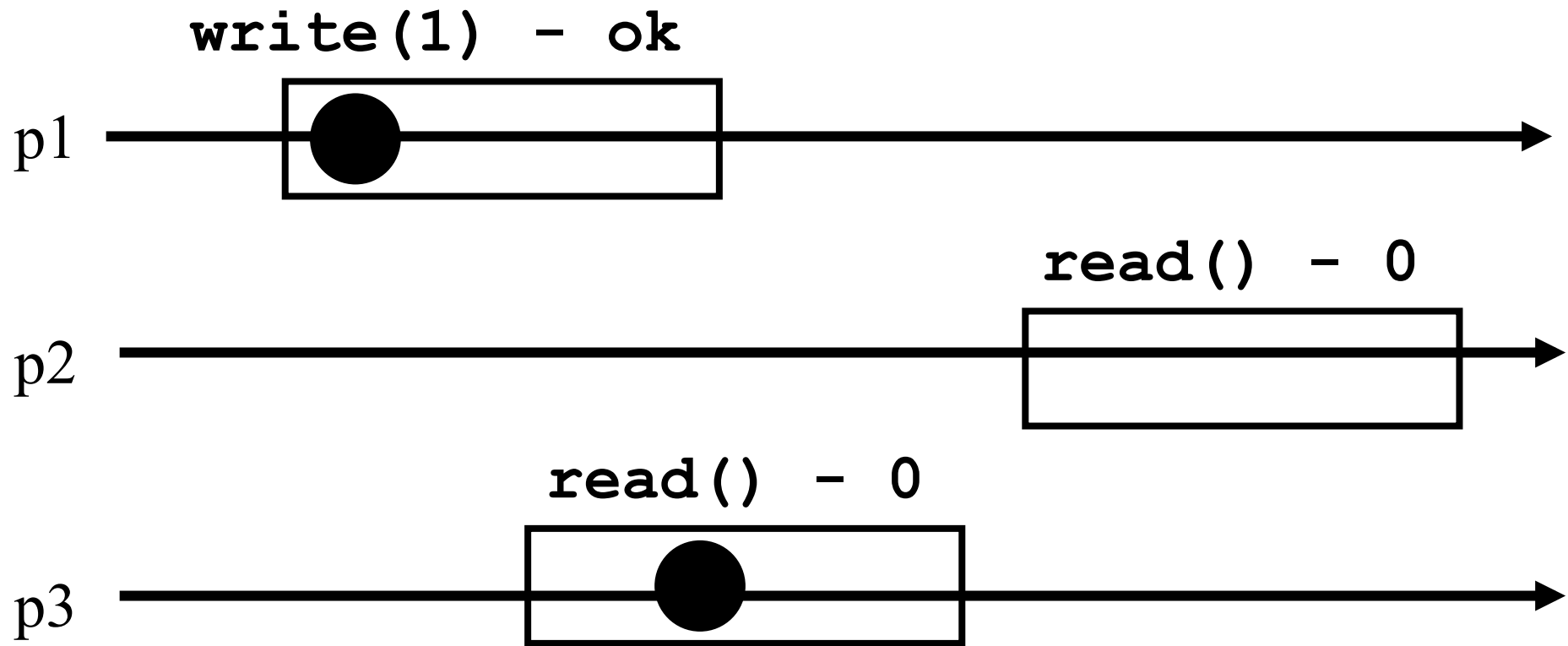
# Atomicity?



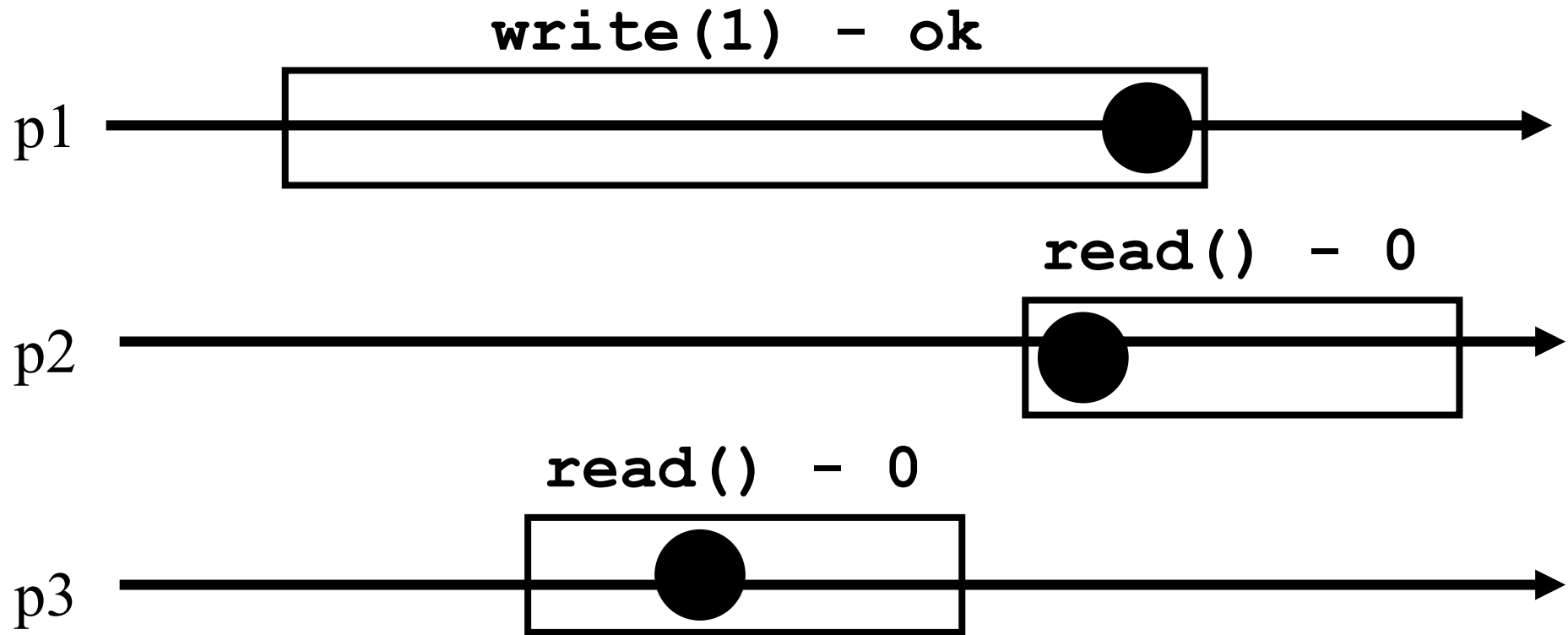
# Atomicity?



# Atomicity?

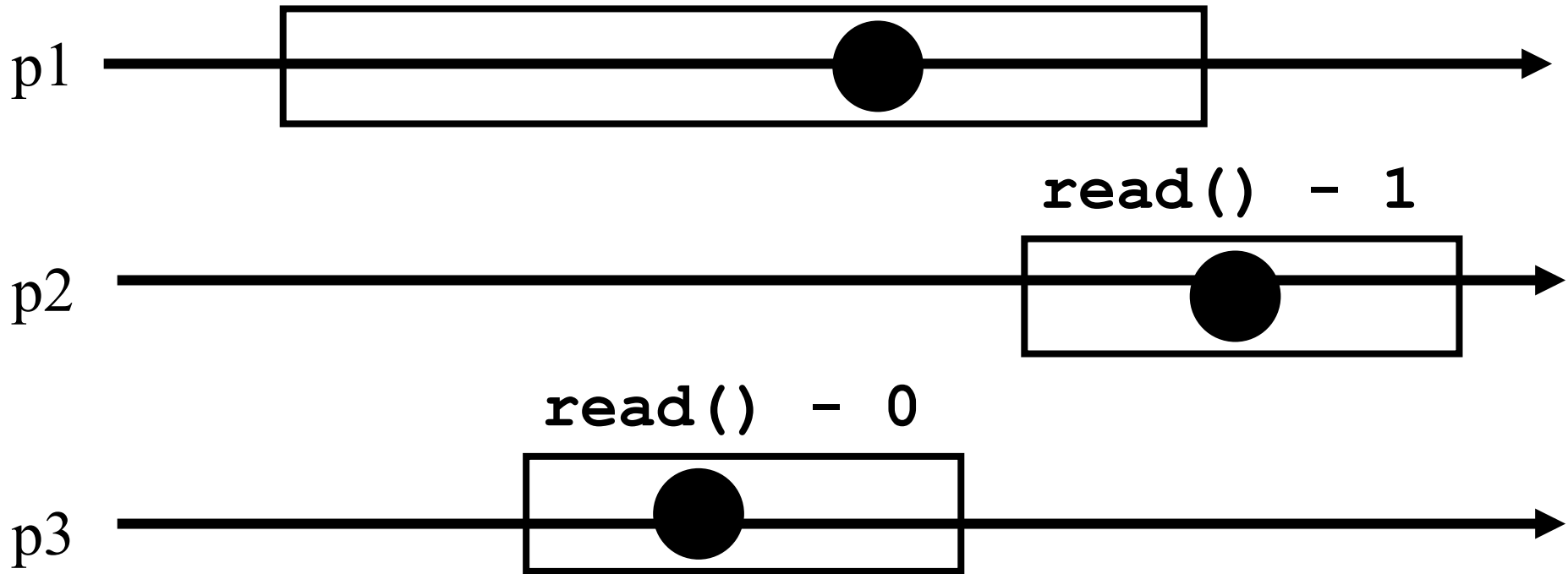


# Atomicity?



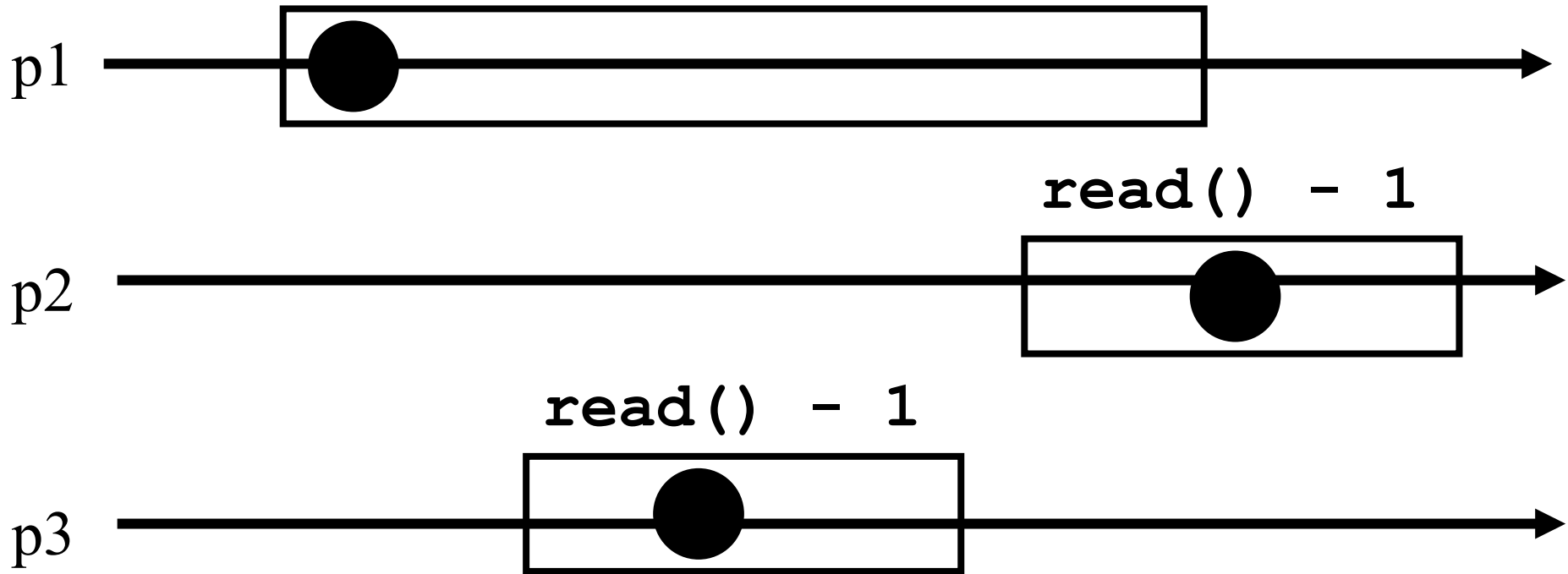
# Atomicity?

`write(1) - ok`



# Atomicity?

`write(1) - ok`



## Example 2

- The producer/consumer synchronization problem corresponds to the ***queue*** object
- Producer processes create items that need to be used by consumer processes
- An item cannot be consumed by two processes and the first item produced is the first consumed

# *Queue*

- A *queue* has two operations: *enqueue()* and *dequeue()*
- We assume that a *queue internally* maintains a list  $x$  which exports operation *appends()* to put an item at the end of the list and *remove()* to remove an element from the head of the list



# ***Sequential specification***

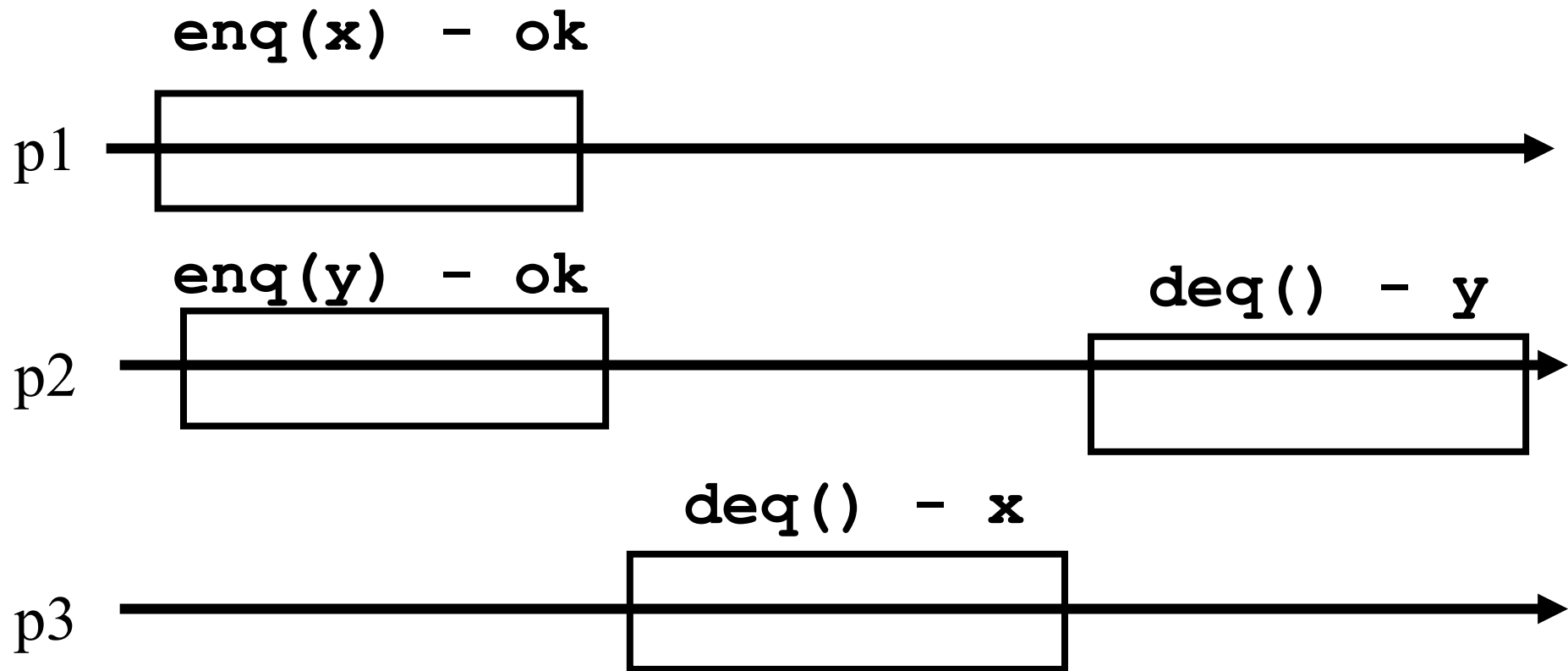
## ***• dequeue()***

- if(x=0) then return(nil);***
- else return(x.remove());***

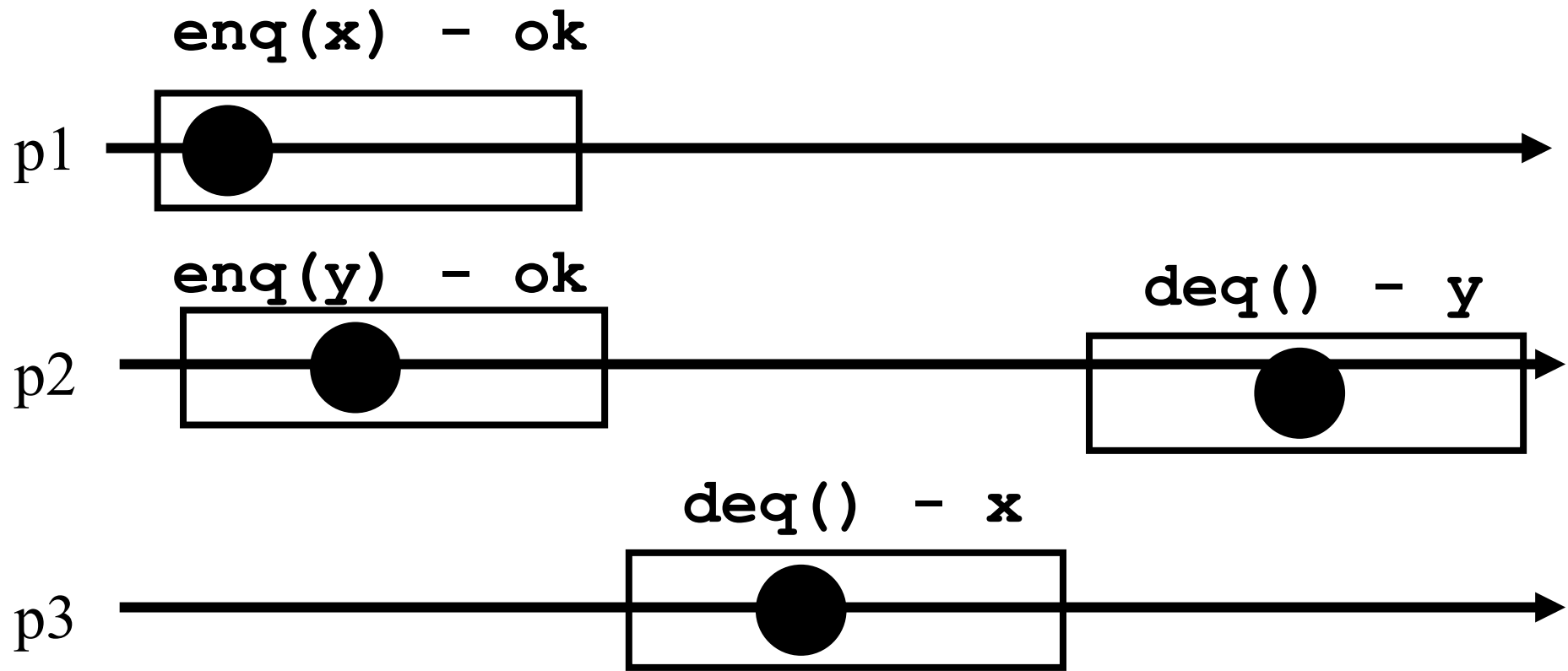
## ***• enqueue(v)***

- x.append(v);***
- return(ok)***

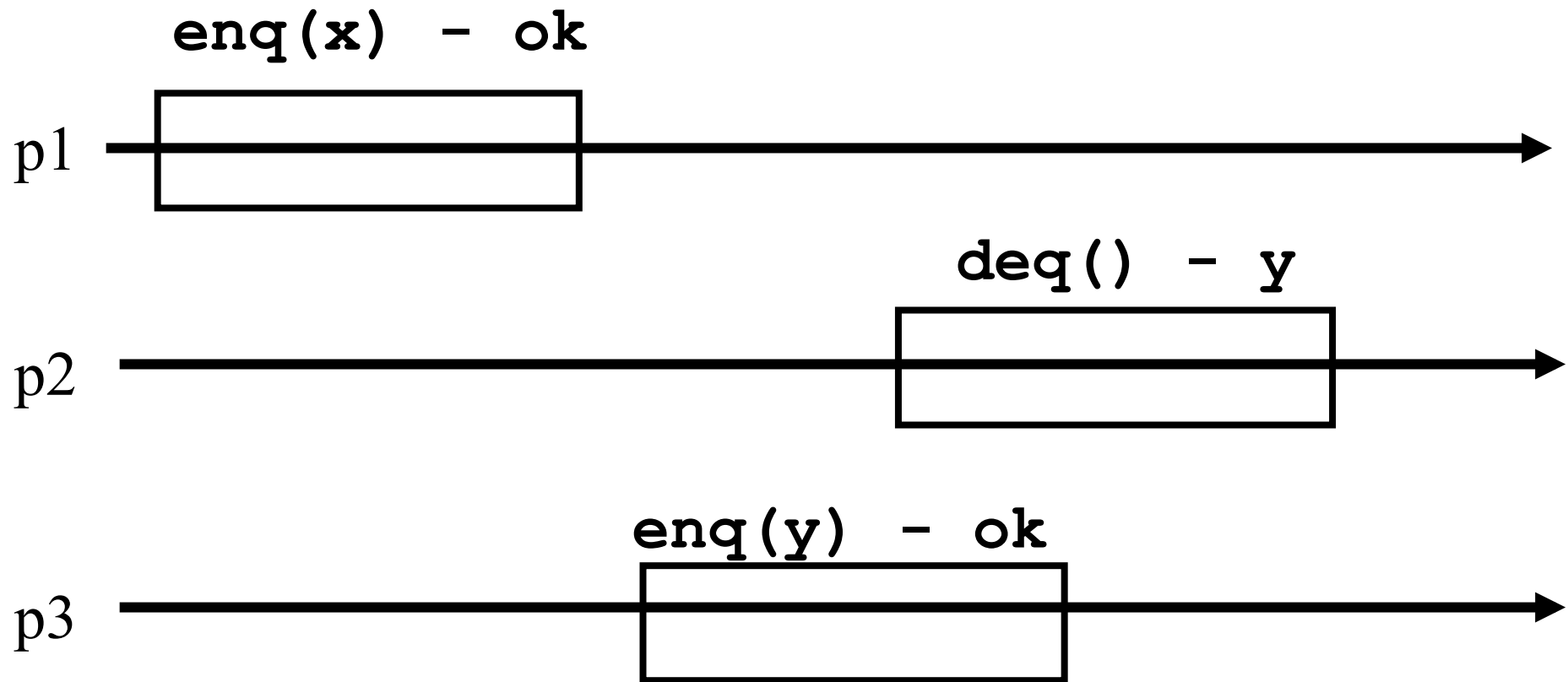
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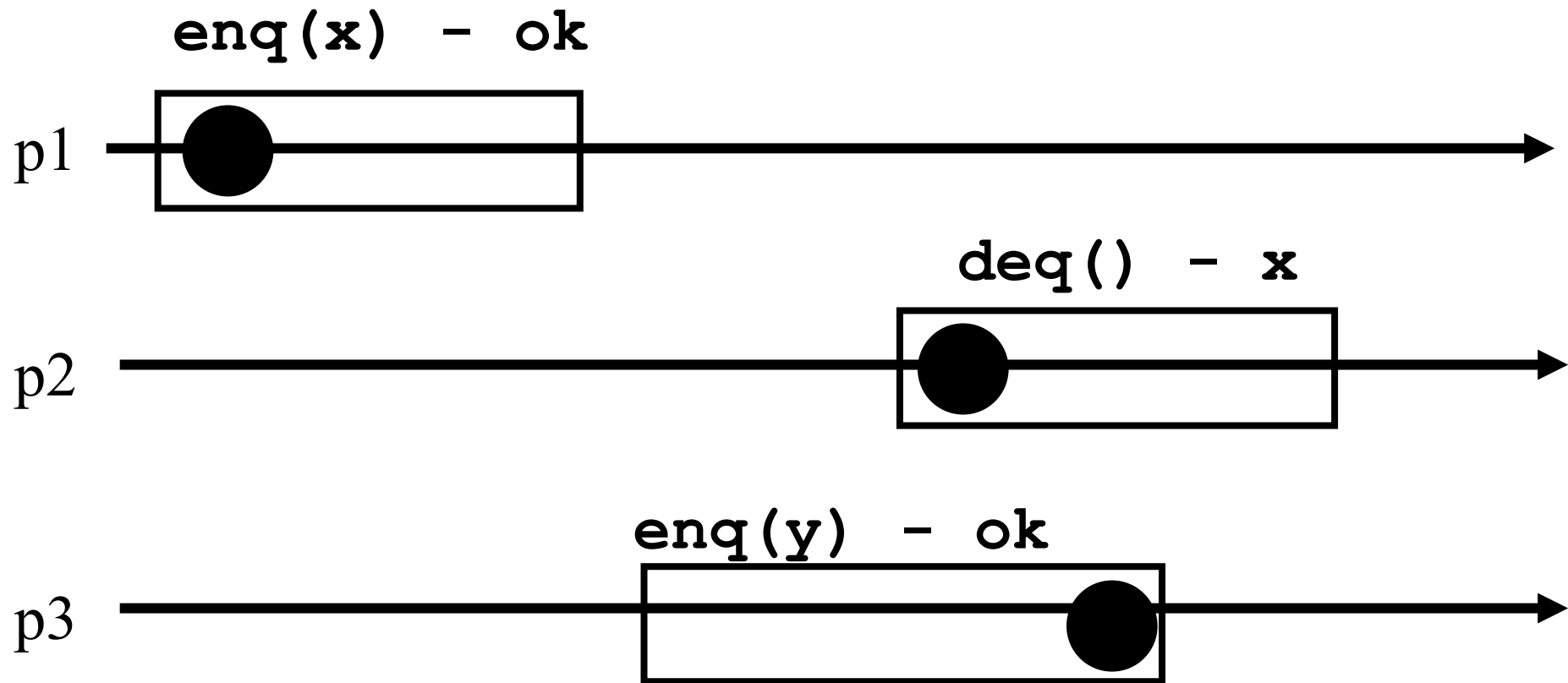
# Atomicity?



# Atomicity?



# Atomicity?



# Roadmap

- *Model*
  - *Processes and objects*
  - *Atomicity and wait-freedom*
- *Examples*
- *Content*

# ***Content***

- ☛ (1) Implementing ***registers***
- ☛ (2) The power & limitation of ***registers***
- ☛ (3) ***Universal*** objects & synchronization number
- ☛ (4) The power of ***time*** & failure detection
- ☛ (5) Tolerating ***failure*** prone objects
- ☛ (6) ***Anonymous*** implementations
- ☛ (7) ***Transaction*** memory

# **In short**

This course shows how to wait-free  
implement high-level atomic  
objects out of basic objects

Remark. Unless explicitly stated  
otherwise, objects mean atomic objects  
and implementations are wait-free